

# Development of **Non-Destructive** Beam Envelope Measurements

## *Using BPMs for Low-Beta Heavy Ion Beams in SRF Cavities*

**RIKEN Nishina Center Accelerator Advanced Group**  
**Takahiro Nishi**

Collaborators

T. Adachi, O. Kamigaito, N. Sakamoto,  
T. Watanabe and K. Yamada



# Outline

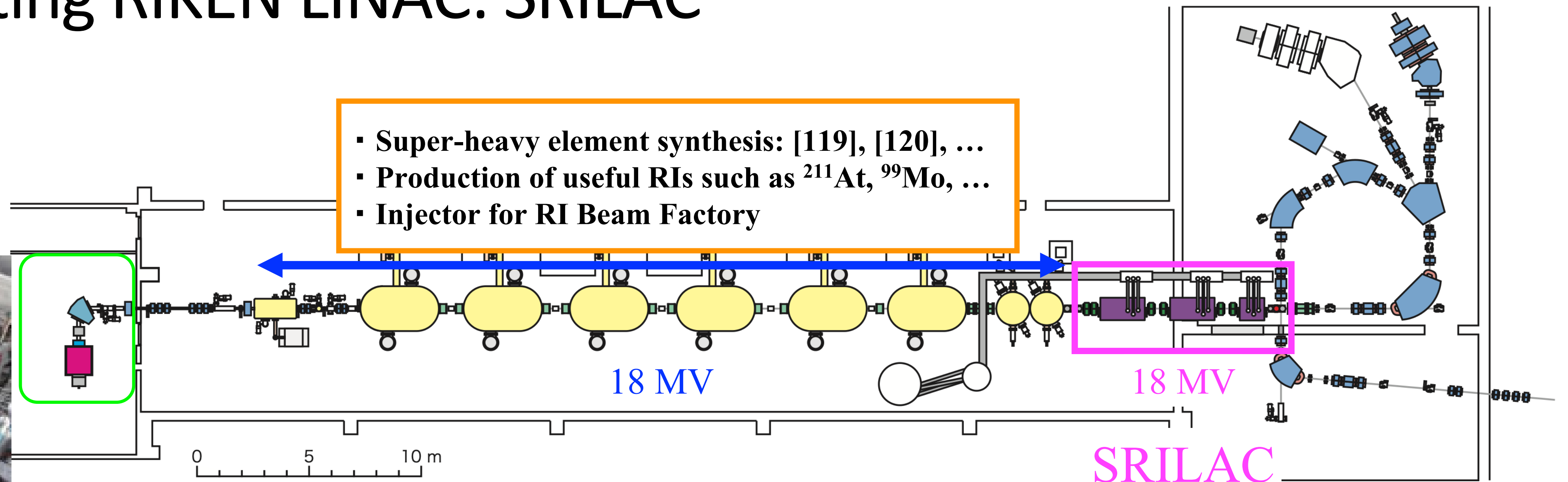
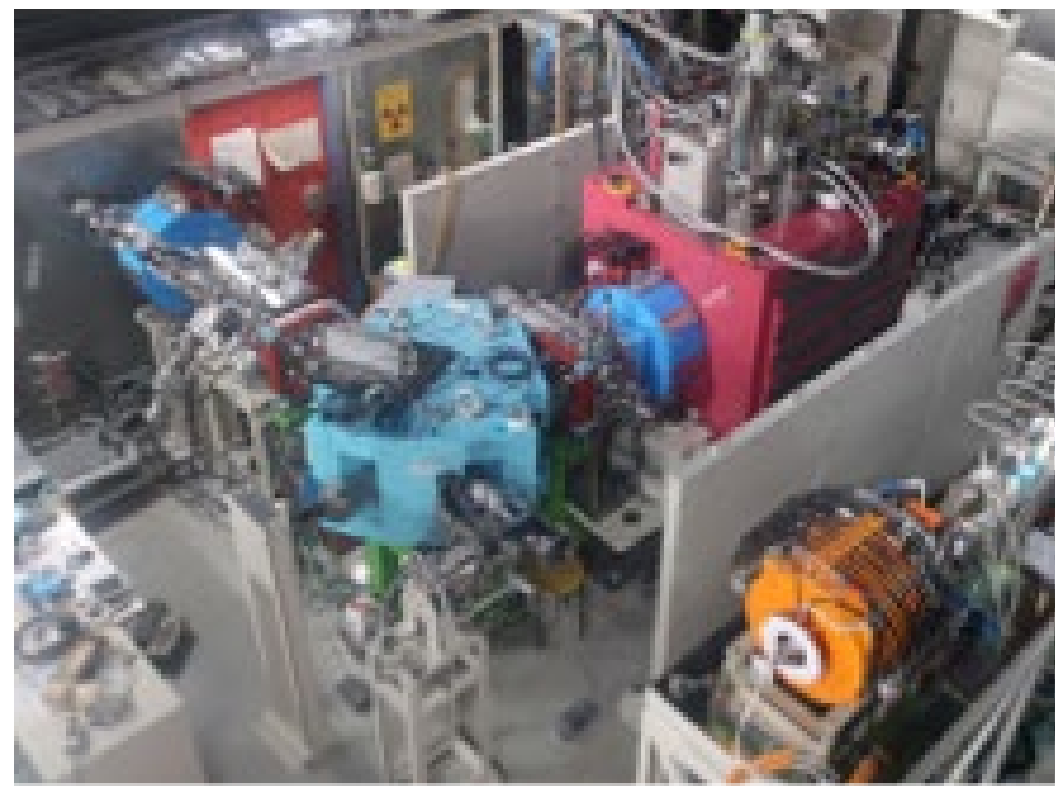
1. Introduction: SRILAC and B(E)PMs
2. Beam envelope estimation by BPM signals
3. Signal distortions caused by BPM shapes with short bunch beam
4. Improvement of sensitivity for beam emittance
5. Example of analysis with experimental data
6. Future Outlook and Summary

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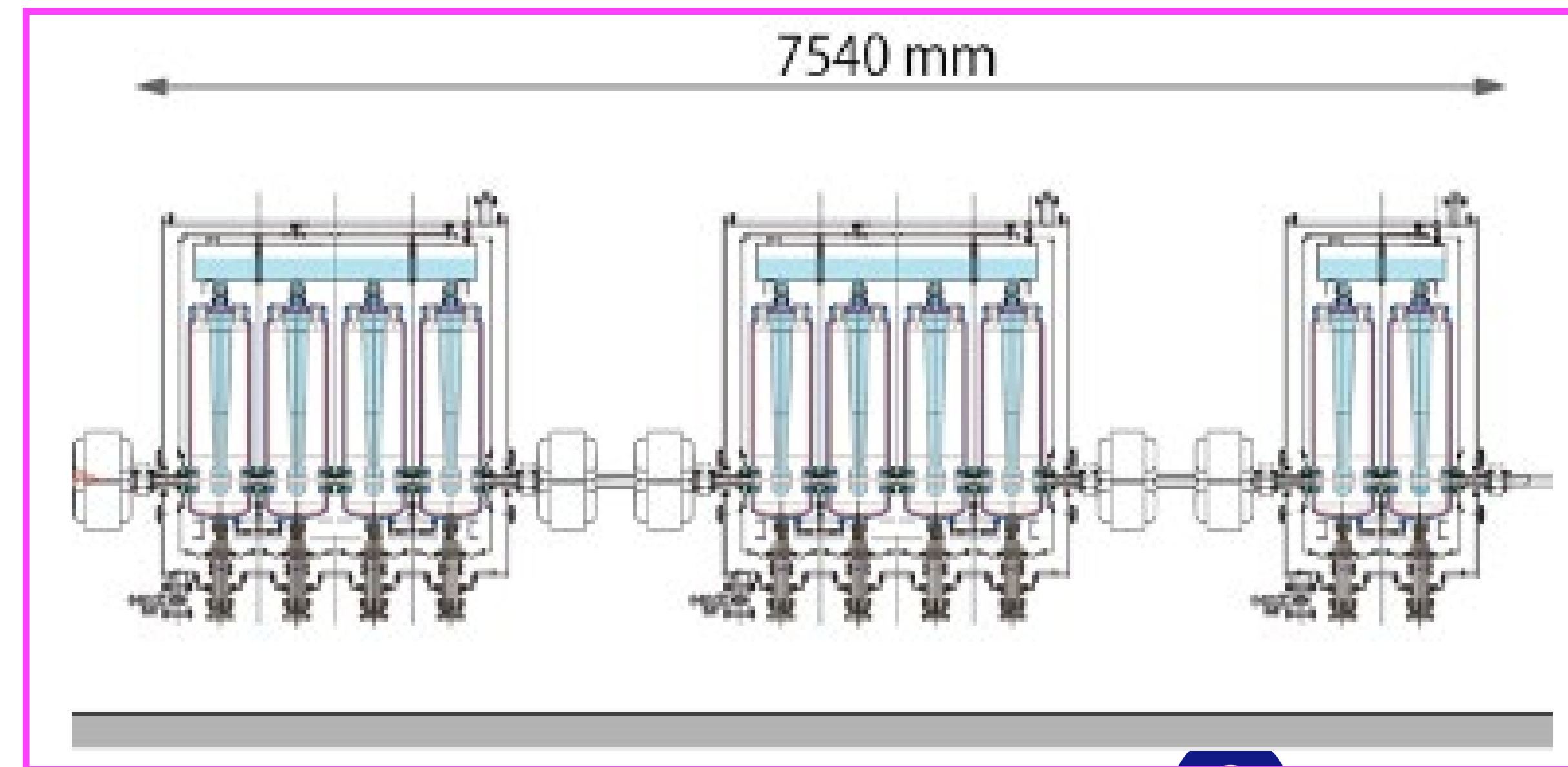
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# Superconducting RIKEN LINAC: SRILAC

28GHz SC-ECRIS

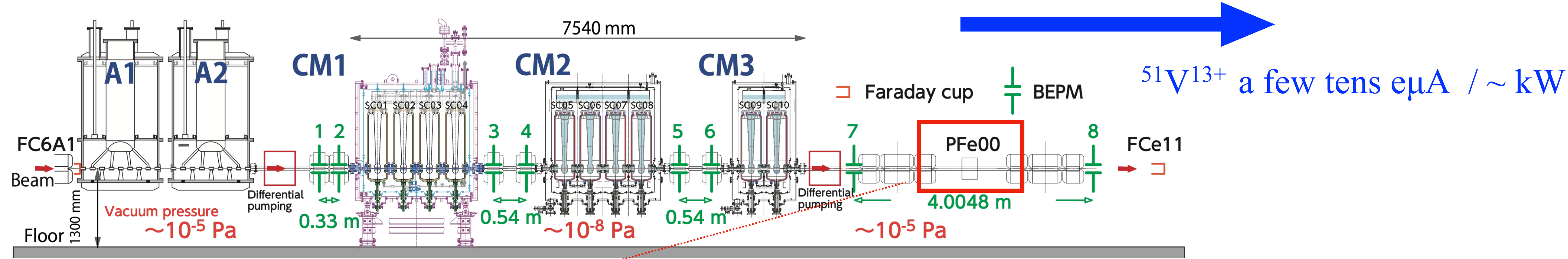


Num. of Cryomodules	3
Num. of Cavities	10 (SC-QWRs)
Frequency	73 MHz (CW)
Operating Temperature	4.5 K
$E_{\text{in}}$	3.6 MeV/u
$E_{\text{out}}$ (design)	6.5 MeV/u for $M/q = 6$ (tunable)
Total voltage (design)	~ 18 MV



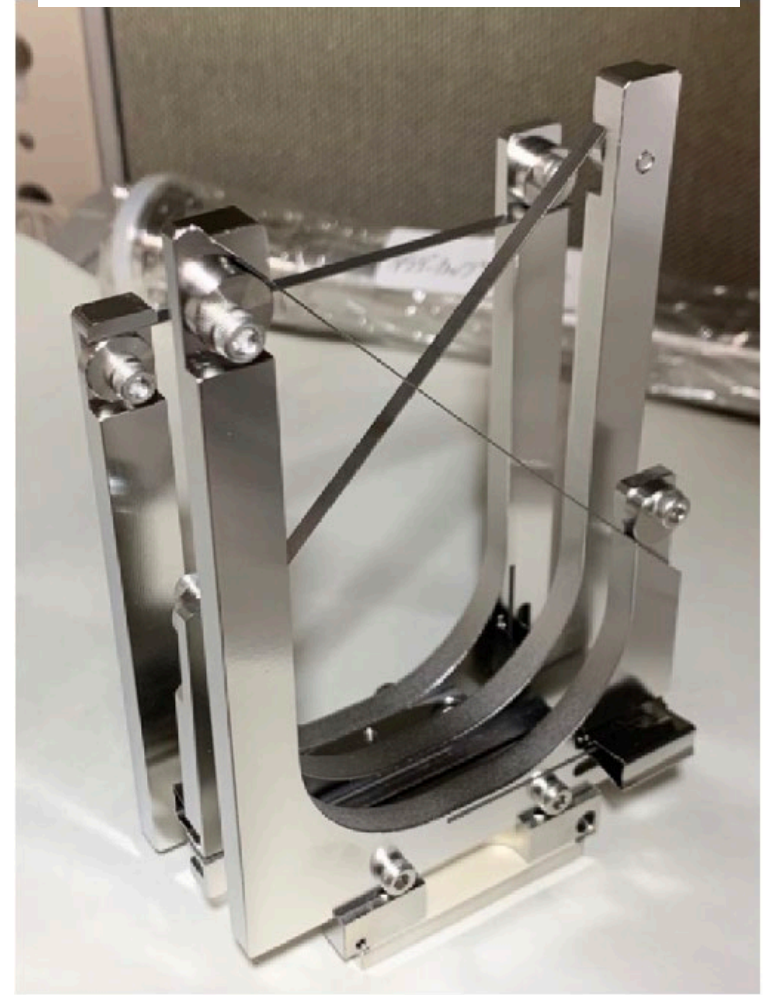


# Beam control after SRILAC: Q-scan method



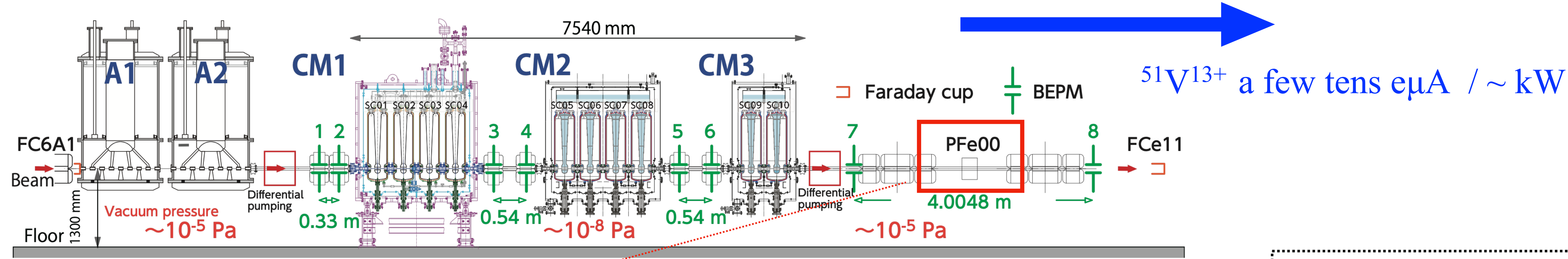
Schematic view of Superconducting RIKEN LINAC (SRILAC)

profile monitor @ e00



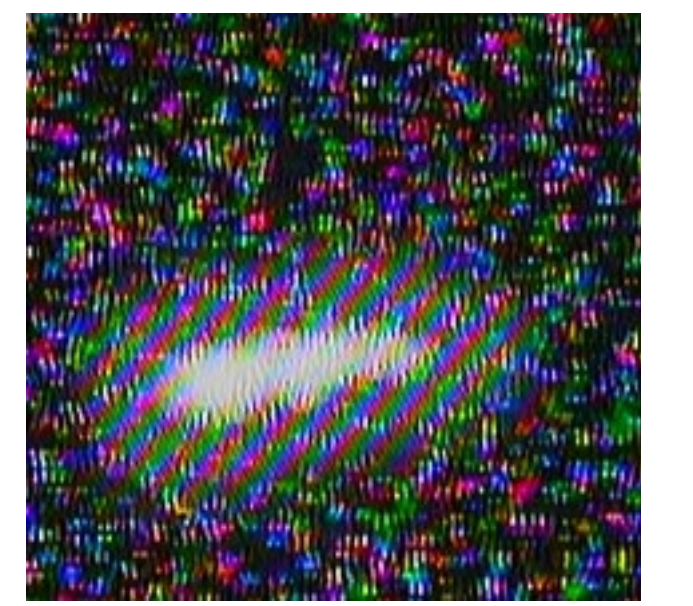
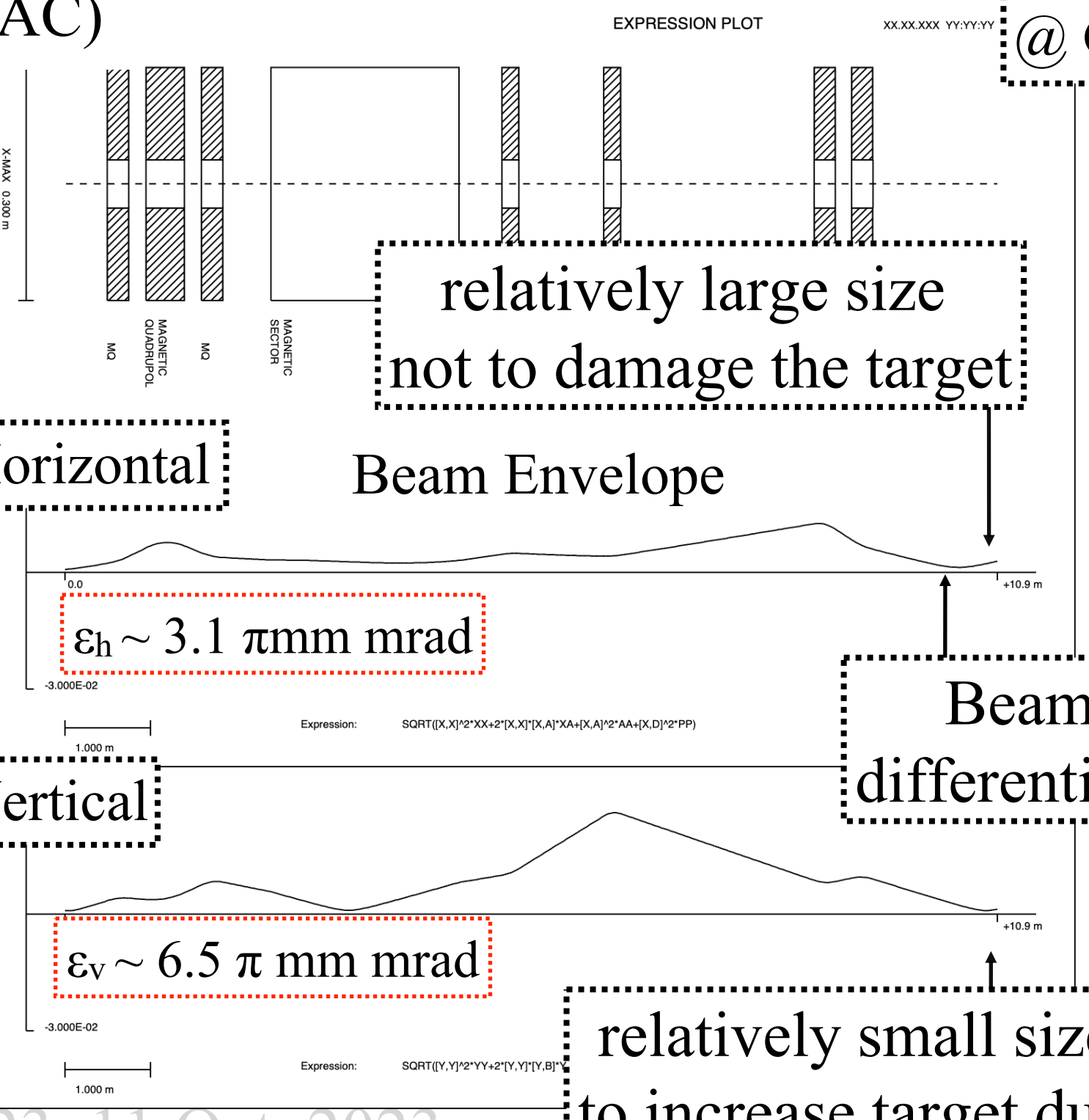
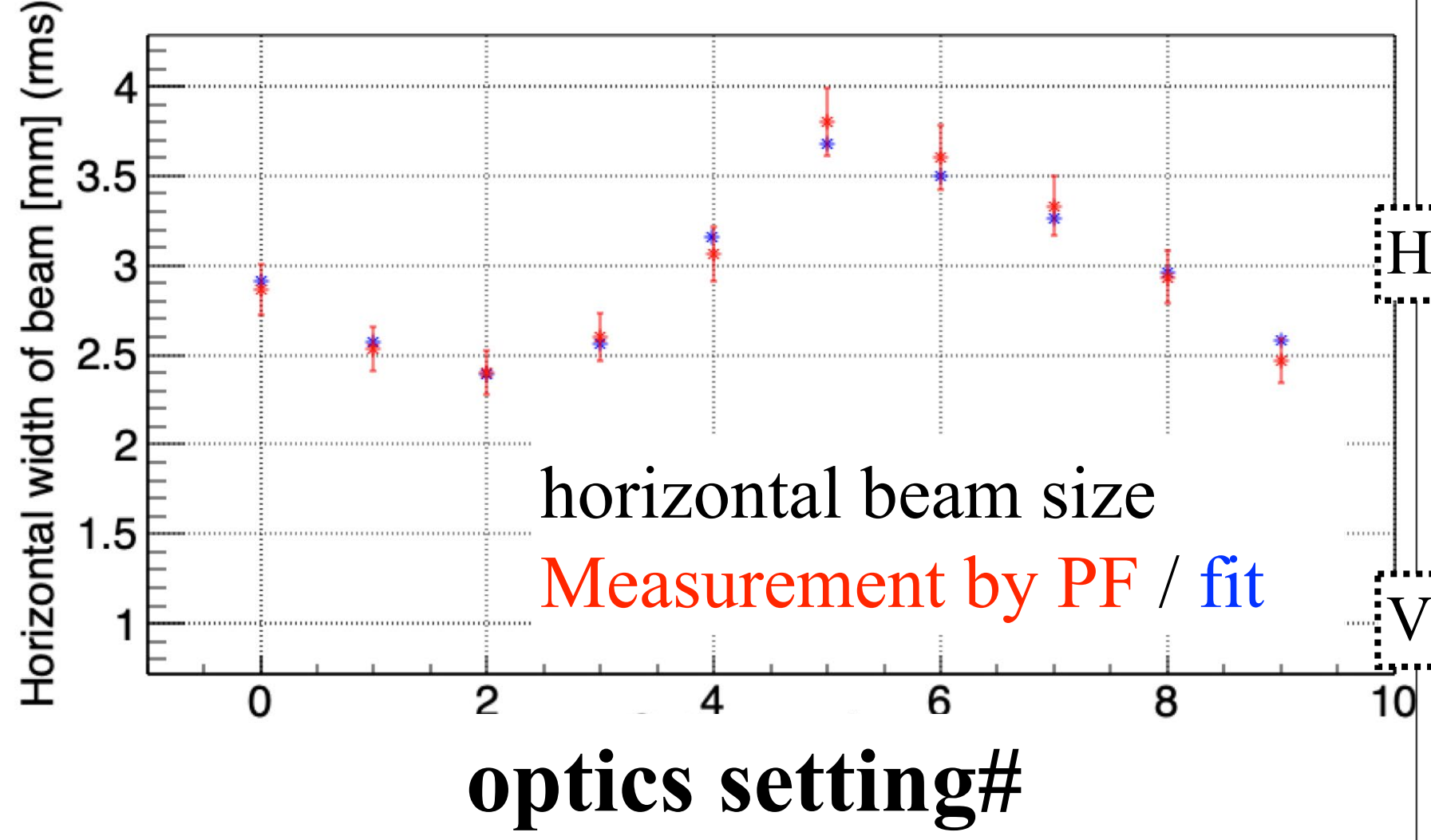
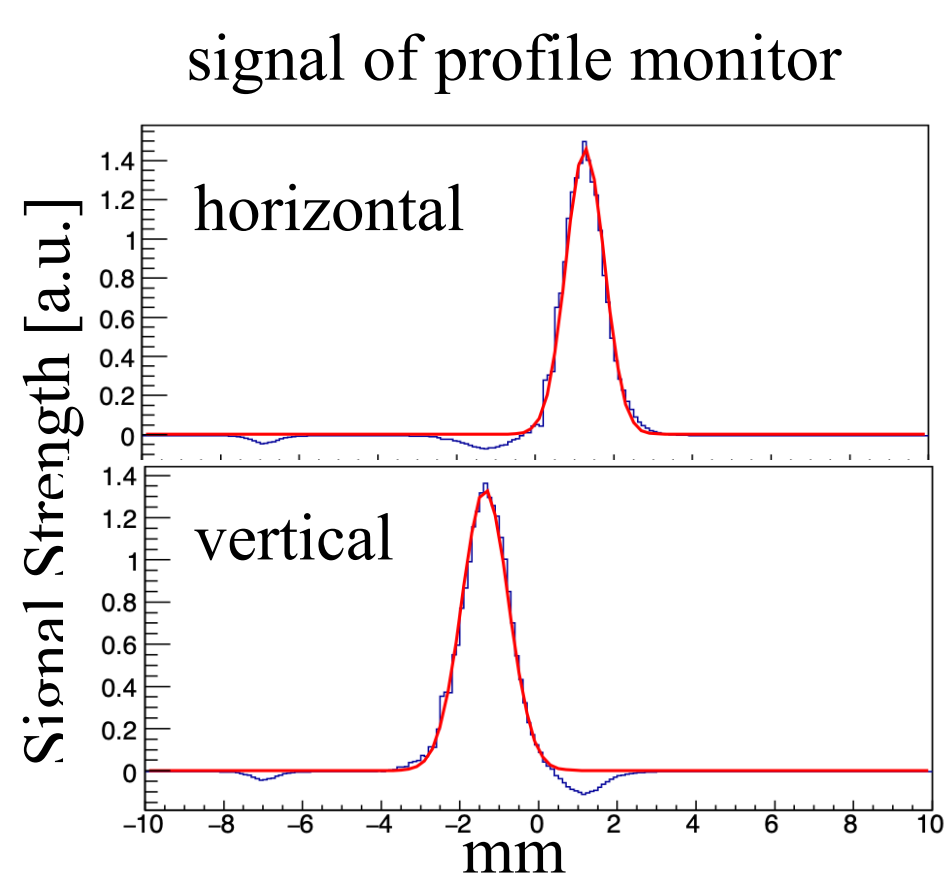


# Beam control after SRILAC: Q-scan method



Schematic view of Superconducting RIKEN LINAC (SRILAC)

Spot image @ GARISIII target (Viewer)



Beam is narrowed at differential pumping system

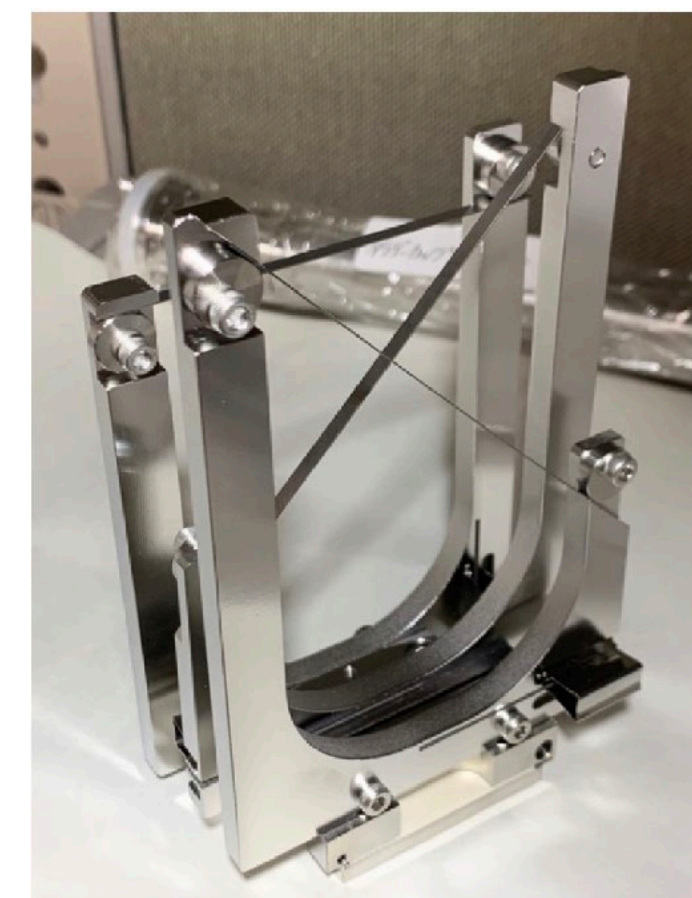
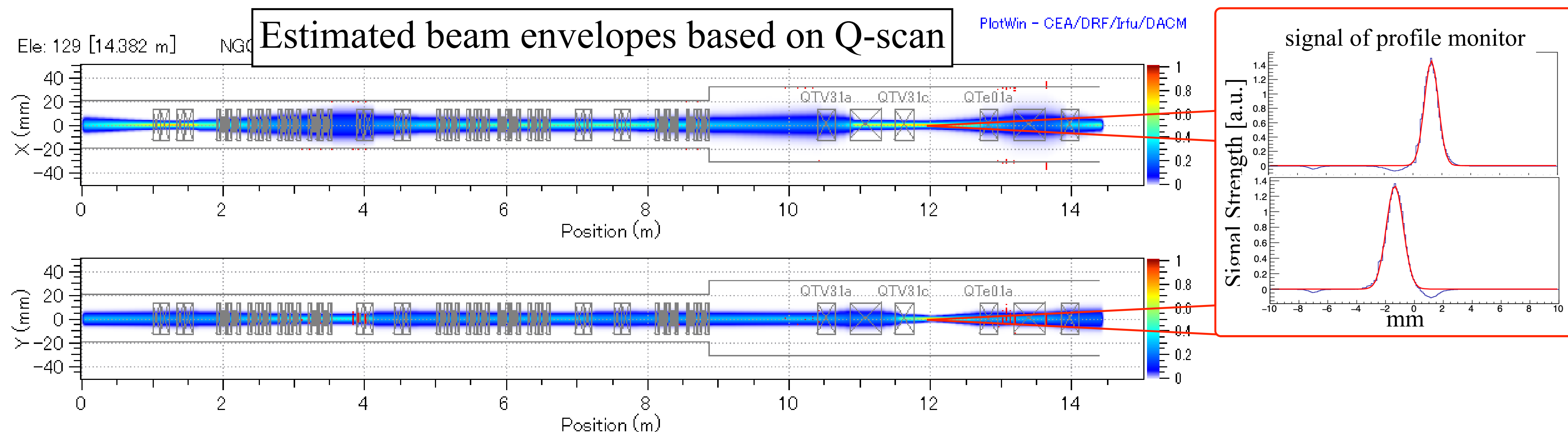
Beam loss < a few % (measured by FC)





# Motivation: Beam envelope / loss control

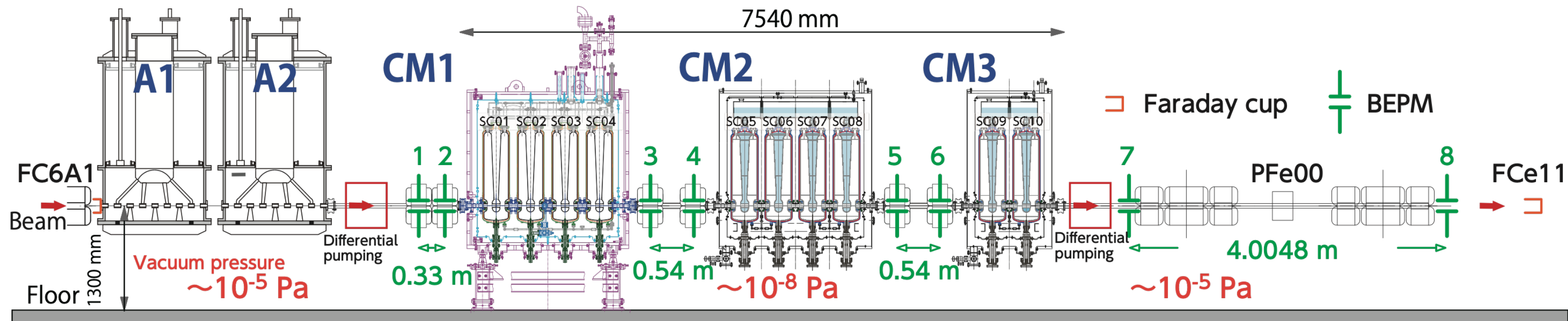
- Control beam envelope / loss is essential especially for SRF cavities....
- Destructive monitors (wire scanner called profile monitors etc...)
  - not installed between cavities to avoid dust creation
- Conventional Q-scan and simulation based on transfer matrix
  - **works well** / needs to **reduce beam intensity** ( $\sim 100$  enA) and to **change optics to several modes**
- For continuous monitor during beam supply, we need **non-destructive method**



profile monitor @ e00



# Candidate: Beam Energy Position Monitor (BEPM)

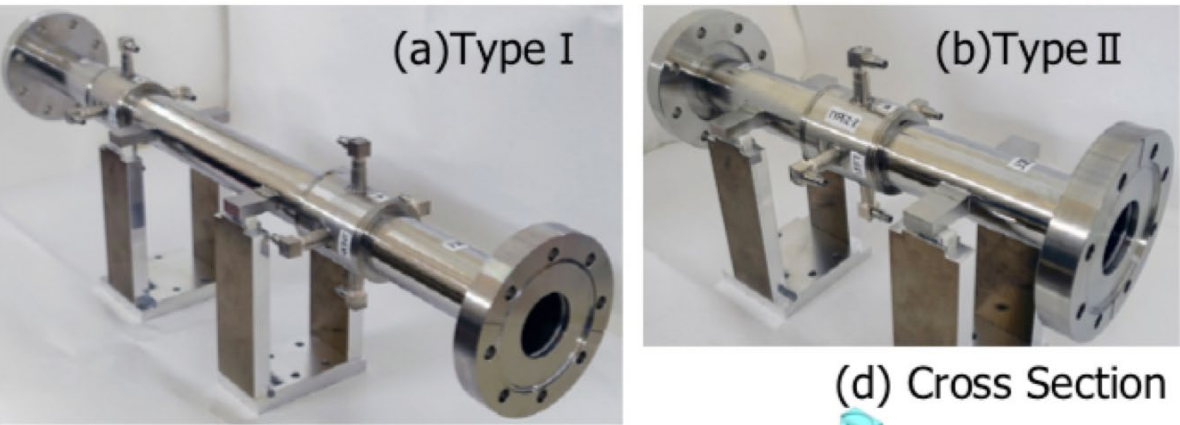


Schematic view of Superconducting RIKEN LINAC (SRILAC)

8 B(E)PMs are installed in beam line

- Position at each BEPMs
- Energy at each sections (2 BEPMs) are continuously monitored.

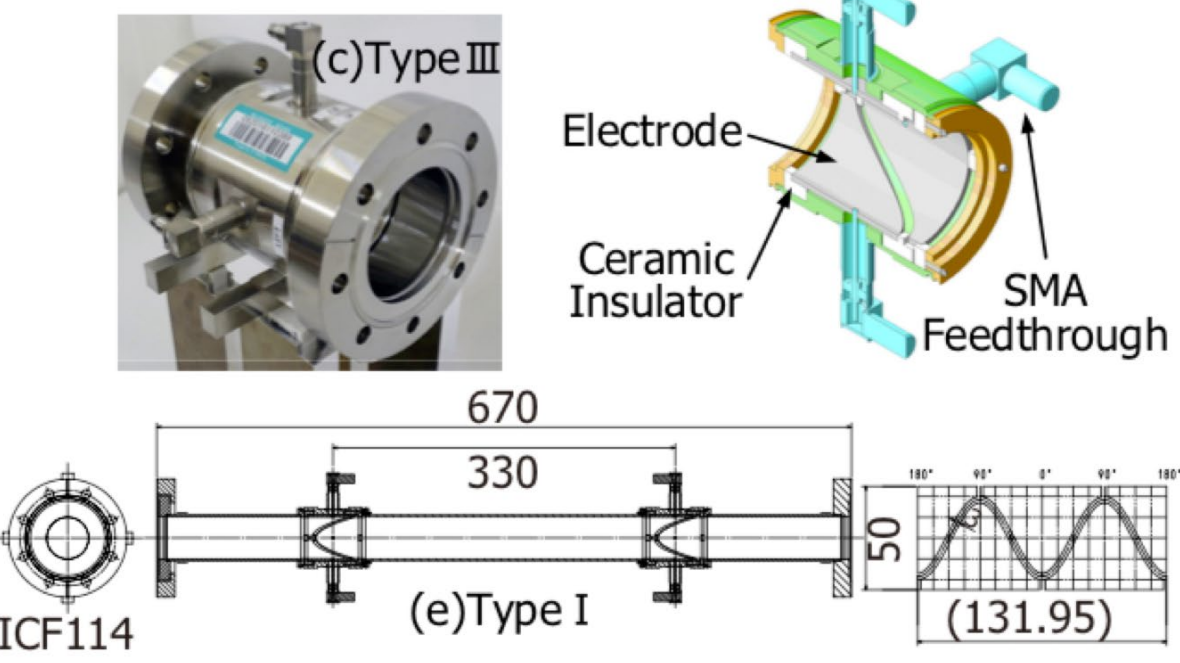
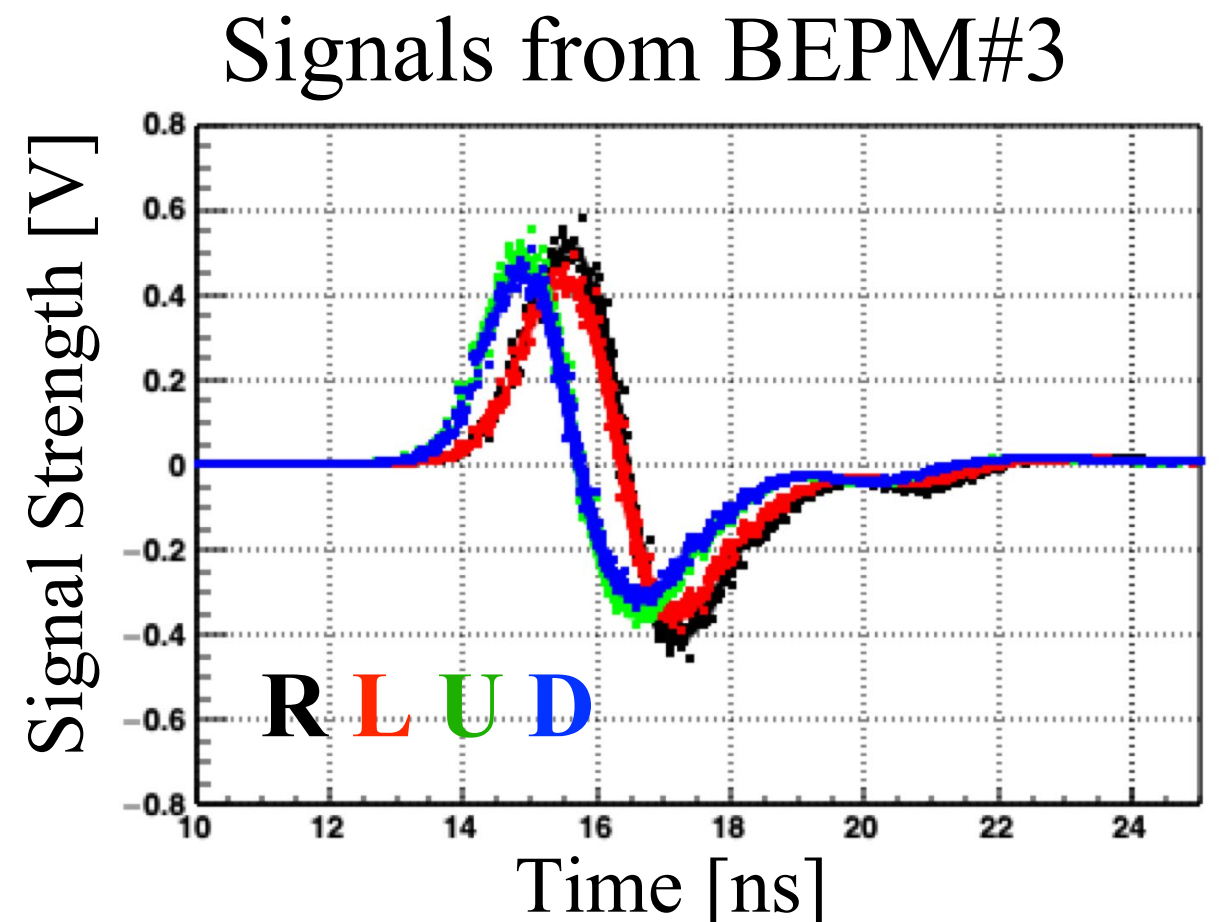
→ utilize these BEPMs for beam envelope measurement



## List of BEPMs in SRILAC beam line

Name in this talk	BEPM#	Length of electrode	Inner radius	Shape
Type A	1 ~ 6	50 mm	20 mm	cos2θ
Type B	7, 8	60 mm	30 mm	

※ TypeI, II: A TypeIII: B



higher sensitivity for position, timing and quadrupole moments

T. Watanabe *et al.*,  
 Proc. of IBIC2020, pp. 718–723, (2020)

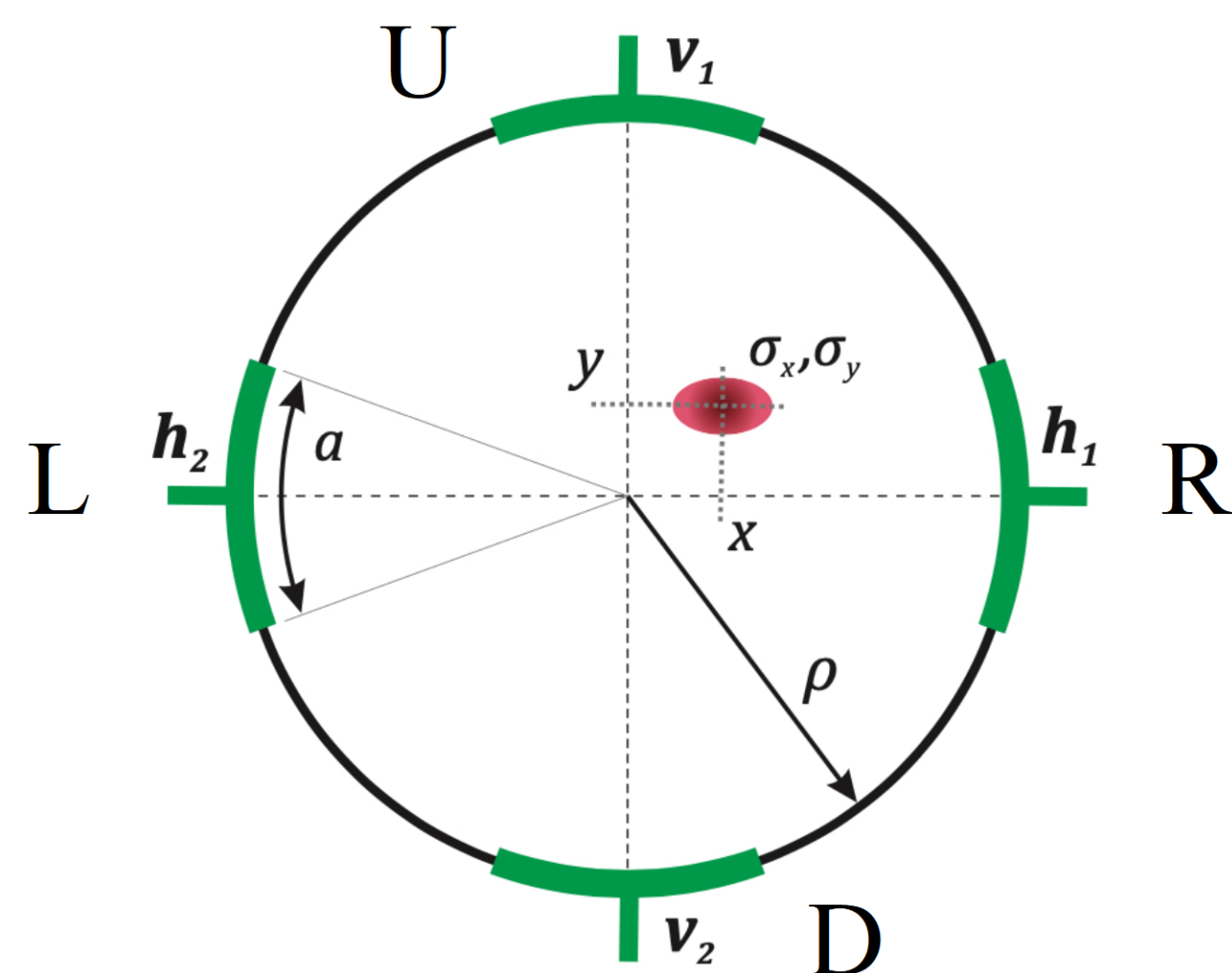


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# Quadrupole measurements by BPMs



Emittance measurements by BPMs are studied in decades...

- R. H. Miller *et al.*, Proc. HEACC'83, pp. 603-605 (1983)
- **A. Sounas *et al.*, Proc. HB2018, pp. 399–403 (2018)**

$$Q \equiv \sigma_x^2 - \sigma_y^2 = \langle x^2 \rangle - \langle y^2 \rangle - \langle x \rangle^2 + \langle y \rangle^2$$

second-order quadrupolar term

schematic view of BPMs

$$V_R = I_{beam}(c_0 + c_1 D_x + c_2 M_2 + c_3 M_{3,x} + \dots)$$

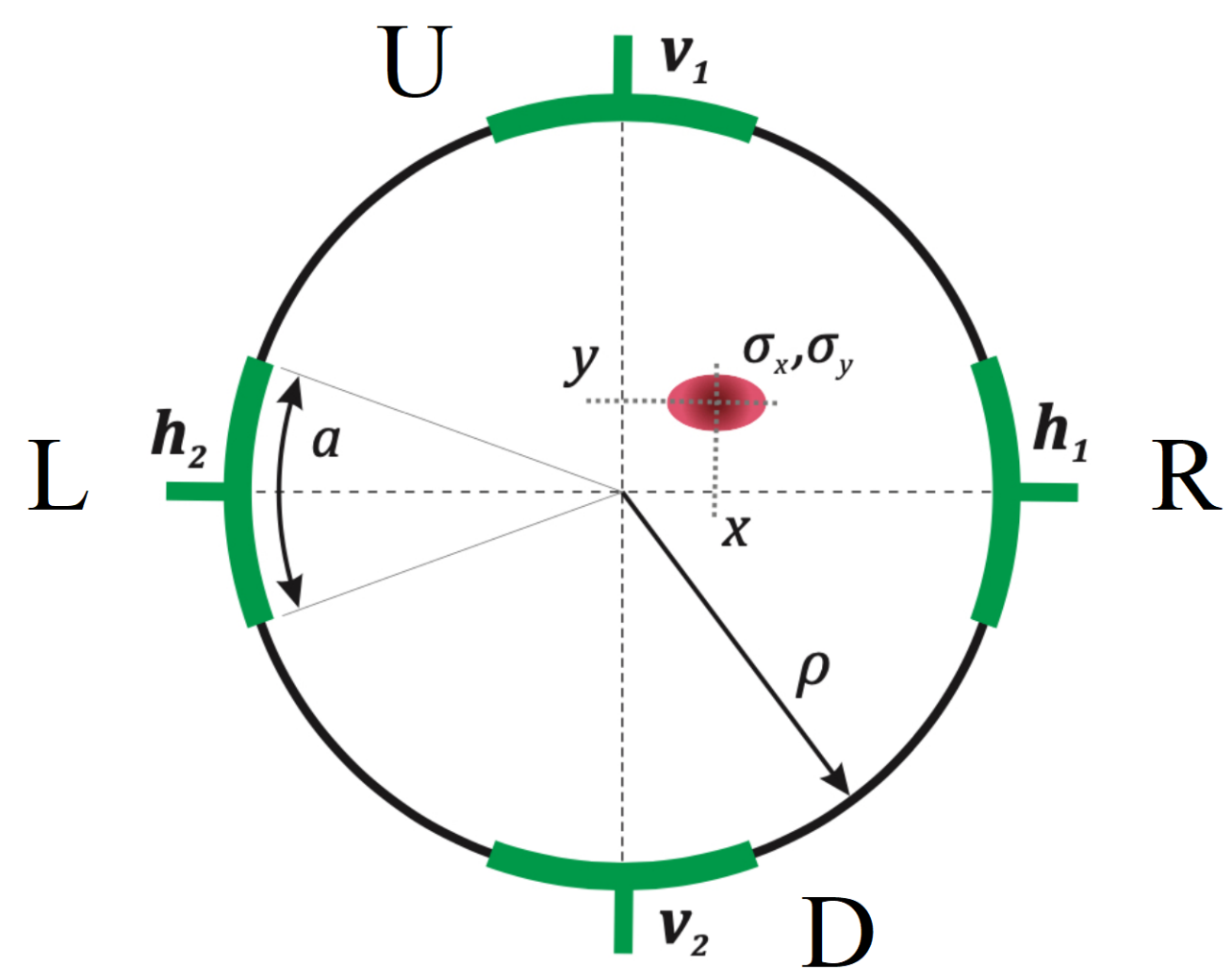
$$V_L = I_{beam}(c_0 - c_1 D_x + c_2 M_2 - c_3 M_{3,x} + \dots)$$

$$V_U = I_{beam}(c_0 + c_1 D_y - c_2 M_2 + c_3 M_{3,y} + \dots)$$

$$V_D = I_{beam}(c_0 - c_1 D_y - c_2 M_2 - c_3 M_{3,y} + \dots)$$

A. Sounas, M. Gasior, and T. Lefevre,  
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 \end{aligned}$$

higher order term

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 Q &\equiv \sigma_x^2 - \sigma_y^2 = \overbrace{\langle x^2 \rangle - \langle y^2 \rangle} - \overbrace{\langle x \rangle^2 + \langle y \rangle^2} \\
 &= \underline{M_2} - D_x^2 + D_y^2 \quad \text{second-order quadrupolar term} \\
 &= k_q \frac{V_R + V_L - V_U - V_D}{V_R + V_L + V_U + V_D} - D_x^2 + D_y^2
 \end{aligned}$$

$$D_x = k_x \frac{V_R - V_L}{V_R + V_L + V_U + V_D}, \quad D_y = k_y \frac{V_U - V_D}{V_L + V_R + V_U + V_D}$$

(neglect higher order term /  $k_q \equiv c_2/c_0$  /  $k_{x,y} \equiv c_1/2c_0$ )

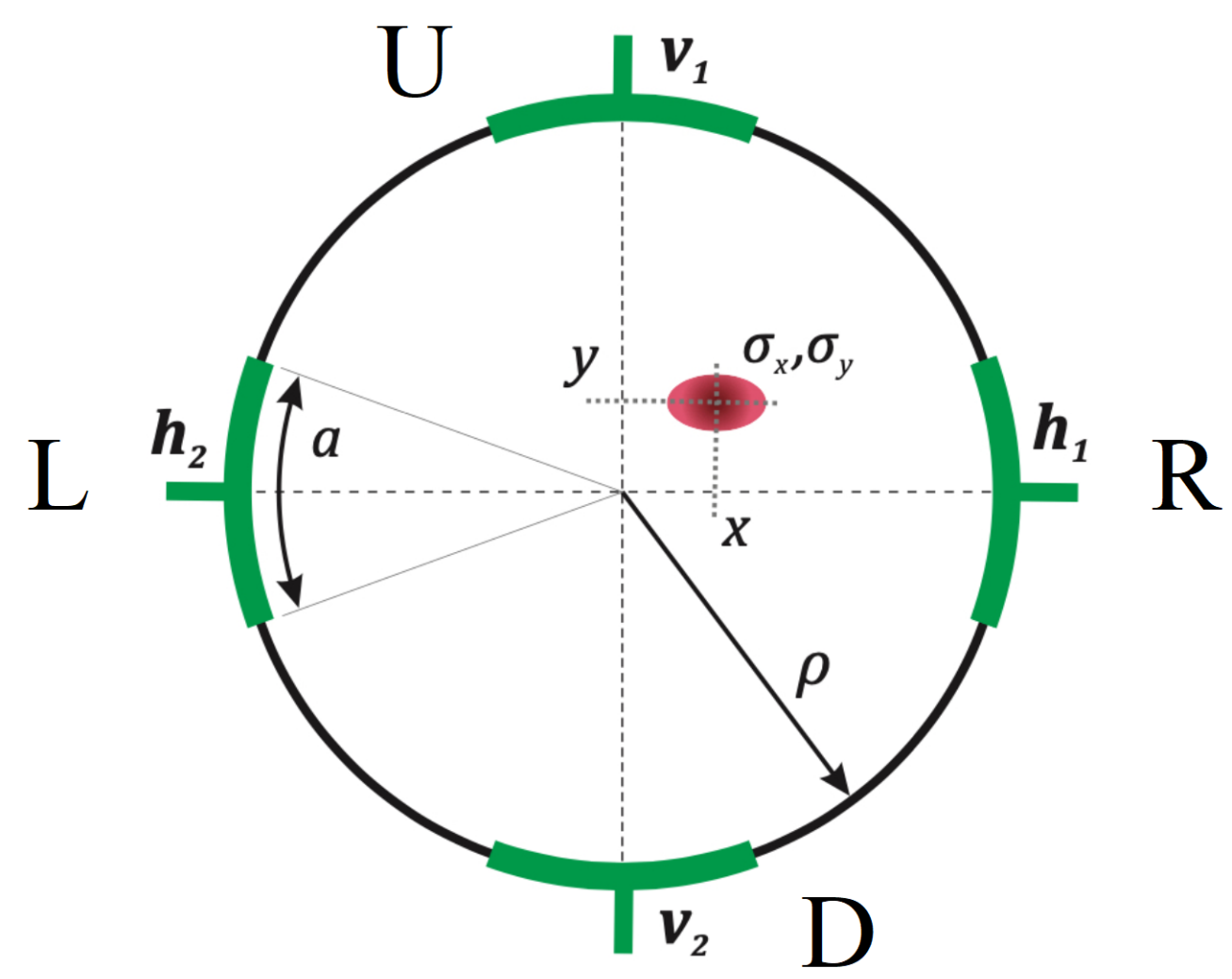
“Their application has been proven to be limited ....”

- low sensitivity for quadrupole momentum Q  
→
- parasitic position signal incorporated into the measured Q  
→





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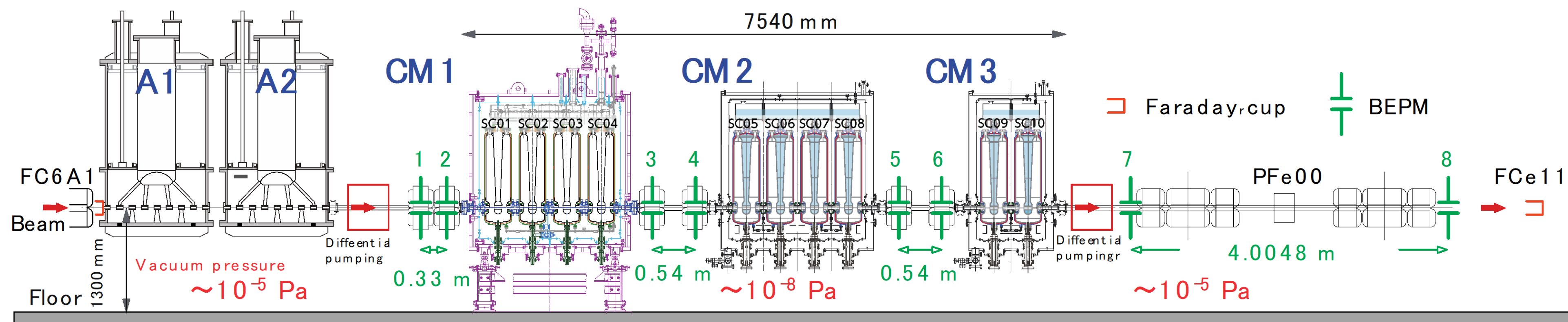
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“Their application has been proven to be limited ....”

- low sensitivity for quadrupole momentum Q  
→ Relatively large beam size (~ a few  $\pi$ mm mrad)
- parasitic position signal incorporated into the measured Q  
→ Small contribution from higher order term (by  $\cos 2\theta$  shape)

# Quadrupole moments and beam envelope

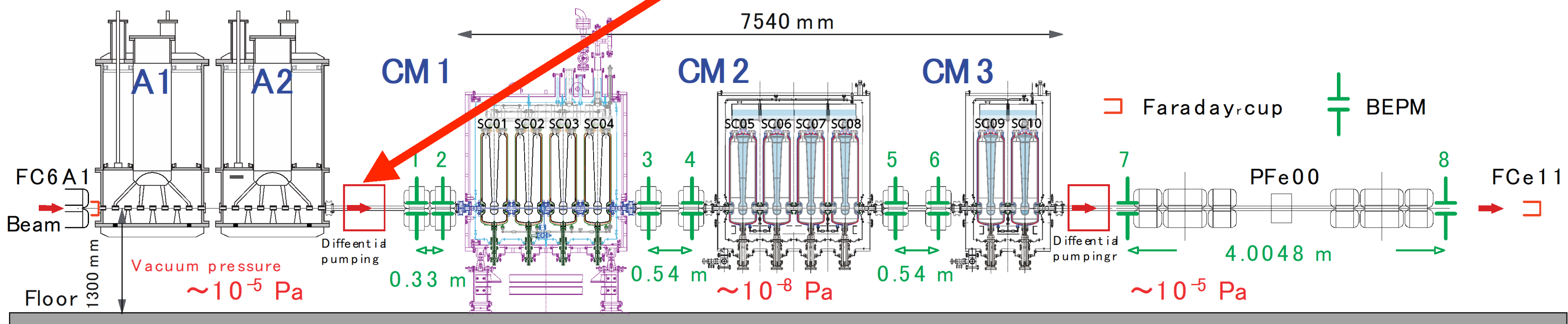
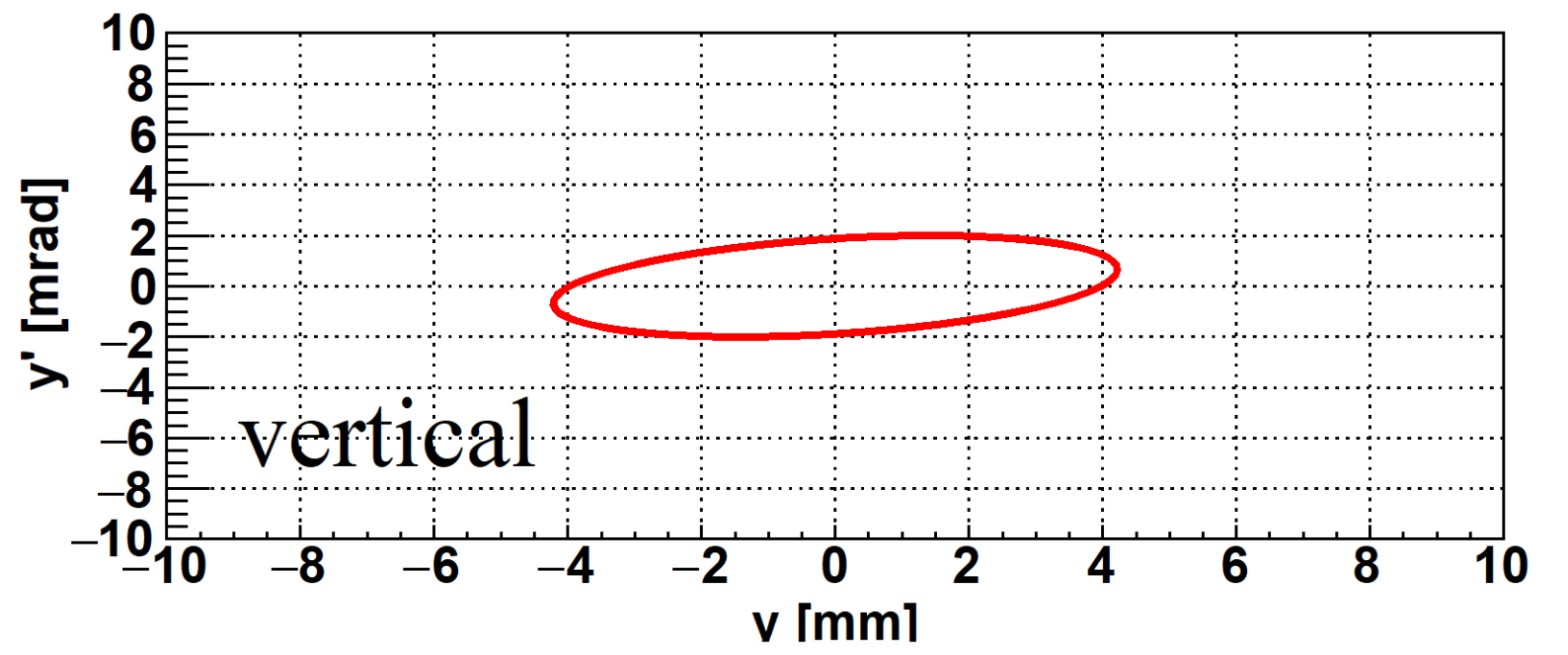
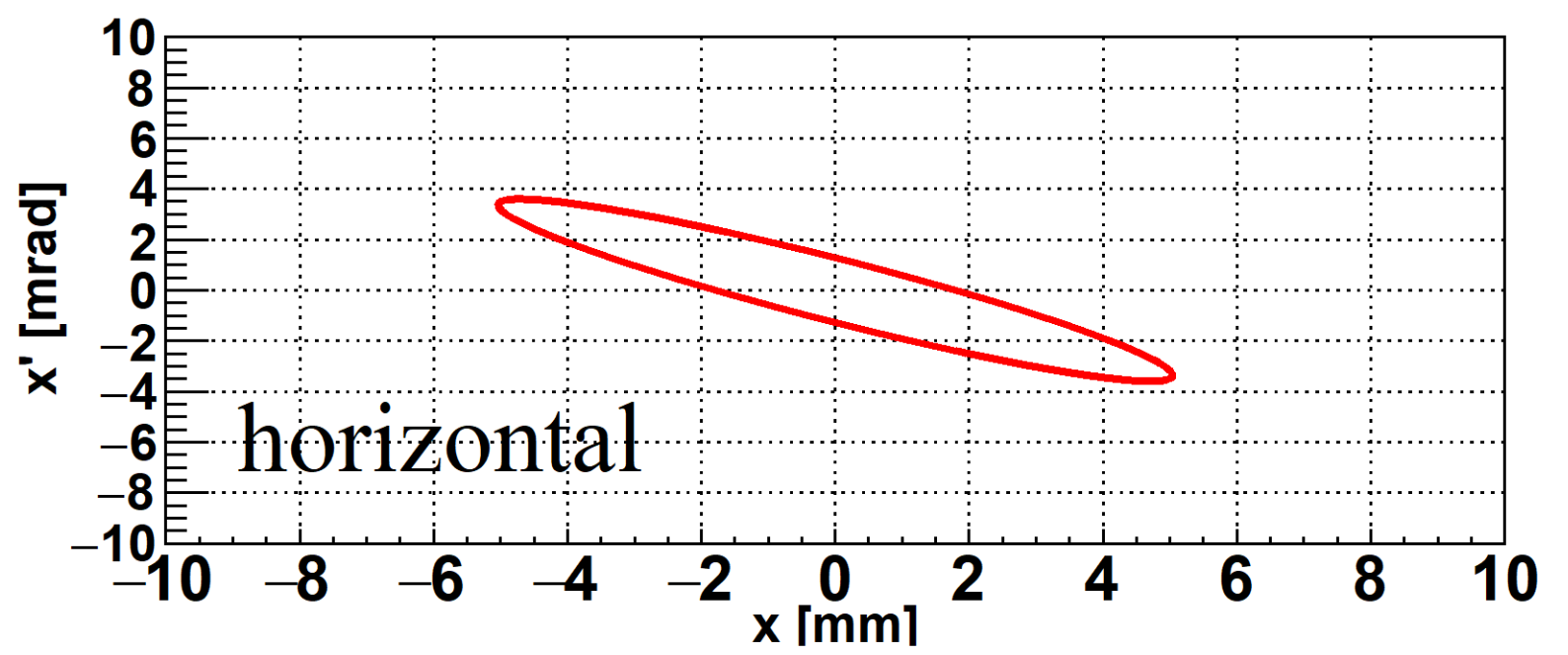
$$\begin{pmatrix} Q_1 \\ Q_2 \\ \square \\ Q_8 \end{pmatrix} = \begin{pmatrix} M_x(1\ 0)_{11}^2, -2M_x(1\ 0)_{11}M_x(1\ 0)_{12}, M_x(1\ 0)_{12}^2, -M_y(1\ 0)_{11}^2, \square \\ M_x(2\ 0)_{11}^2, -2M_x(2\ 0)_{11}M_x(2\ 0)_{12}, M_x(2\ 0)_{12}^2, -M_y(2\ 0)_{11}^2, \square \\ \square \\ M_x(8\ 0)_{11}^2, -2M_x(8\ 0)_{11}M_x(8\ 0)_{12}, M_x(8\ 0)_{12}^2, -M_y(8\ 0)_{11}^2, \square \end{pmatrix} \begin{pmatrix} \sigma_{xx}(0) \\ \sigma_{xx'}(0) \\ \sigma_{yy}(0) \\ \sigma_{yy'}(0) \end{pmatrix}$$



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Phase Ellipse at input point

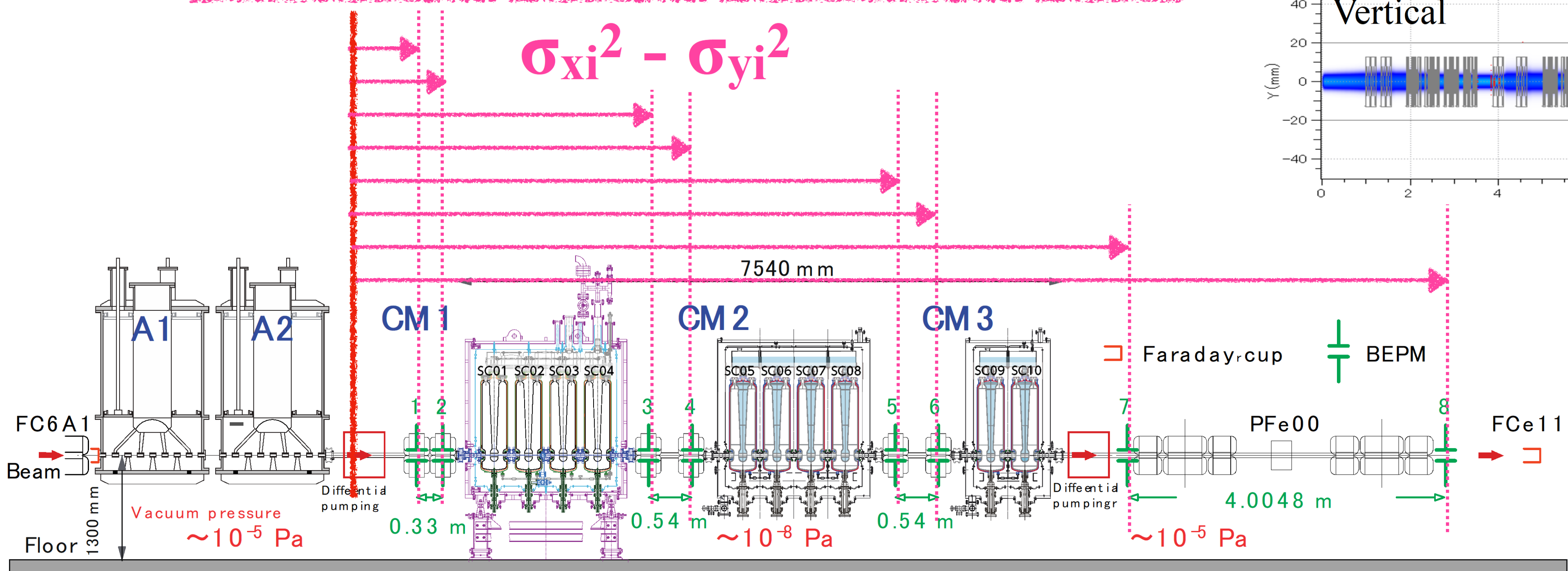
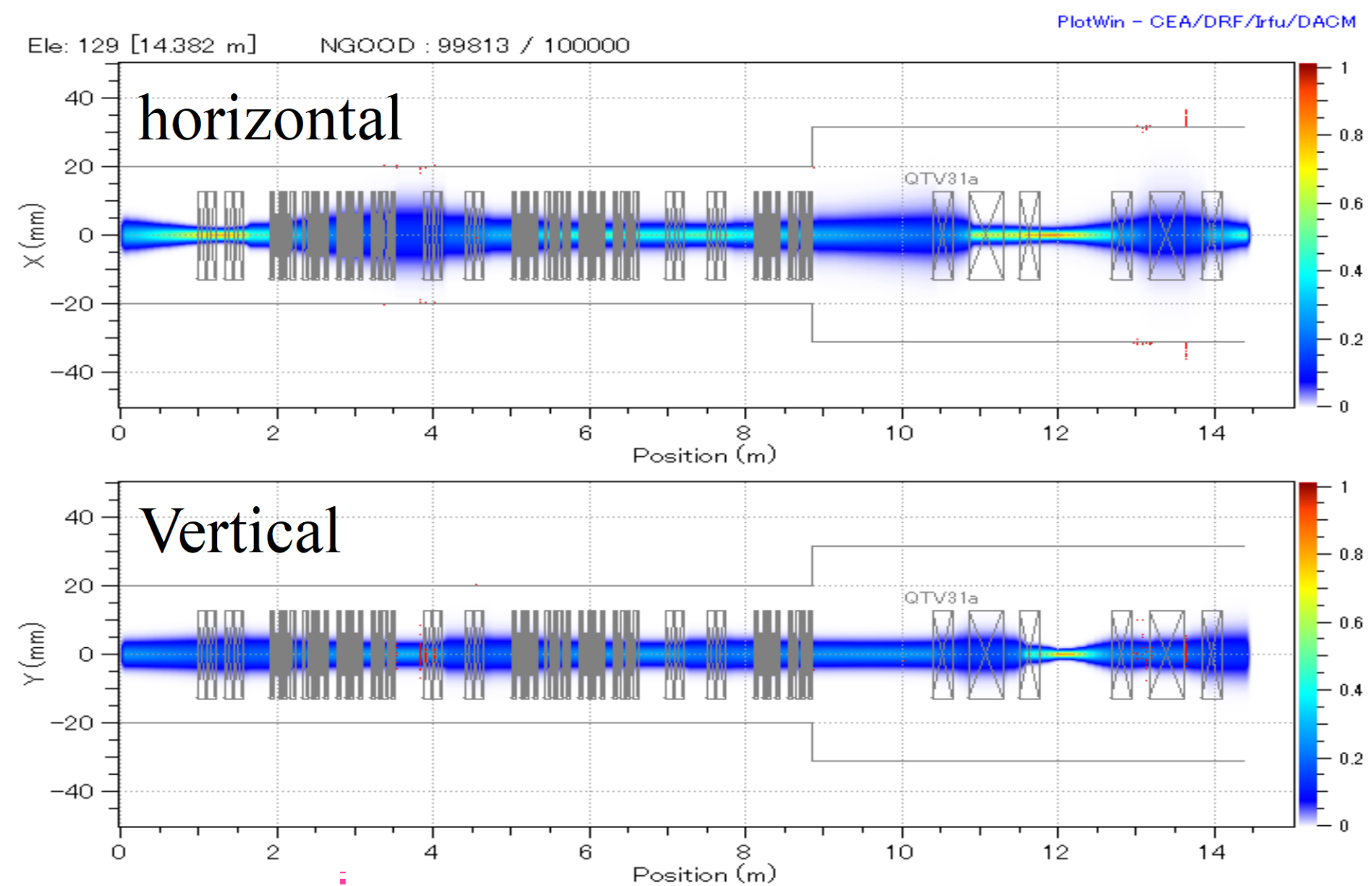




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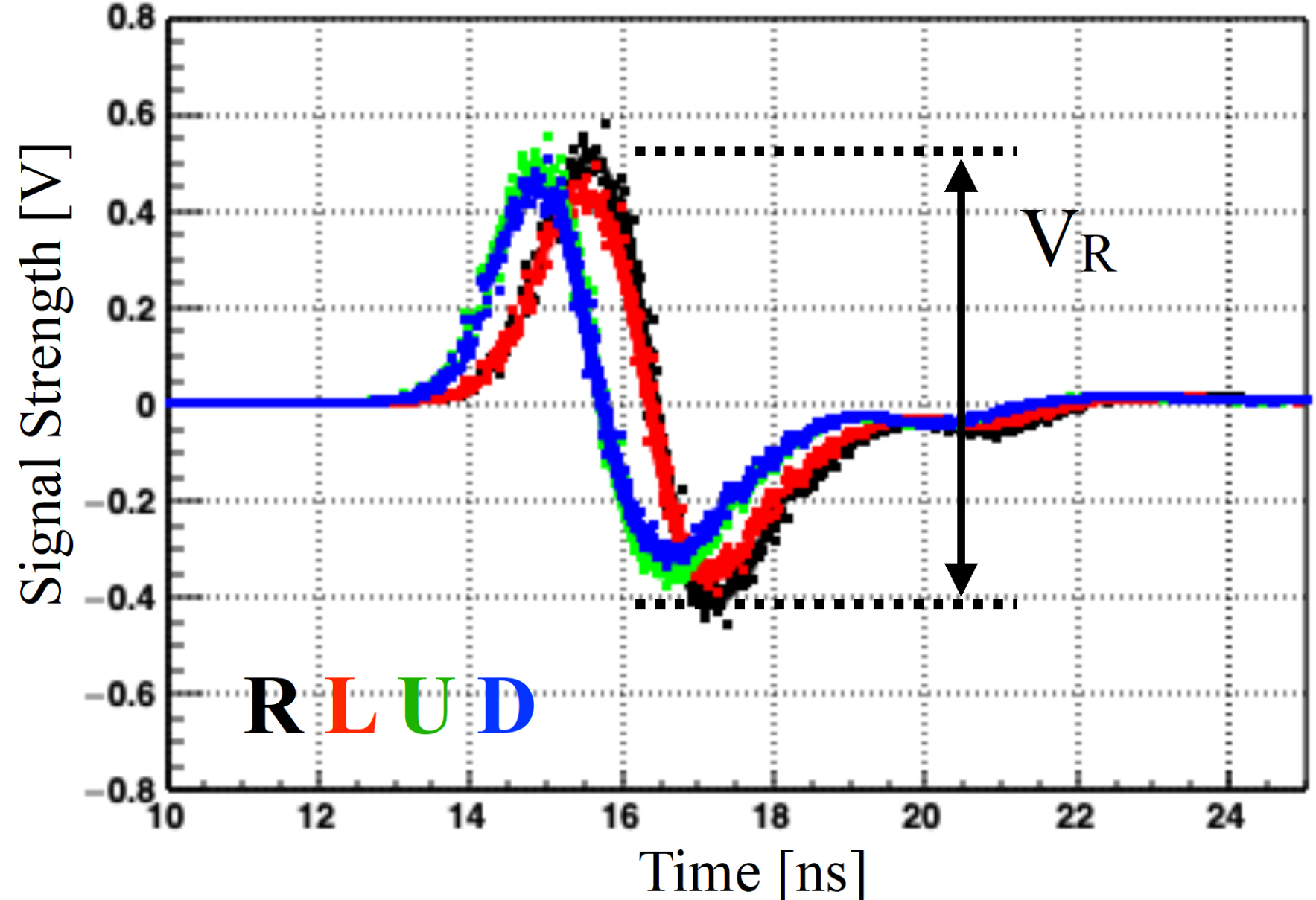
Beam Envelope (calc. by TraceWin)



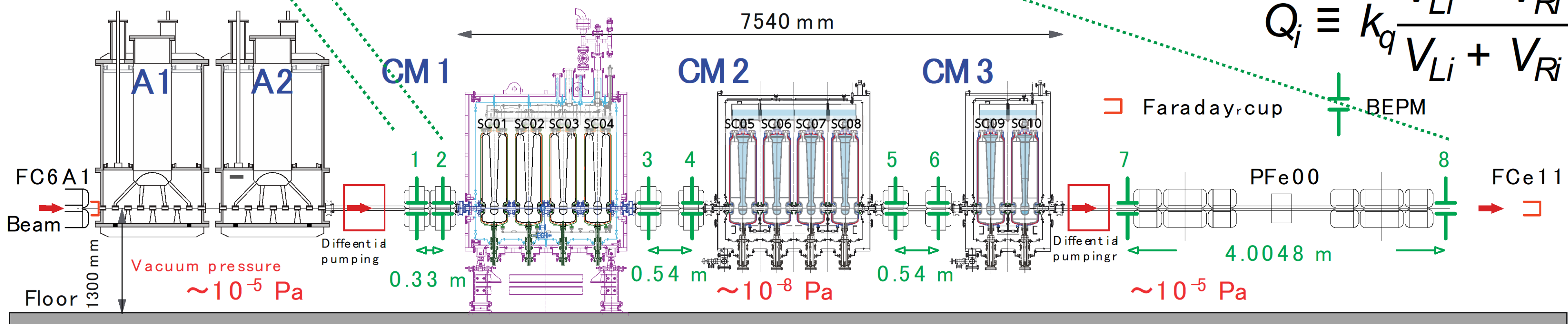
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Signals from BEPM#3



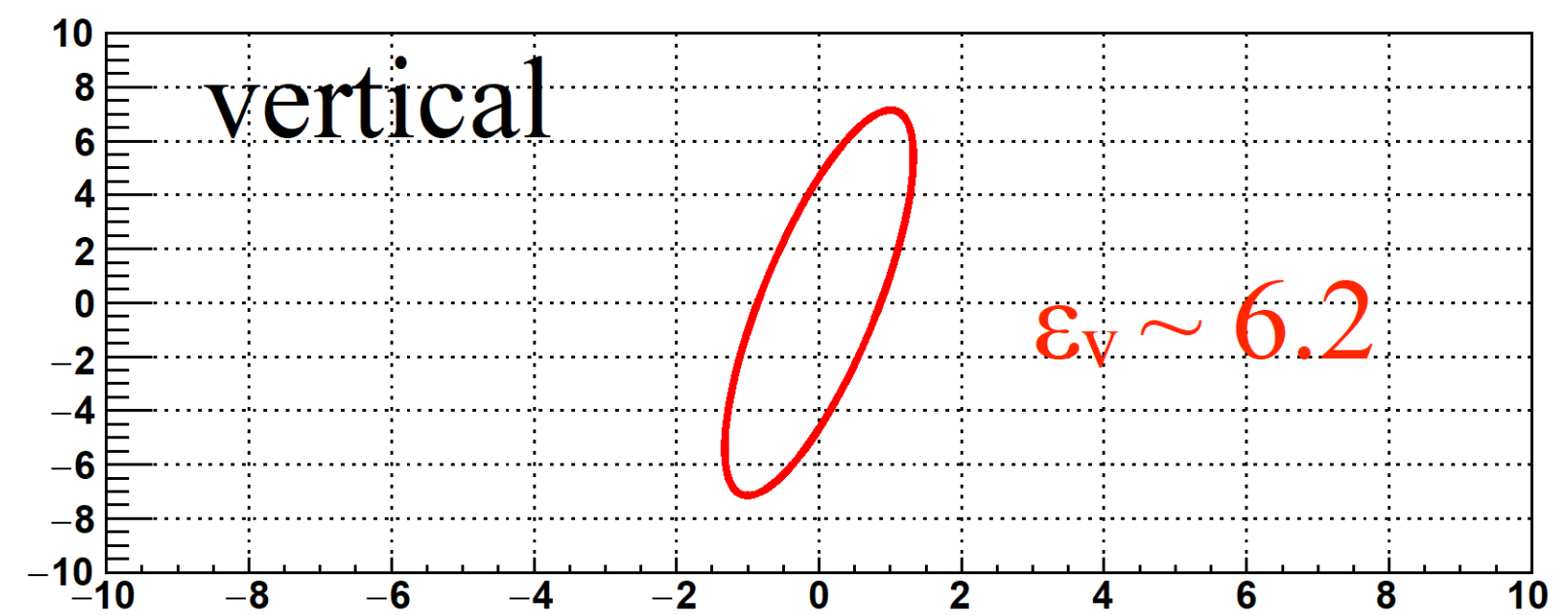
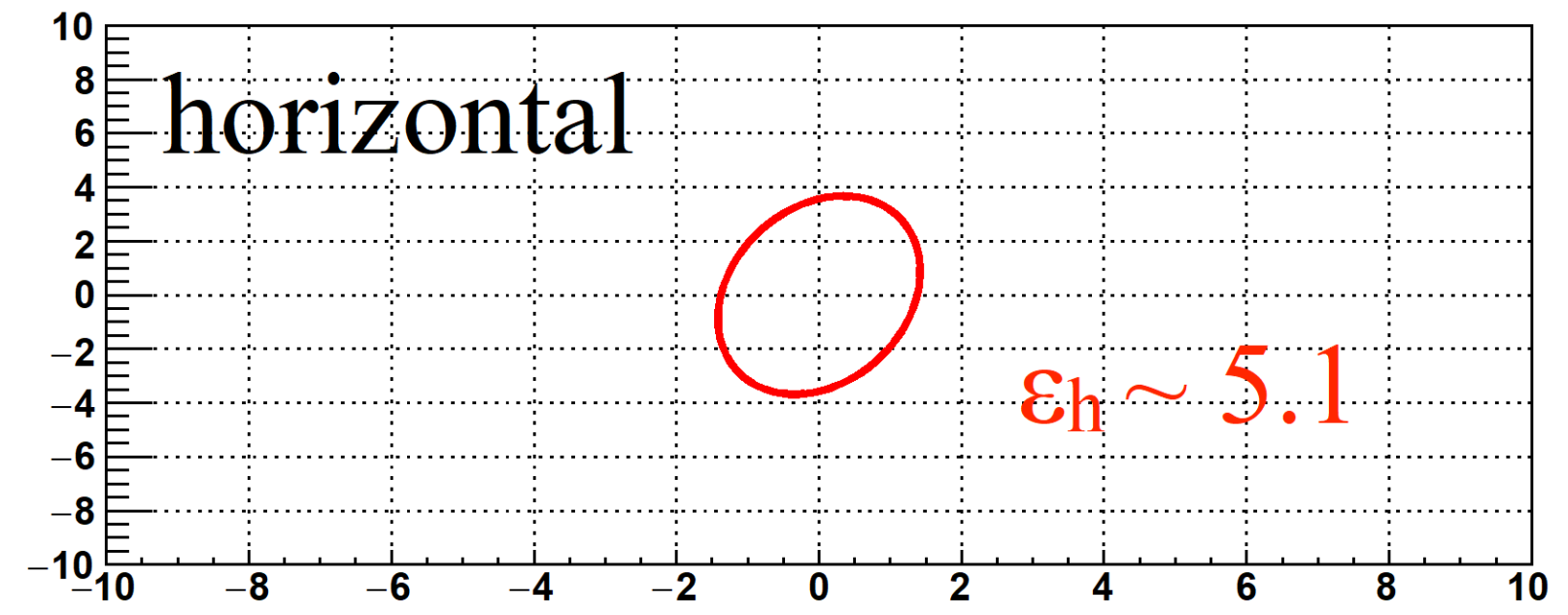
$$Q_i \equiv k_q \frac{V_{Li} + V_{Ri} - V_{Ui} - V_{Di}}{V_{Li} + V_{Ri} + V_{Ui} + V_{Di}} - \square x^2 + \square y^2$$



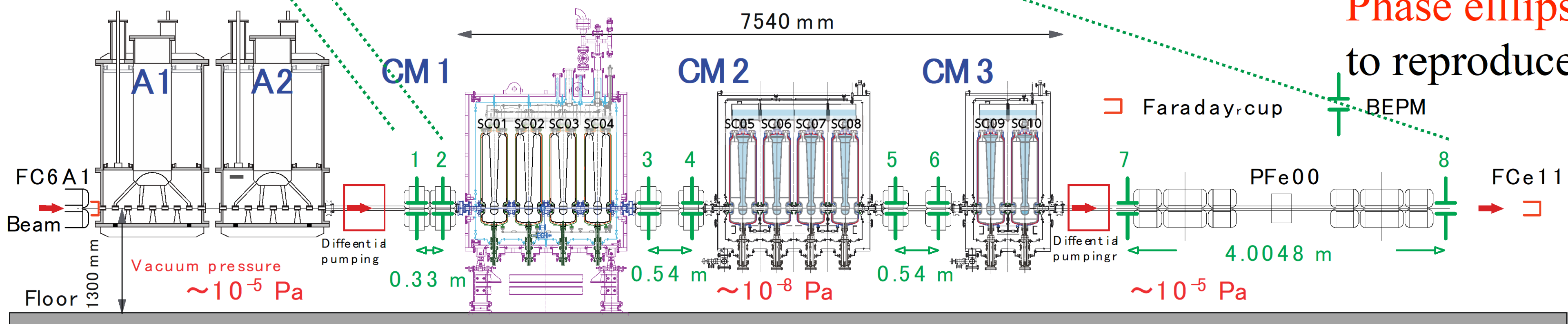


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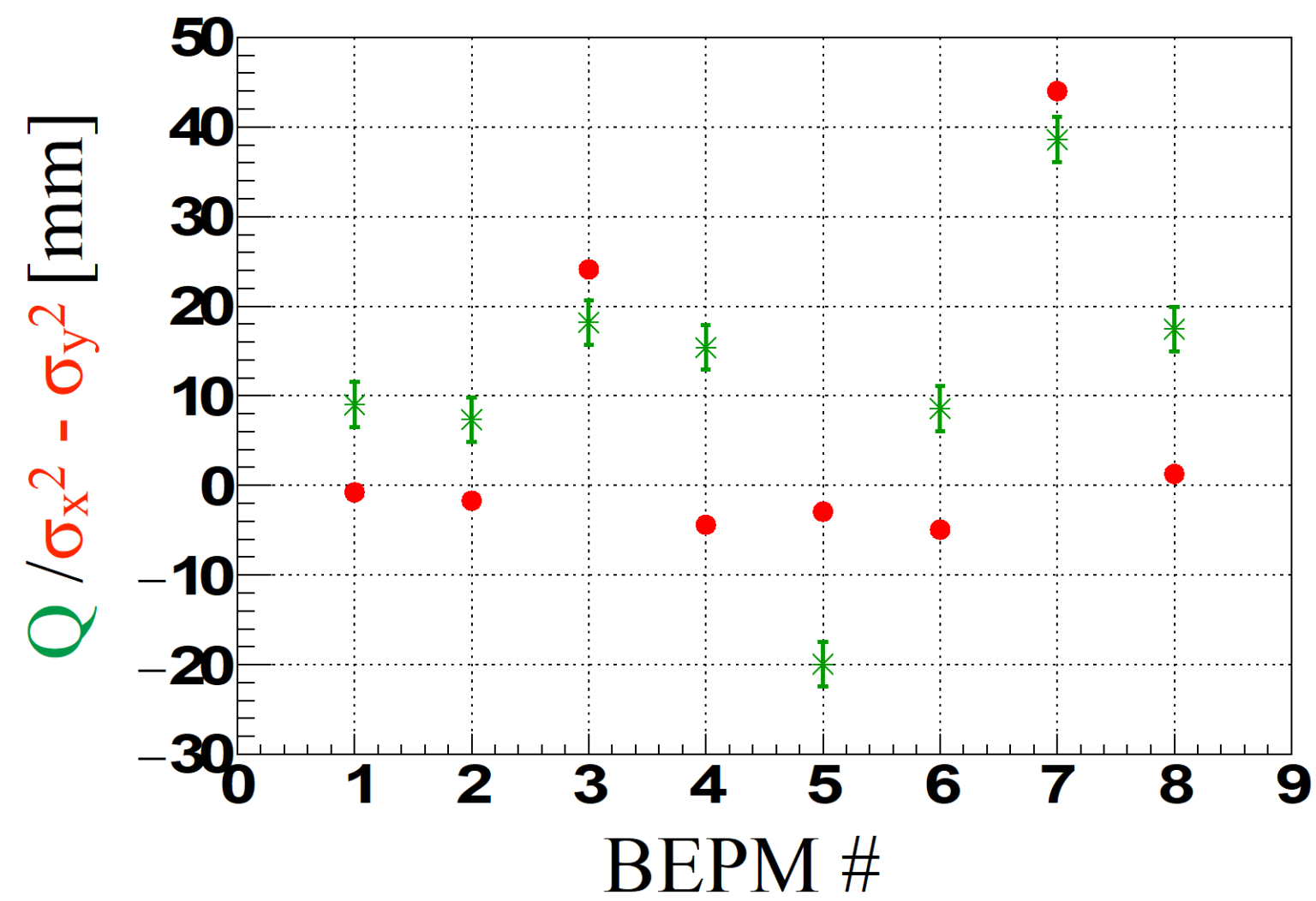
Phase ellipses are estimated to reproduce measured  $Q_s$ .



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# First trial to reproduce experimental data



Measured

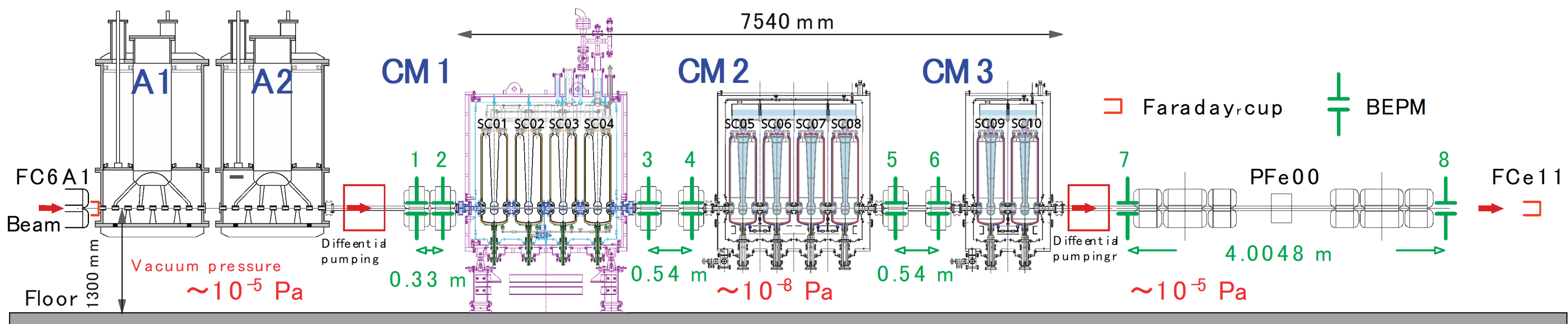
Fit

$$\begin{pmatrix} Q_1 \\ Q_2 \\ \square \\ Q_8 \end{pmatrix}$$

$$= \begin{pmatrix} M_x(1\ 0)_{11}^2, -2M_x(1\ 0)_{11}M_x(1\ 0)_{12}, M_x(1\ 0)_{12}^2, -M_y(1\ 0)_{11}^2, \square \\ M_x(2\ 0)_{11}^2, -2M_x(2\ 0)_{11}M_x(2\ 0)_{12}, M_x(2\ 0)_{12}^2, -M_y(2\ 0)_{11}^2, \square \\ \square \\ M_x(8\ 0)_{11}^2, -2M_x(8\ 0)_{11}M_x(8\ 0)_{12}, M_x(8\ 0)_{12}^2, -M_y(8\ 0)_{11}^2, \square \end{pmatrix}$$

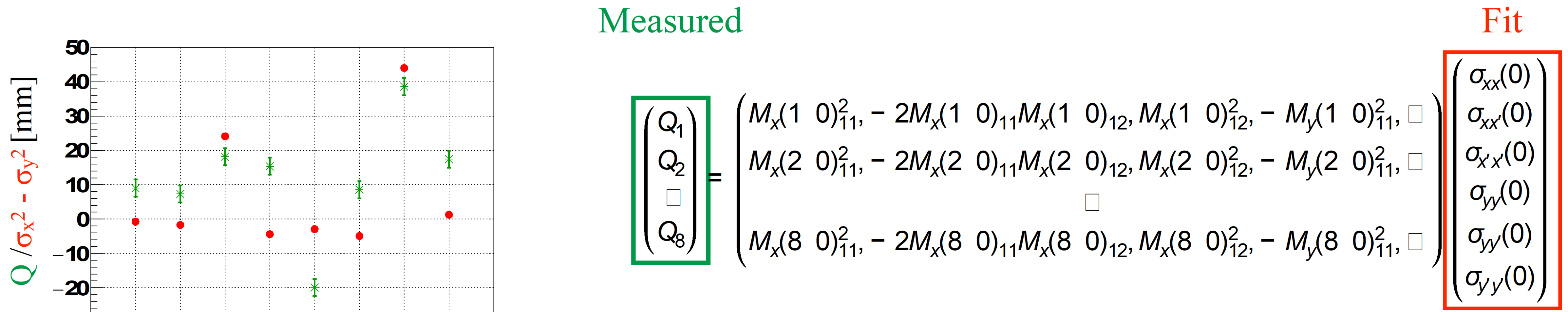
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Could **NOT** reproduce exp. data...

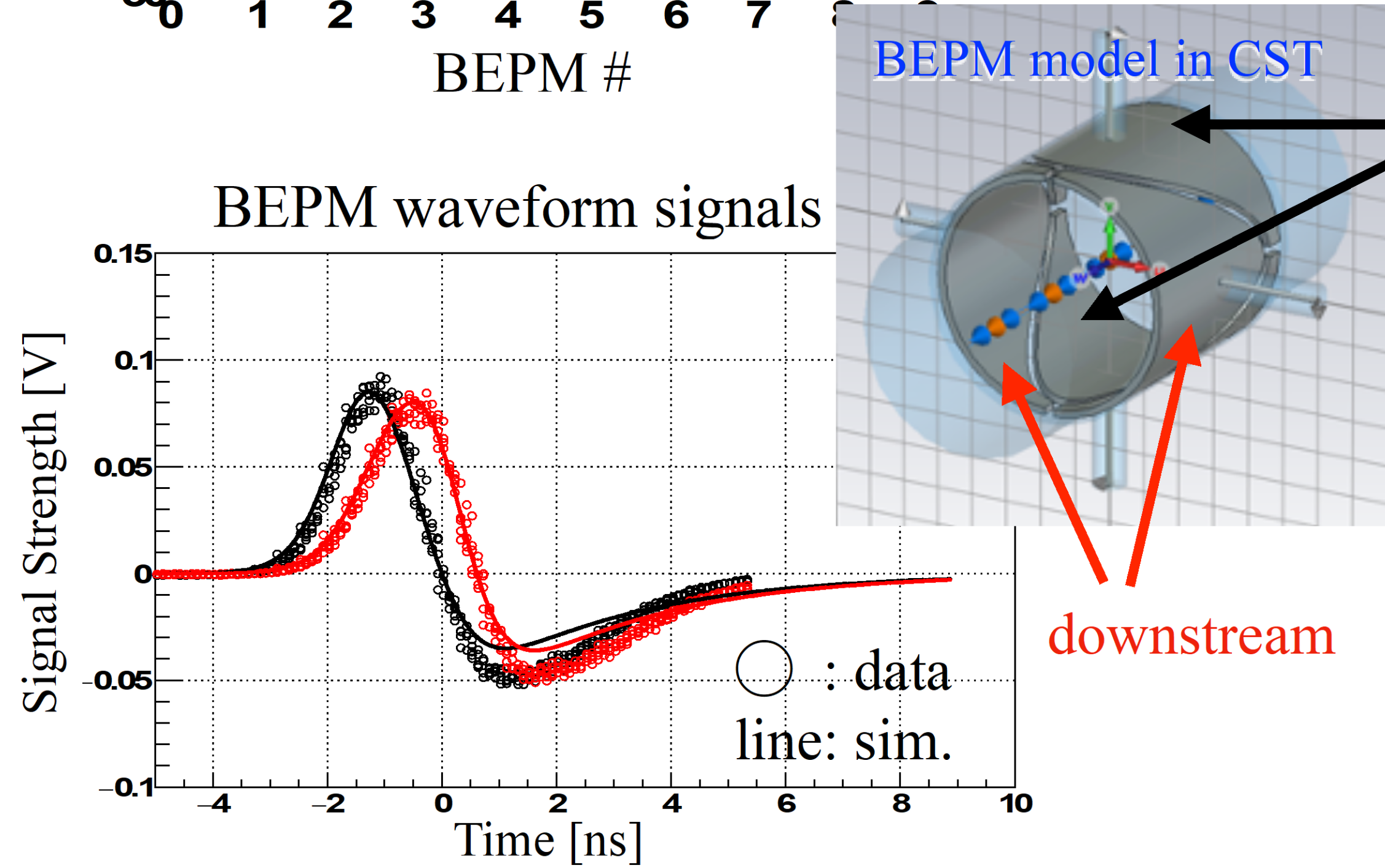




# First trial to reproduce experimental data



Could **NOT** reproduce exp. data...



$V_{\text{downstream}}$  tends to be **smaller** than  $V_{\text{upstream}}$  in both experimental and simulation data.

$$V_{\text{upstream}} = b \times V_{\text{downstream}}$$

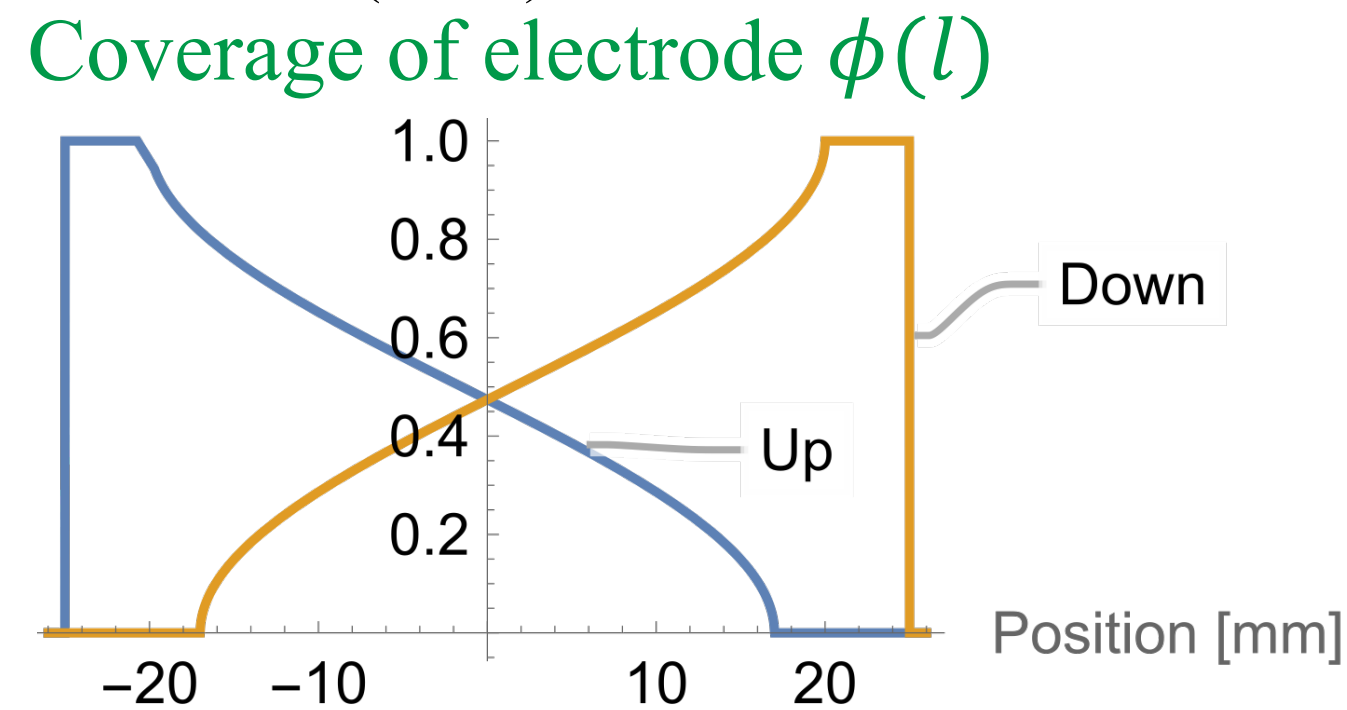
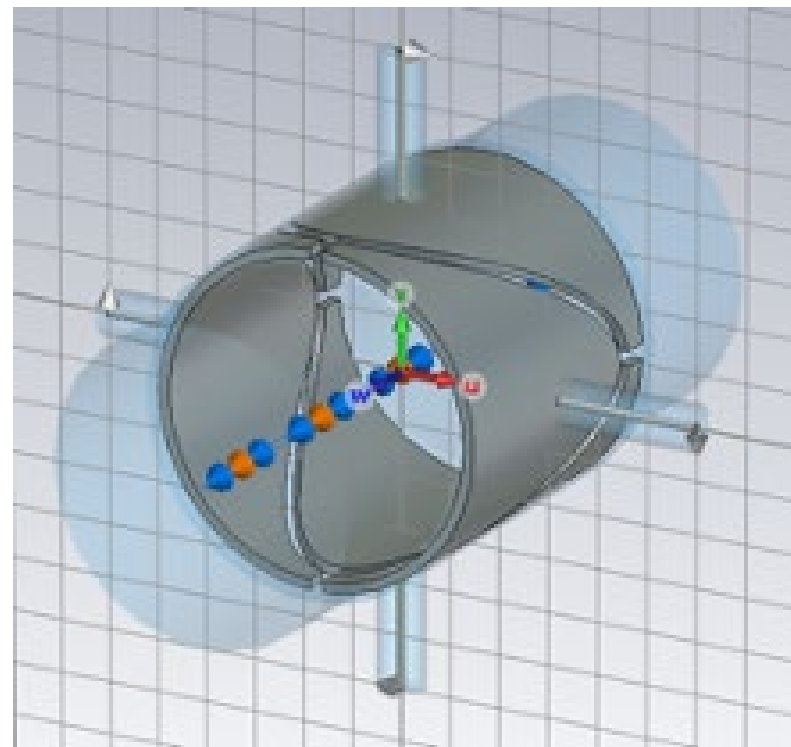
$b$  (bias factor) : 1.03  $\square$  1.06

# Origin of the bias: BEPM structure / short bunch length

Calculation of the output voltage with structure effect

CST simulation with TypeA BEPM  
( $L = 50 \text{ mm} / \sigma_t^{\text{beam}} \sim 0.5 \text{ ns} \Leftrightarrow 10^\circ$  for RF)

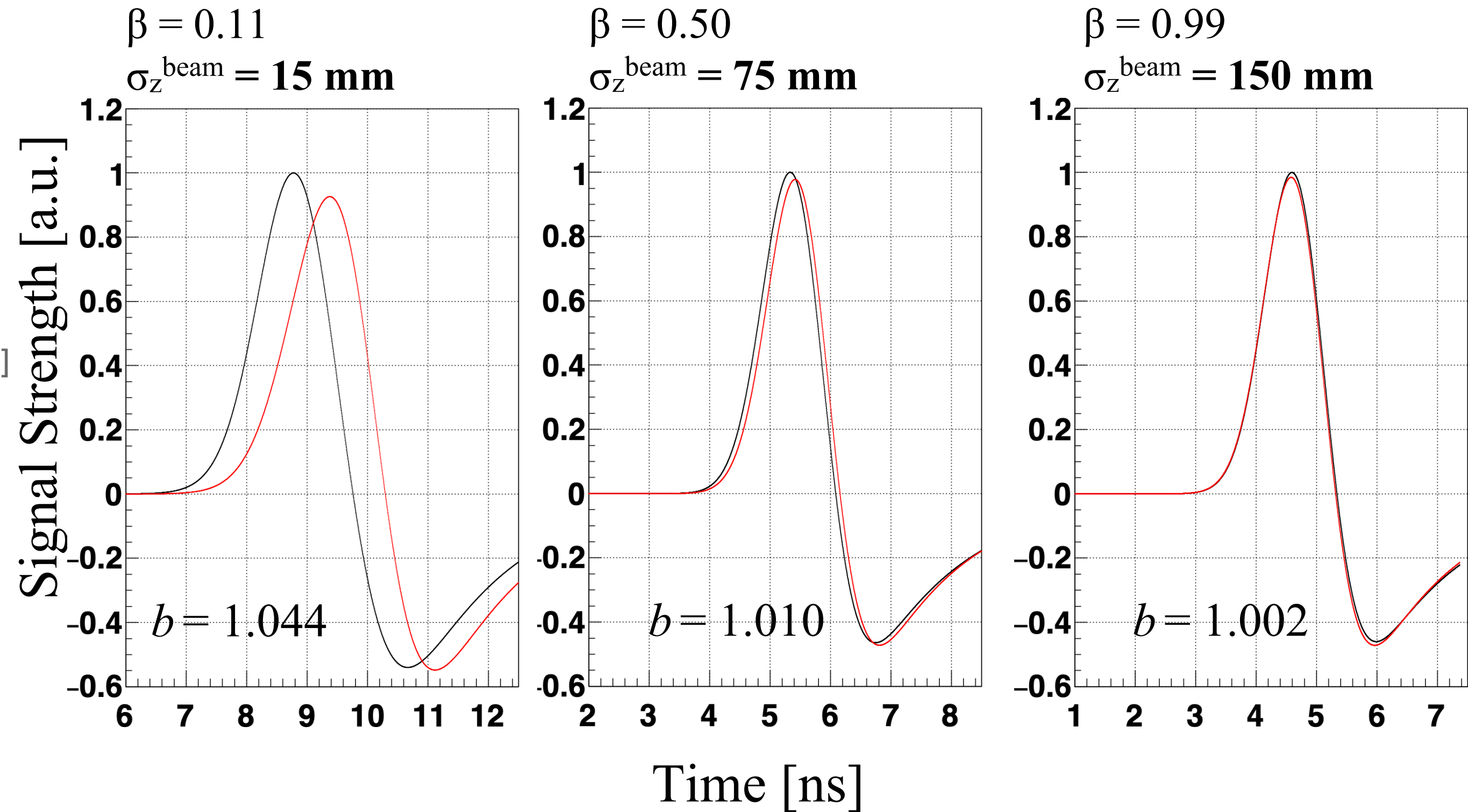
T. Adachi *et al.*, Proc. of PASJ2023, THOA4 (2023)



Shape functions of Up and Down electrode

$$V(t) = \frac{1}{L} \int_{-L/2}^{L/2} \left\{ \frac{\phi(l)}{\bar{\phi}} V(t - 1/\beta c) \right\} dl$$

parameter	explanation
t	time
V(t)	output voltage at time t w/o structure effect
L	electrode length
$\frac{1}{\bar{\phi}}$	longitudinal position of an electrode
$\phi(l)$	averaged electrode coverage angle
$\phi(l)$	electrode coverage angle at l
$\beta, c$	velocity of beam and light



This effect become significant when bunch length  $\sigma_z^{\text{beam}} \leq L$   
 c.f.  $\sigma_z^{\text{beam}}$  in SRILAC  $\sim 10 \text{ mm}$   
 $L_{\text{electrode}} = 50 \text{ mm (typeA)} / 60 \text{ mm (typeB)}$

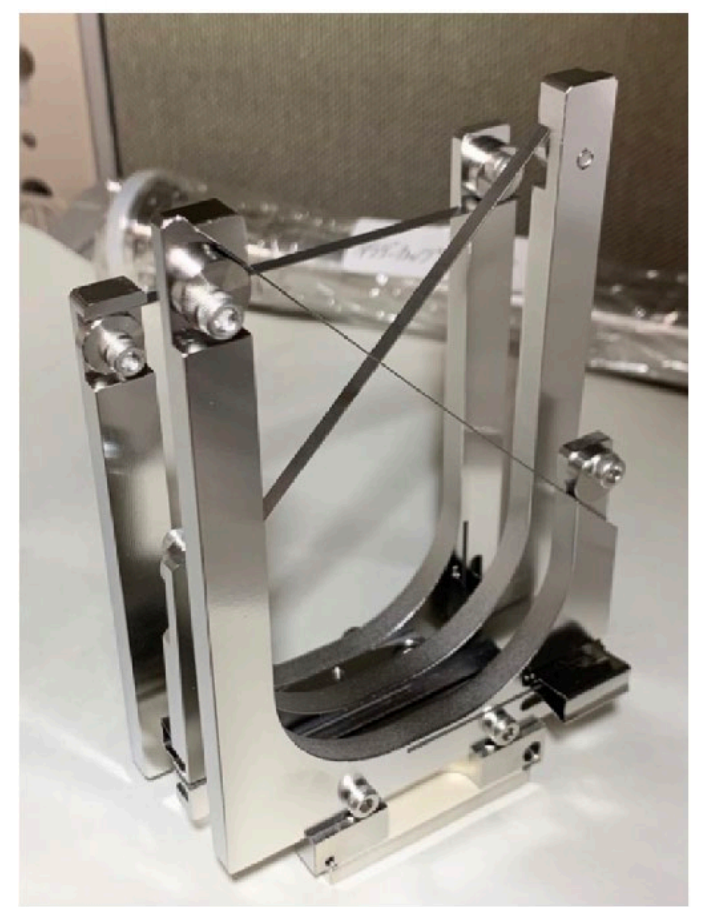
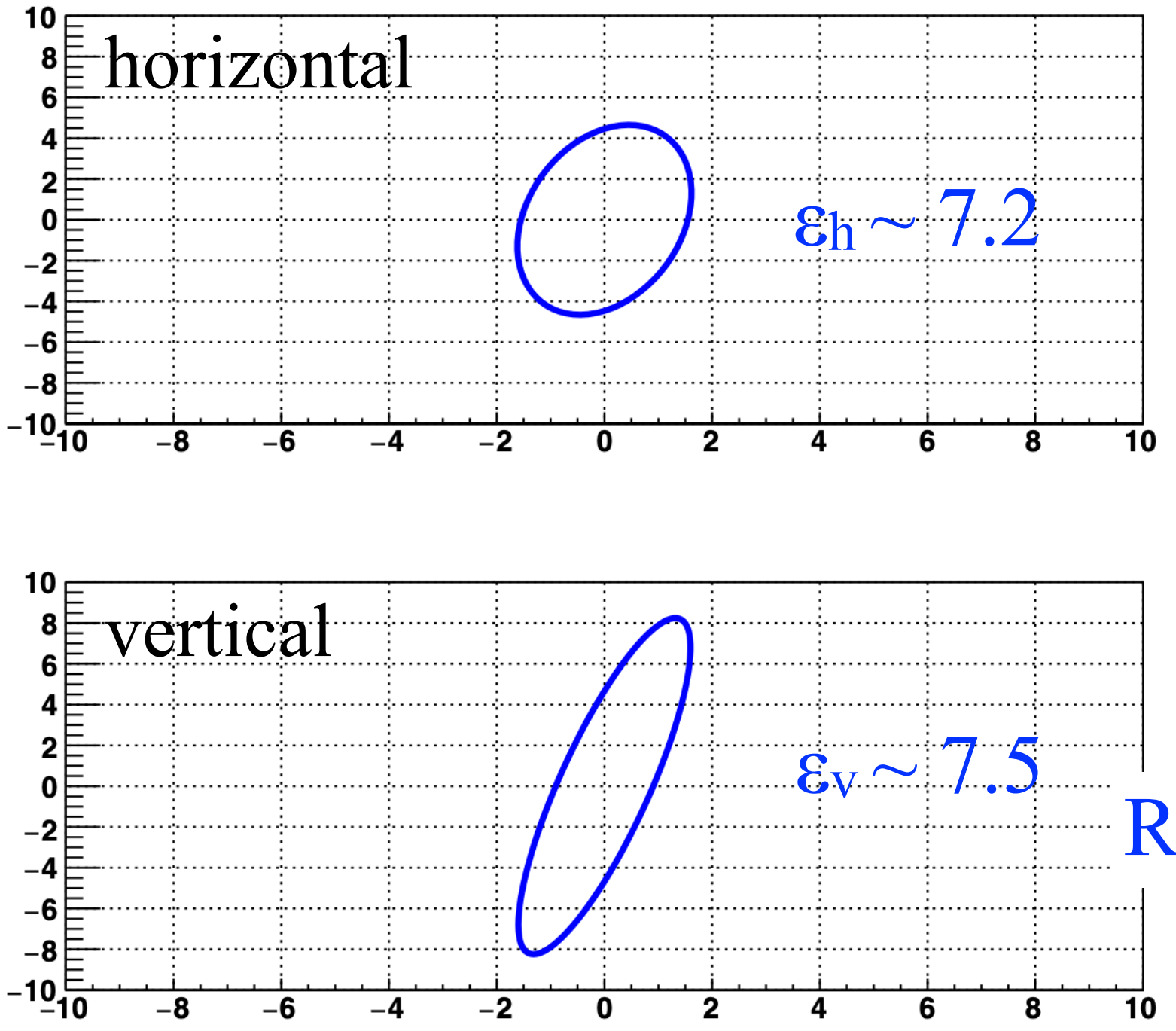
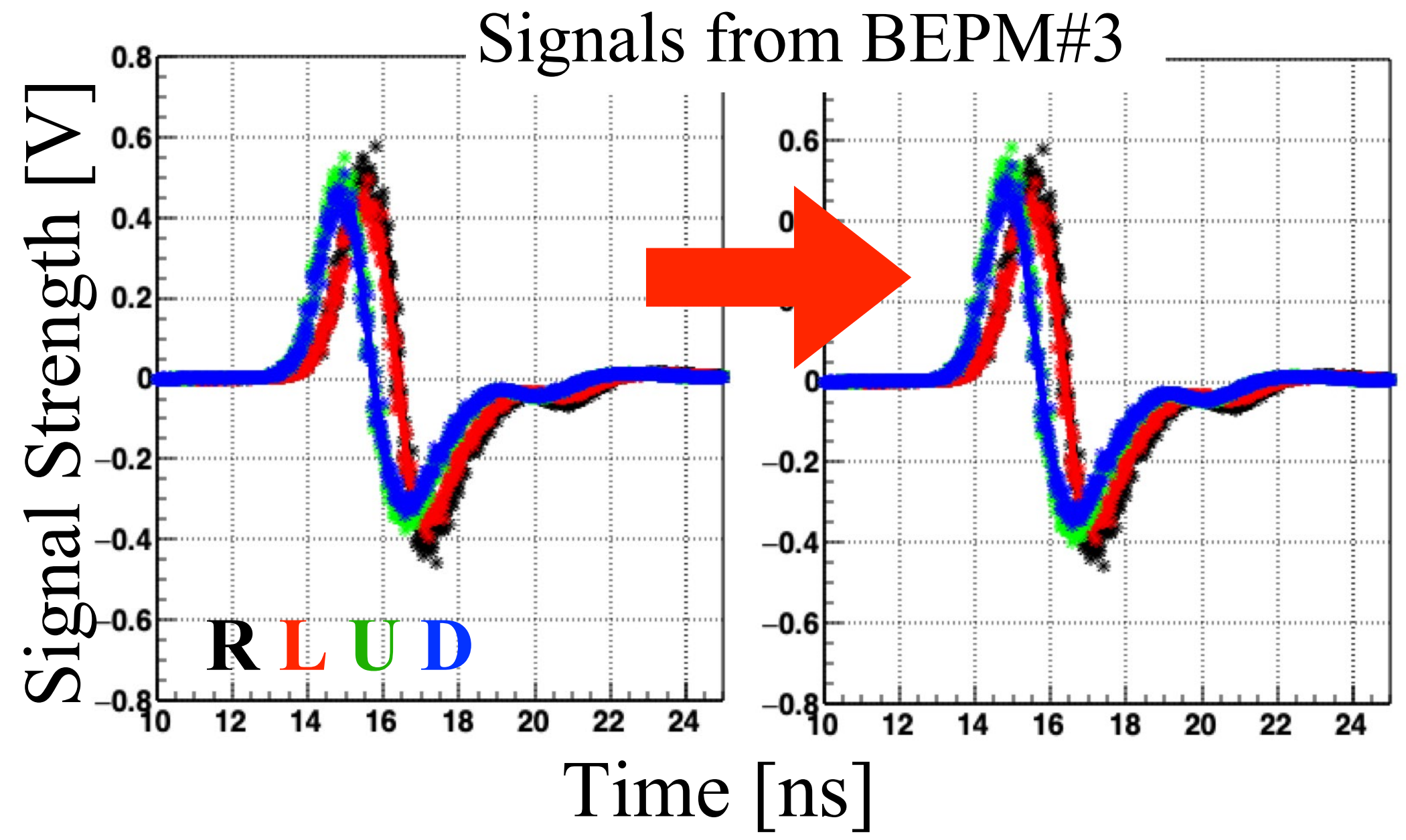




# Solution A: bias factor correction

Bias factors can be estimated to reproduce Q-scan results.

### Phase Ellipse at profile monitor e00



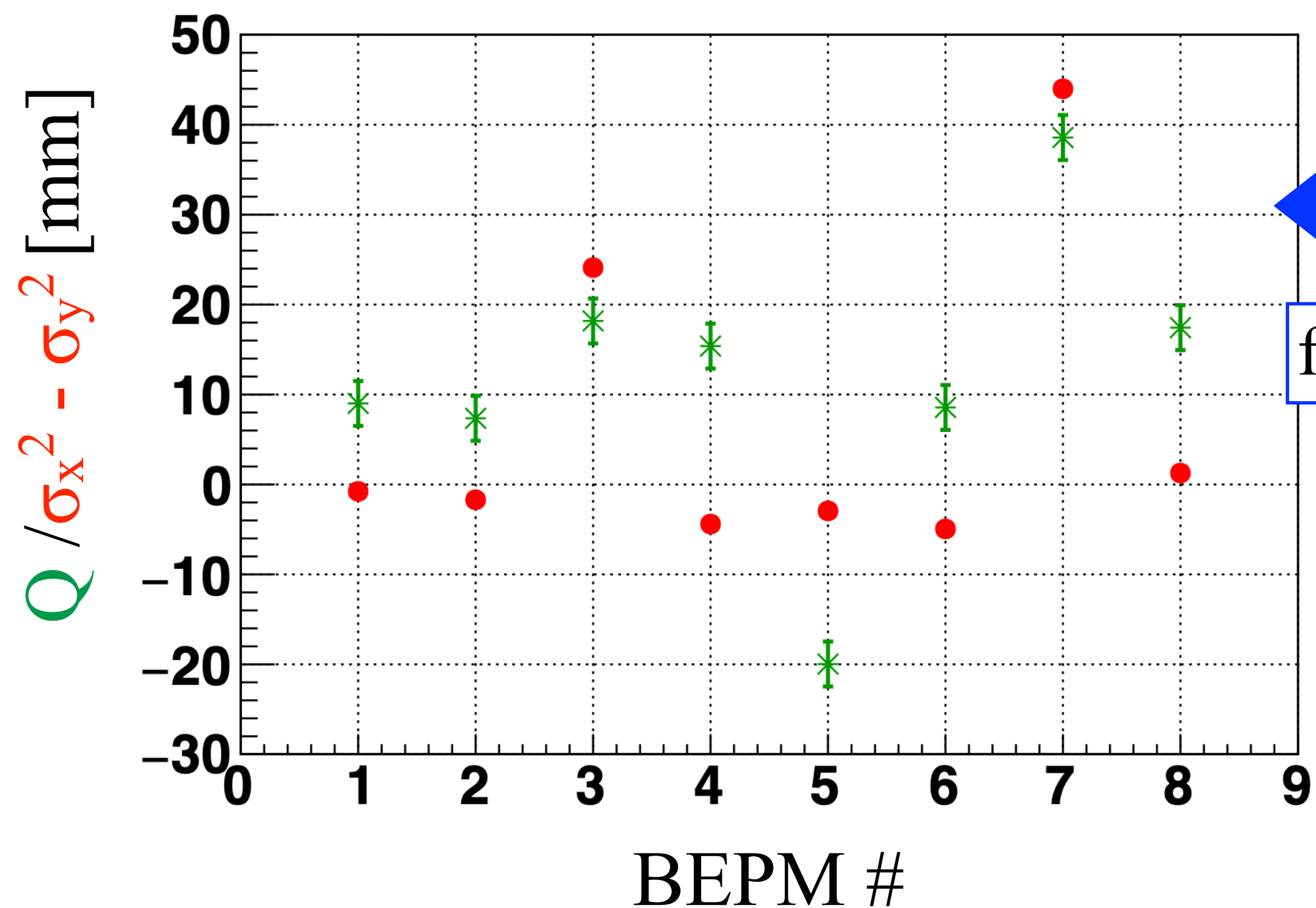
profile monitor @ e00

Result of Q-scan

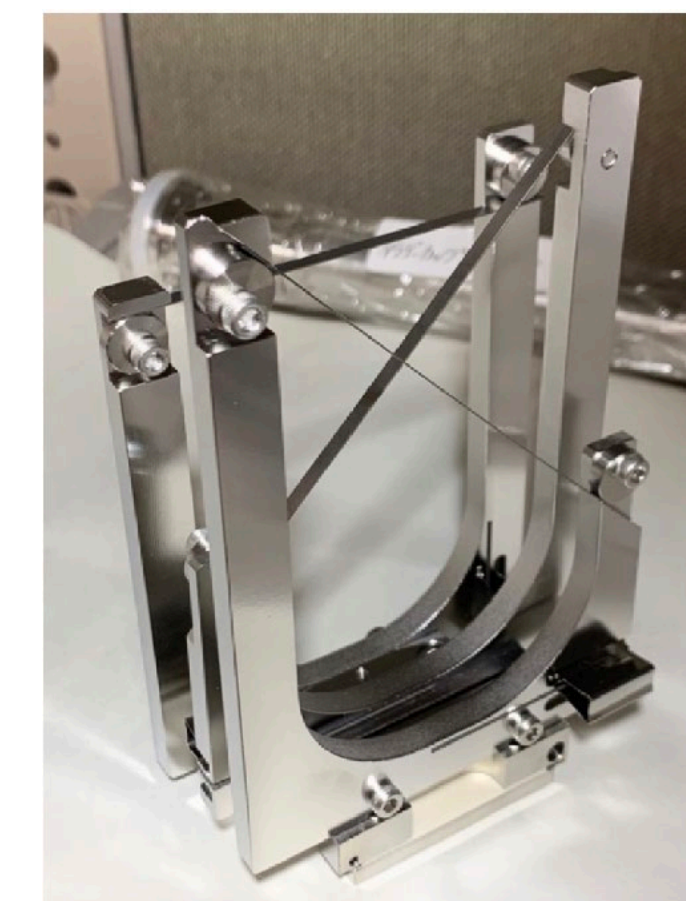
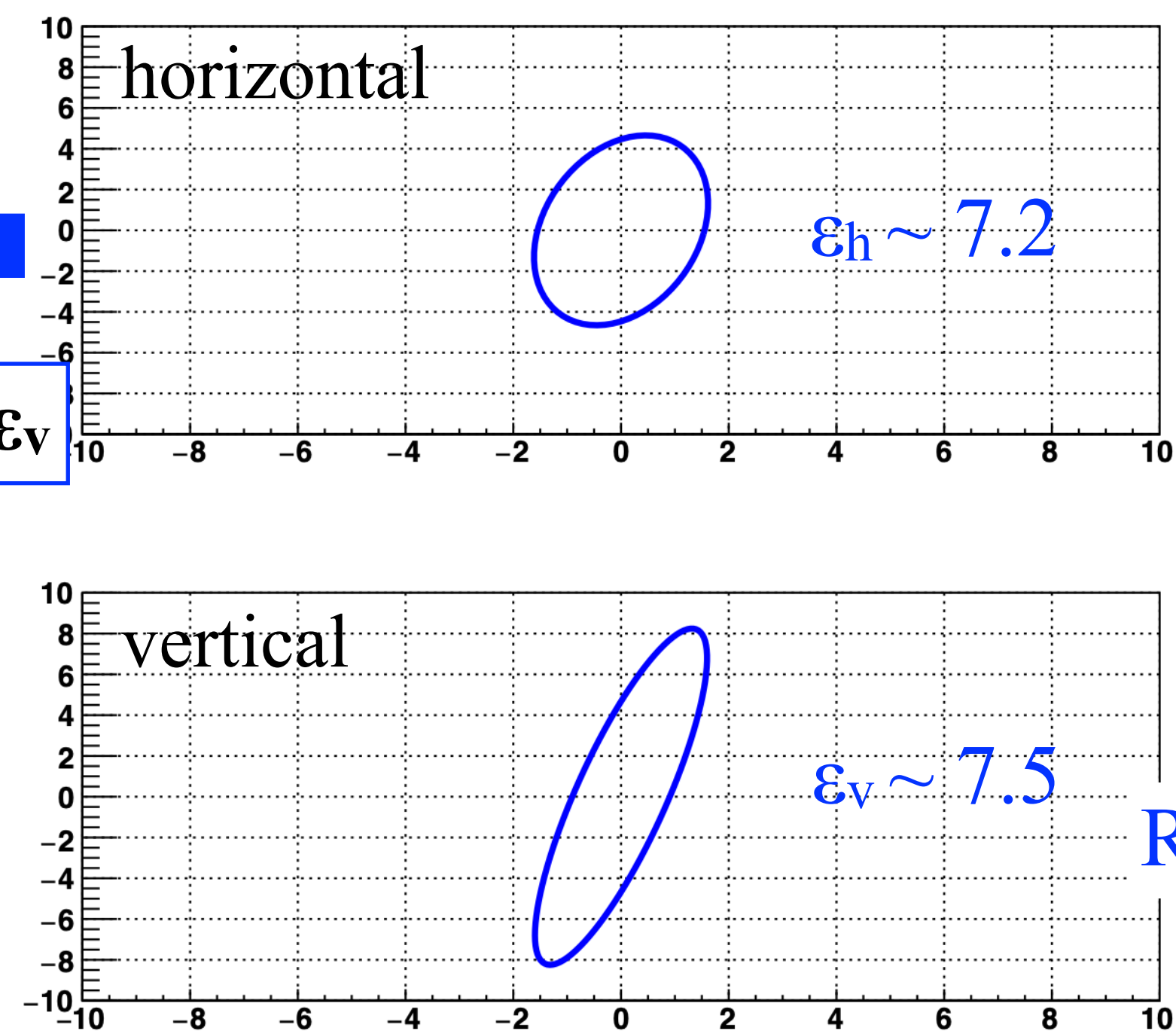


# Solution A: bias factor correction

w/o bias correction



Phase Ellipse at profile monitor e00



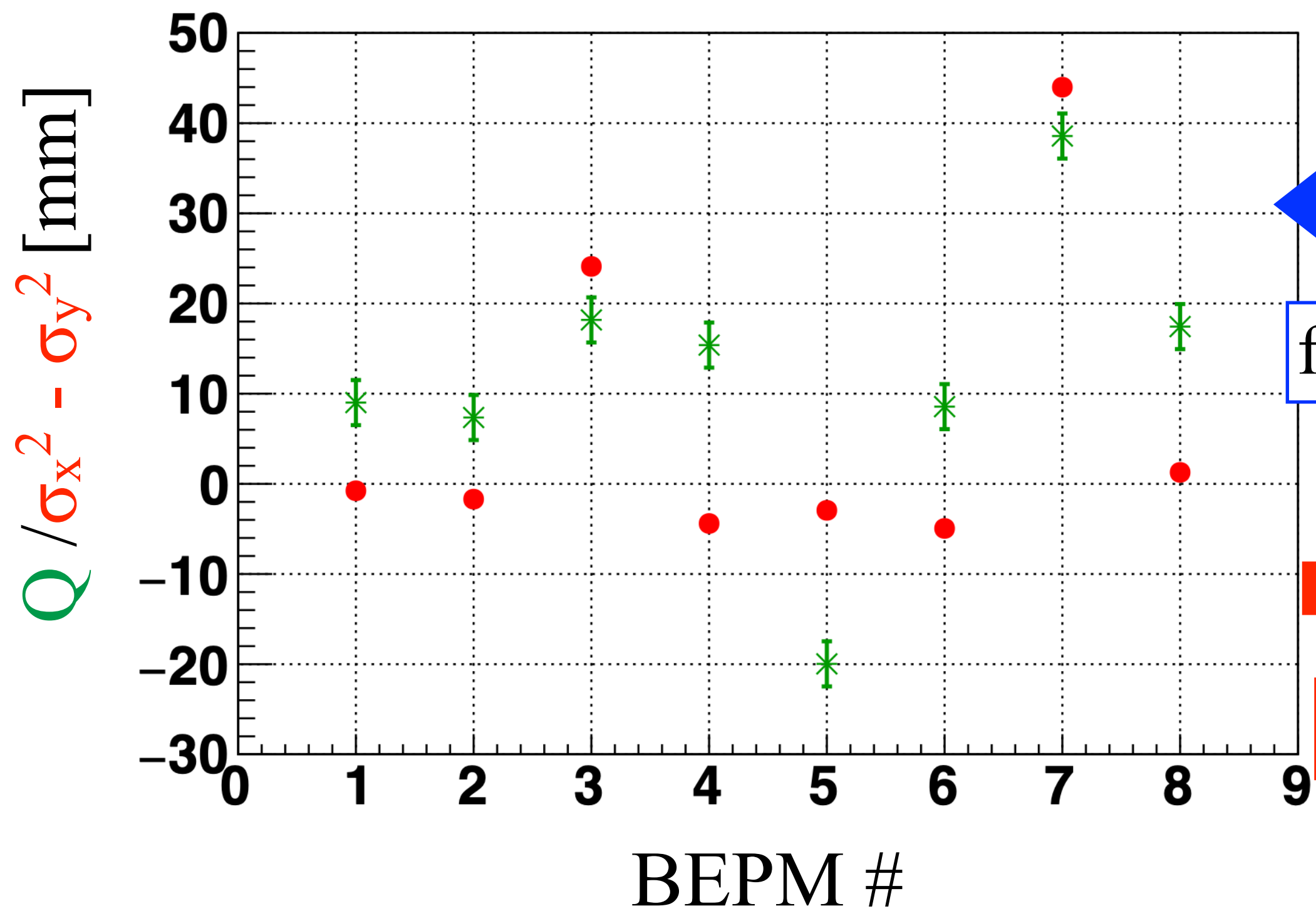
profile monitor @ e00

Result of Q-scan

# Solution A: bias factor correction

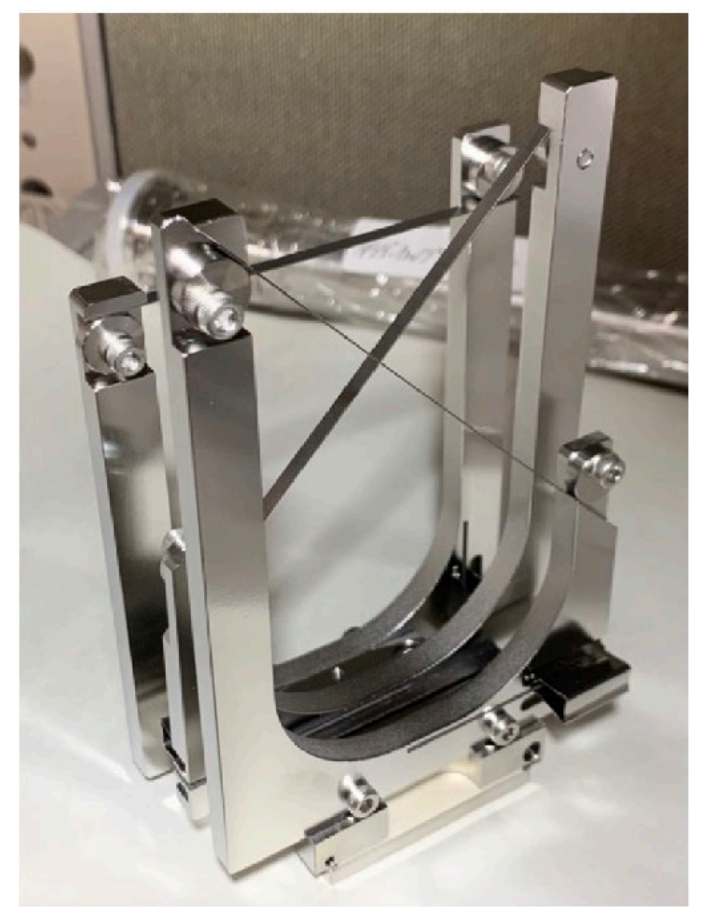
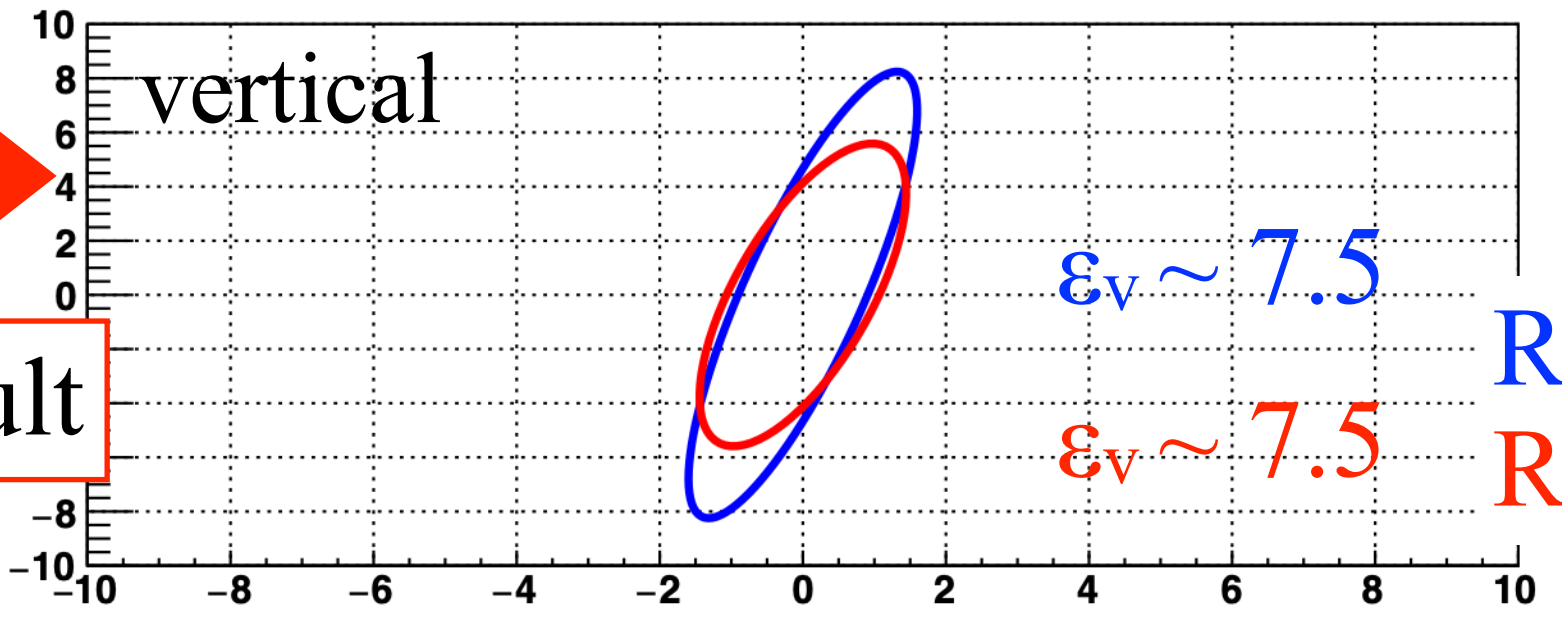
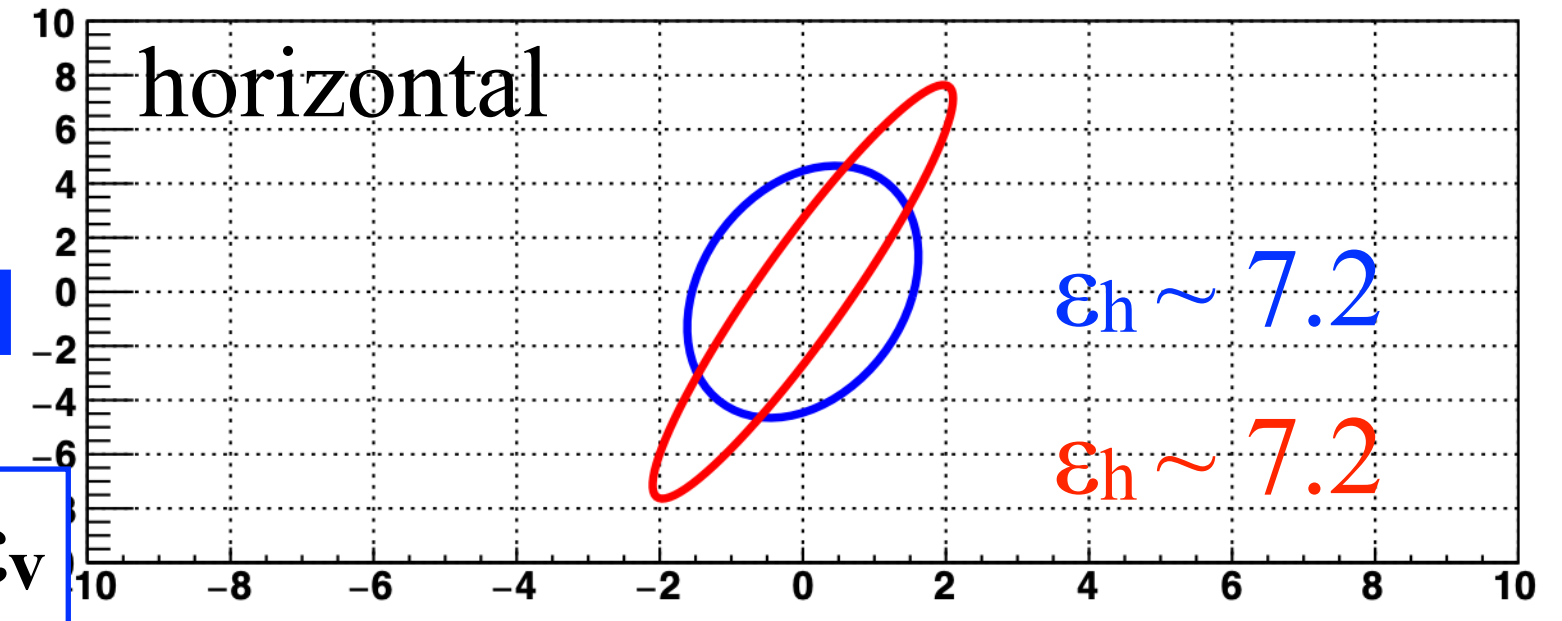
w/o bias correction

Phase Ellipse at profile monitor e00



fix  $\epsilon_h, \epsilon_v$

fit result



profile monitor @ e00

Result of Q-scan  
 Result of BEPM analysis

Measured Qs are not reproduced by the fitting w/o bias correction...

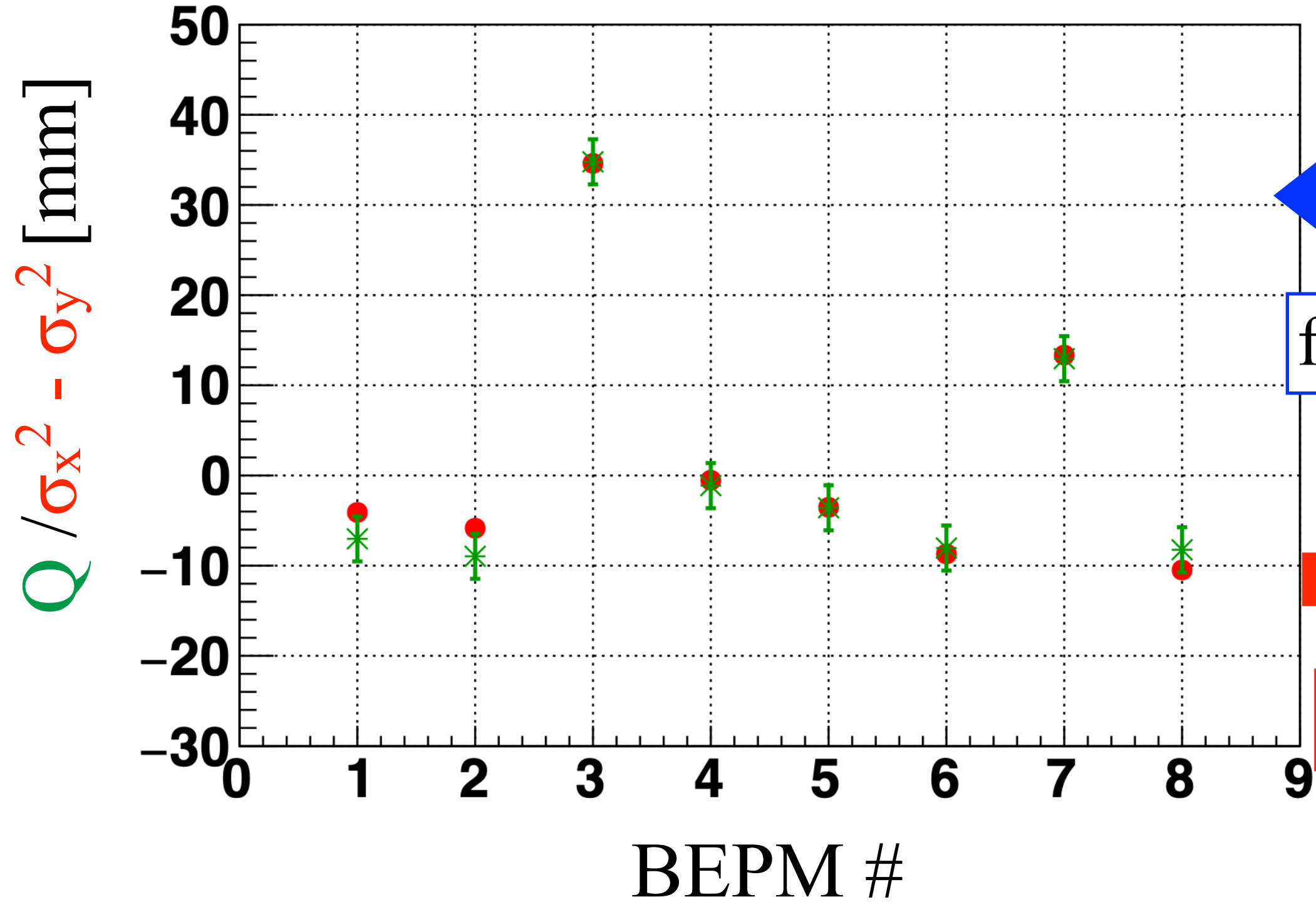


# Solution A: bias factor correction

w/ bias correction

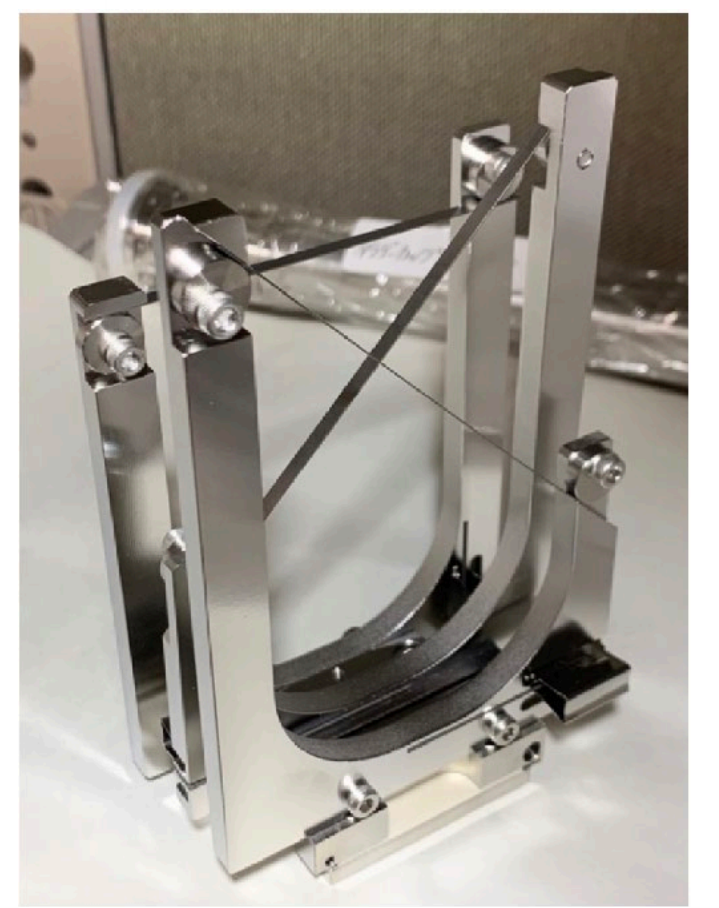
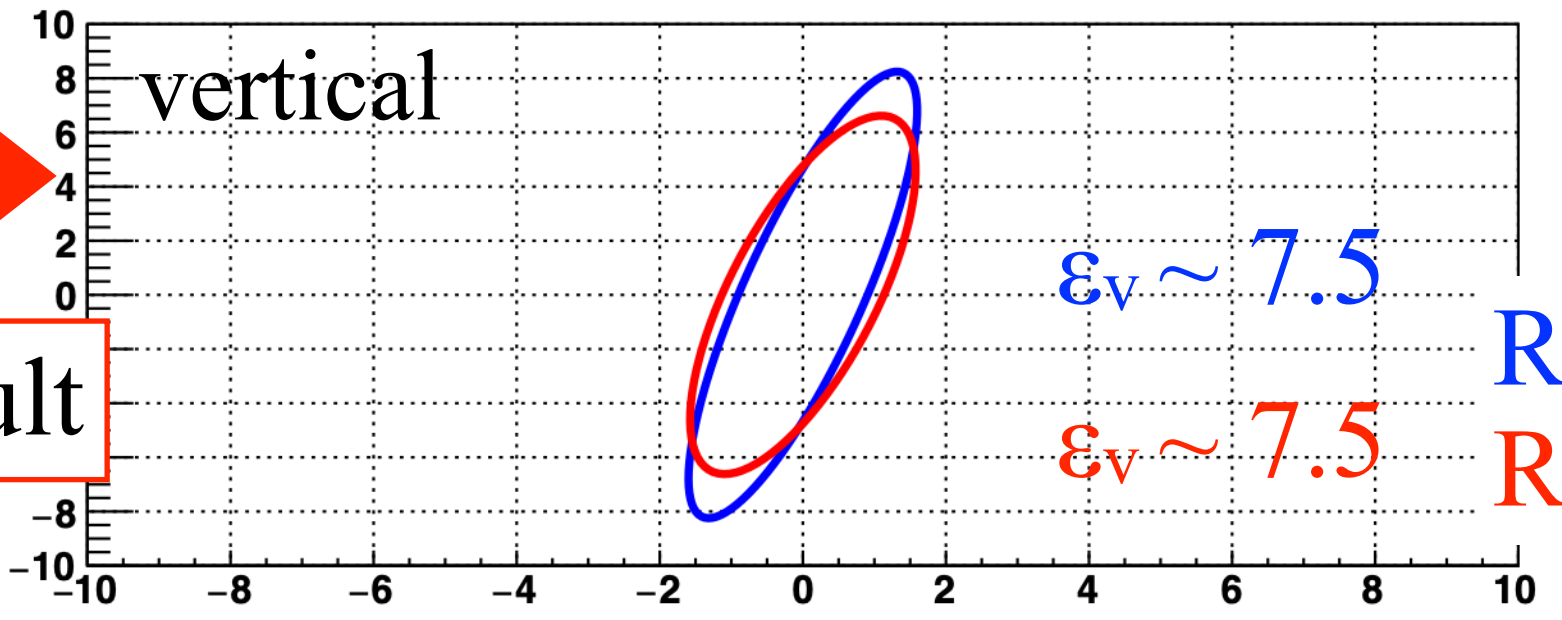
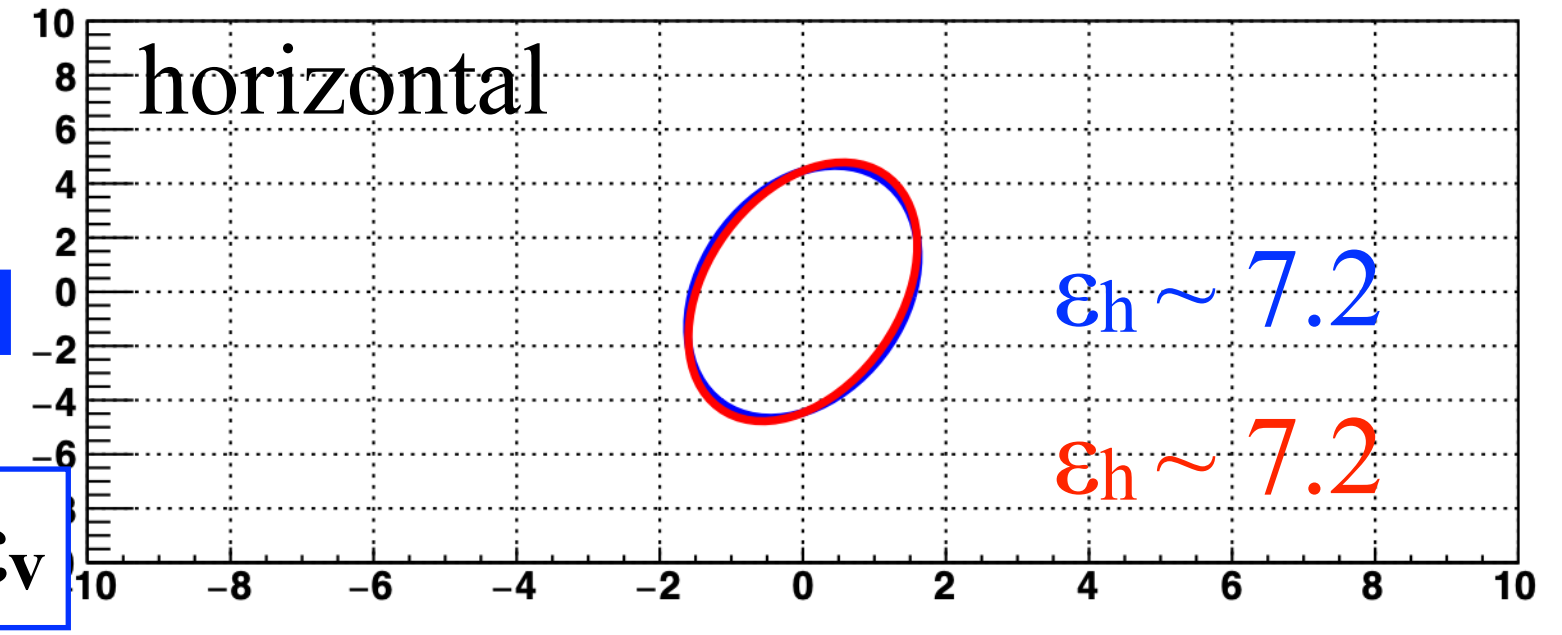
**b = 1.060 / 1.044 (typeA/B)**

Phase Ellipse at profile monitor e00



fix  $\epsilon_h, \epsilon_v$

fit result



profile monitor @ e00

Result of Q-scan  
 Result of BEPM analysis

Measured Qs are well reproduced by the fitting **with fixed emittance!**

※ Analysis w/o fixed emittance will be discussed latter...

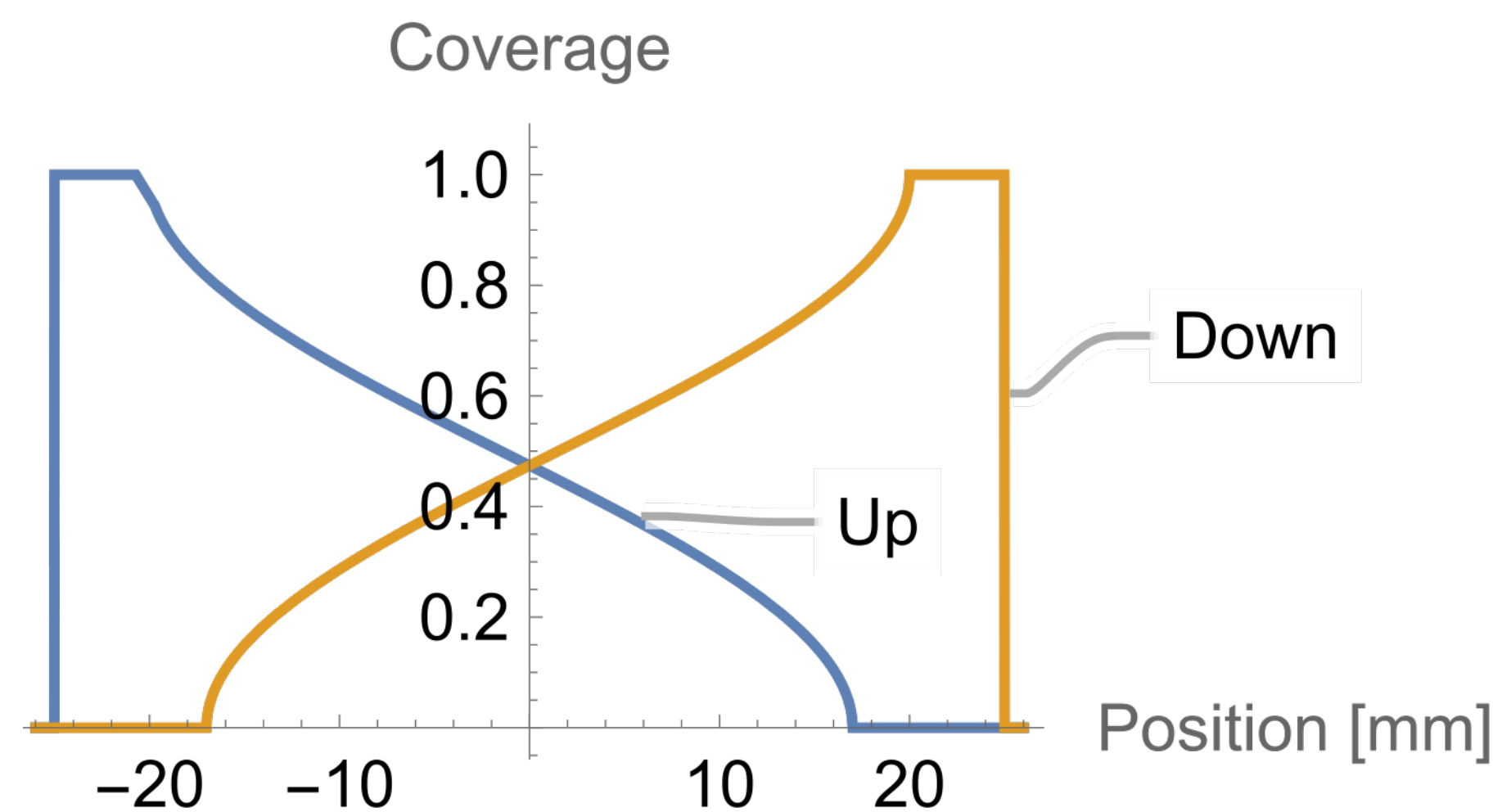
# Solution B: Integral wave form signals

## Solution B: Use double integrated signals

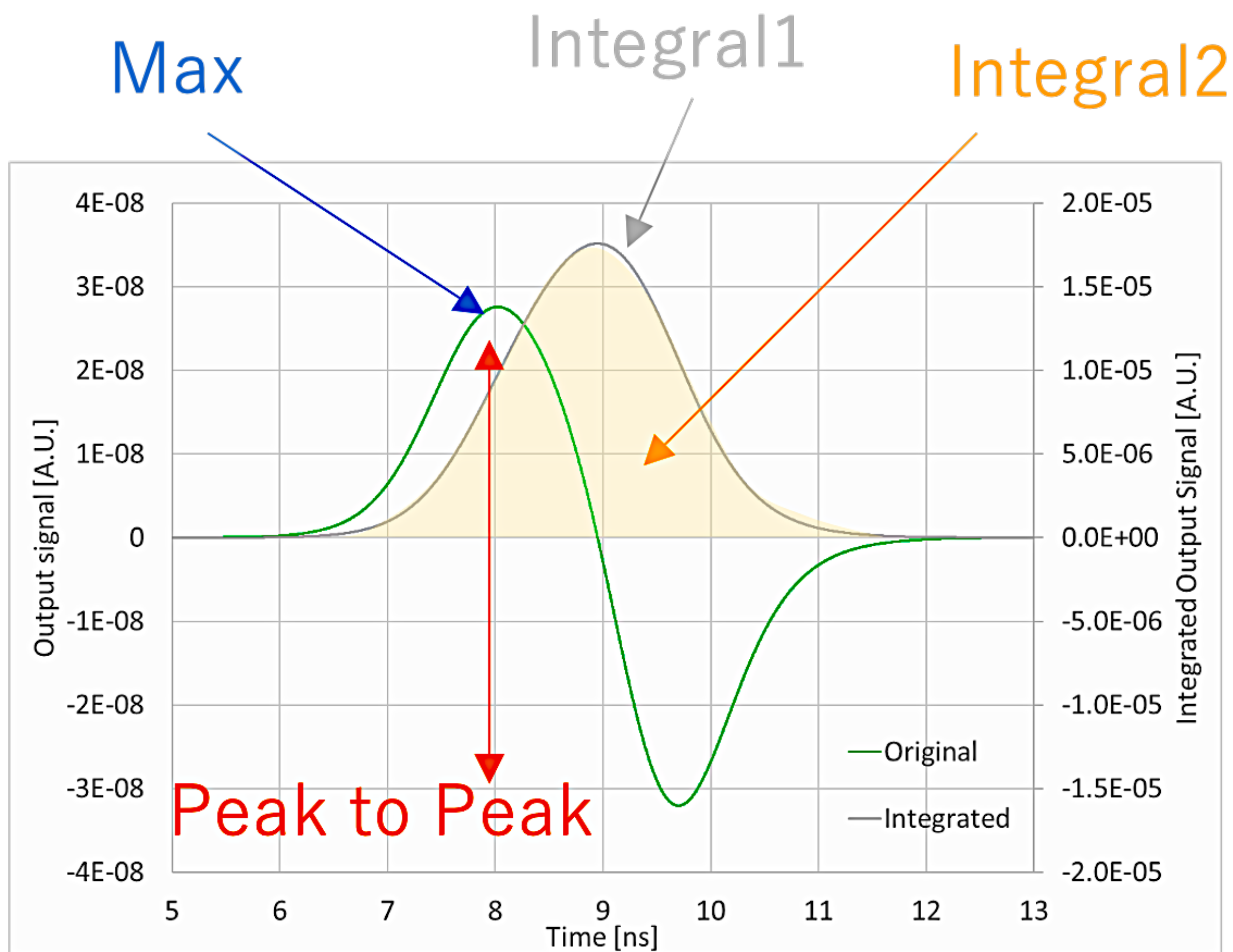
The effect caused by

**time difference from different part of electrode**

→ The effect disappear for the integrated signals.



Shape functions of Up and Down electrode

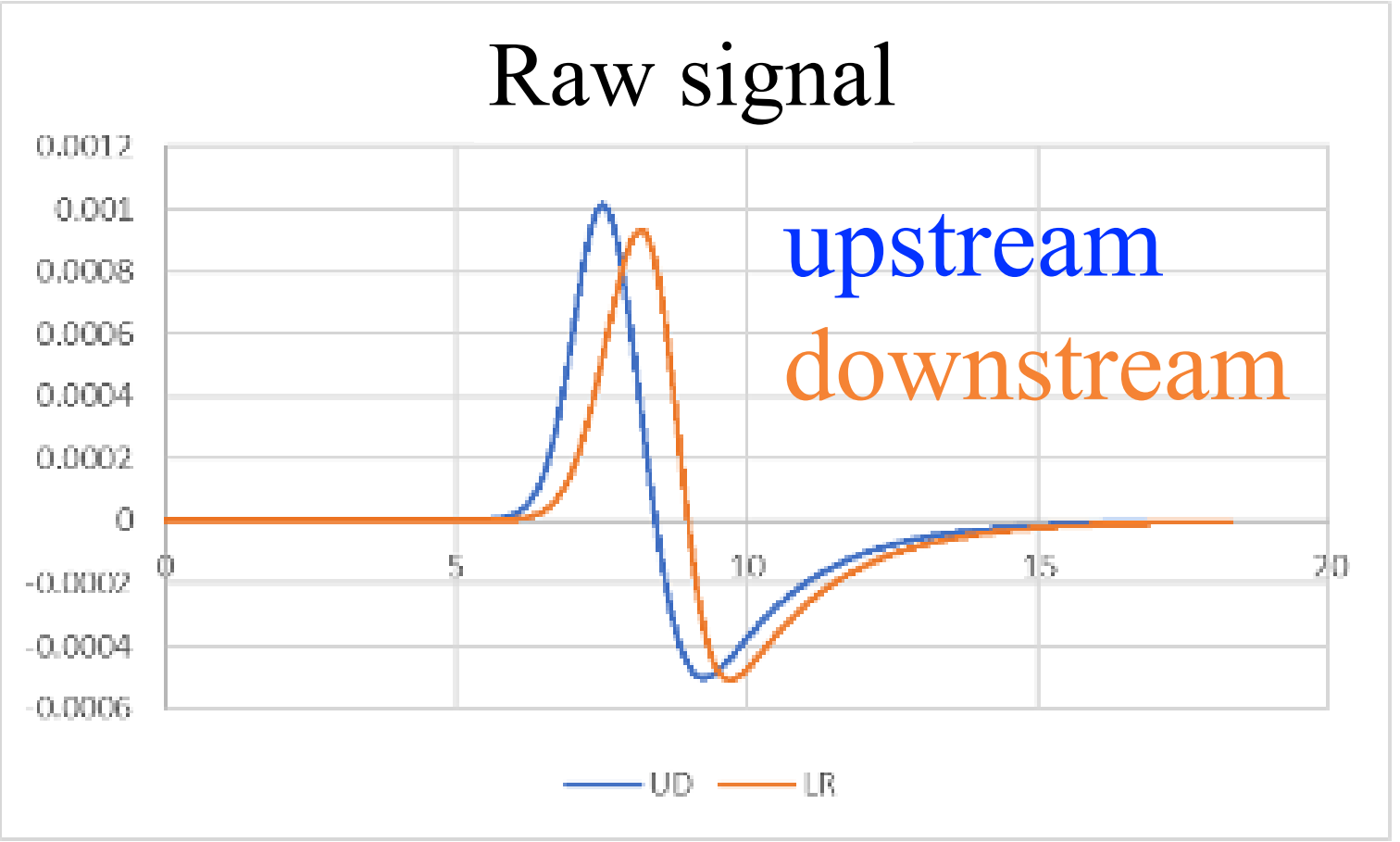




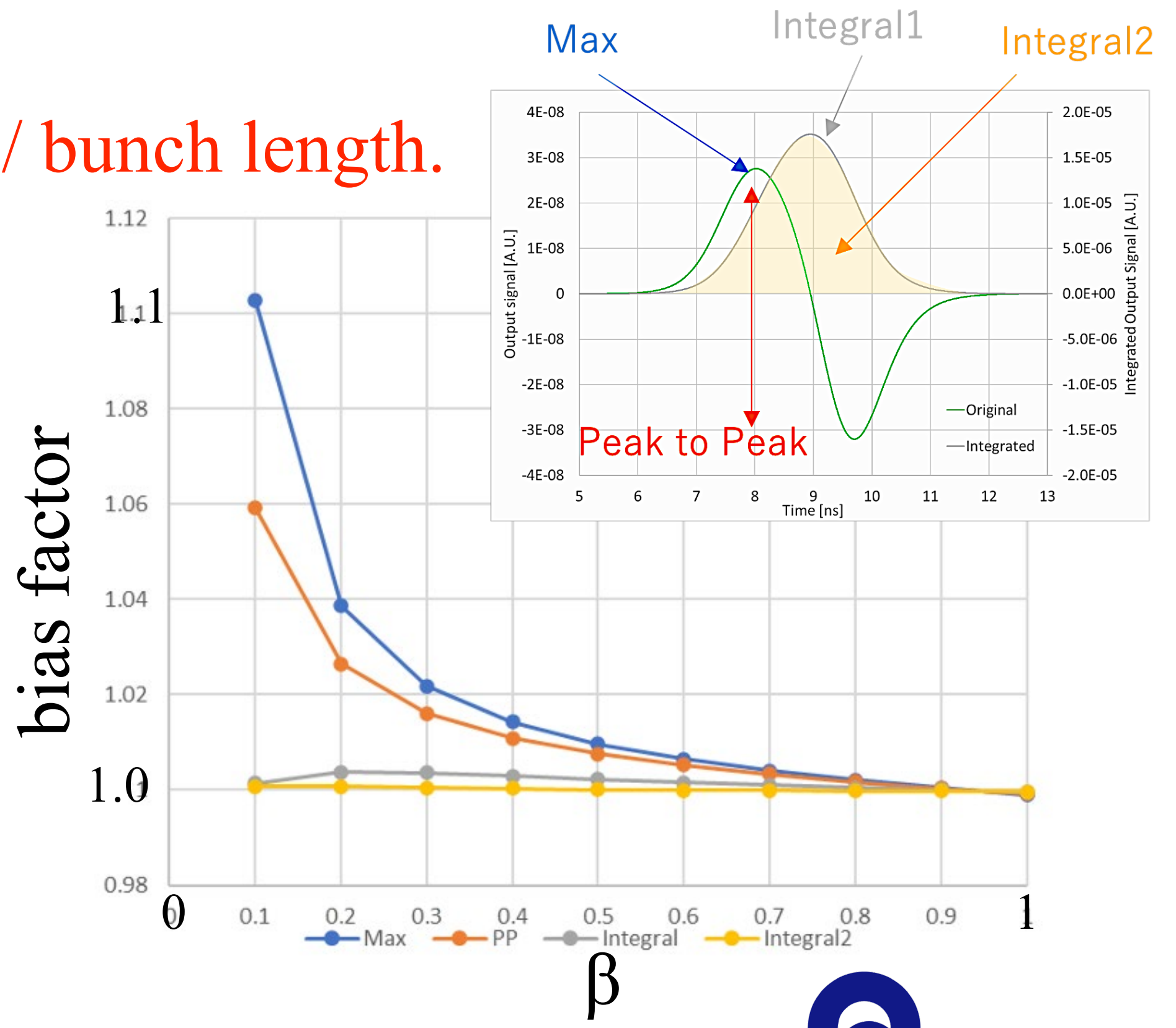
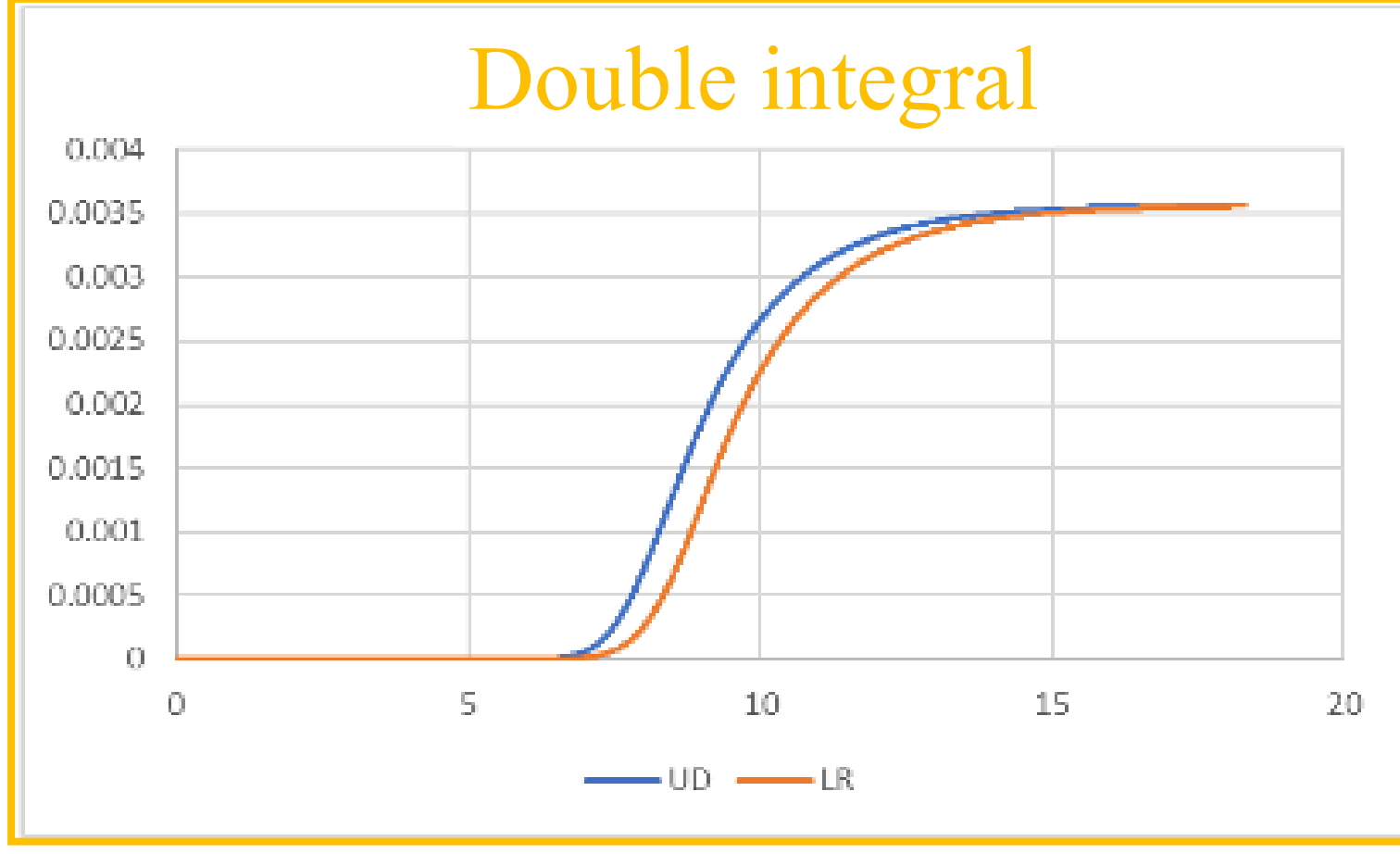
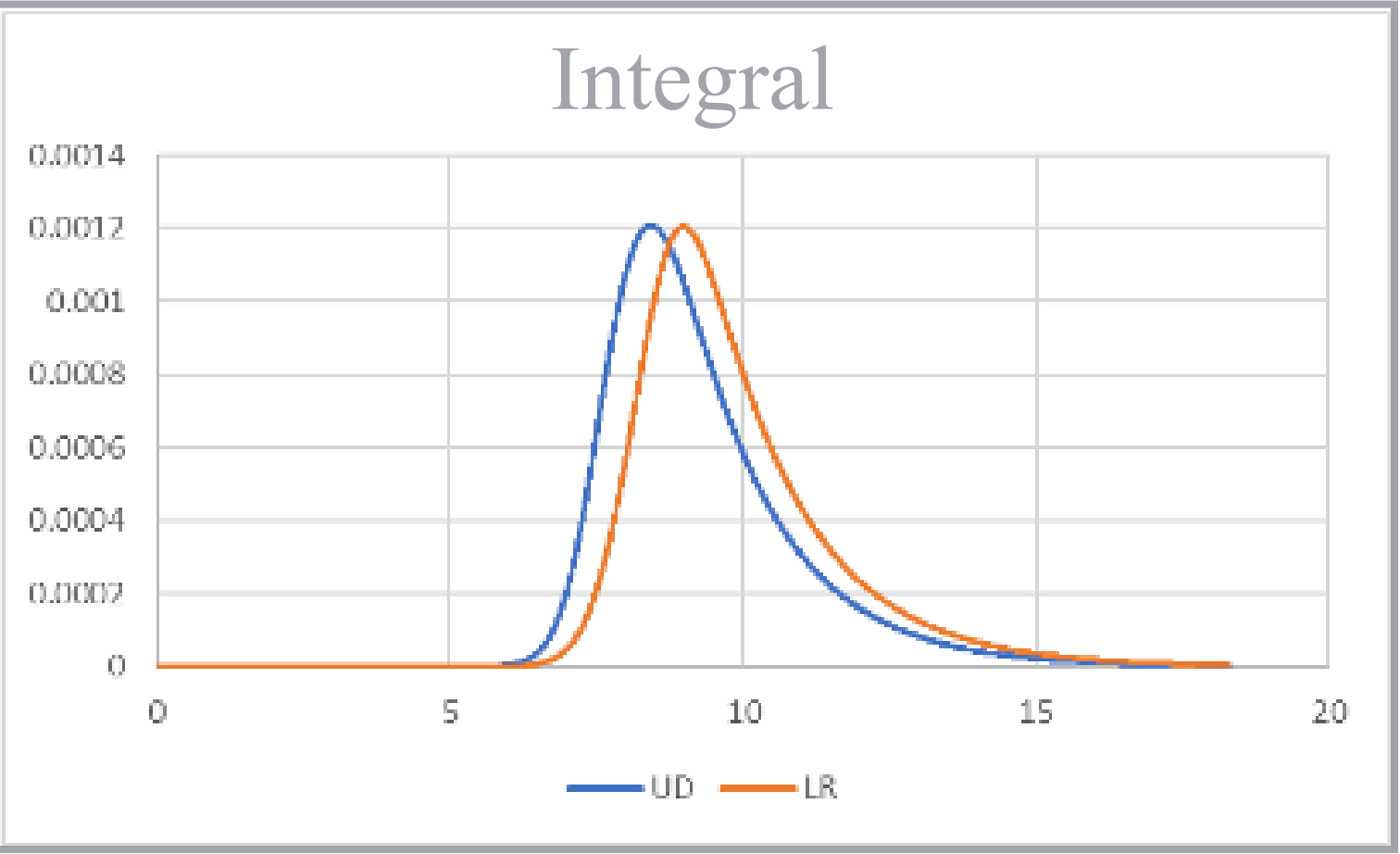
# Solution B: Integral wave form signals

CST Simulation

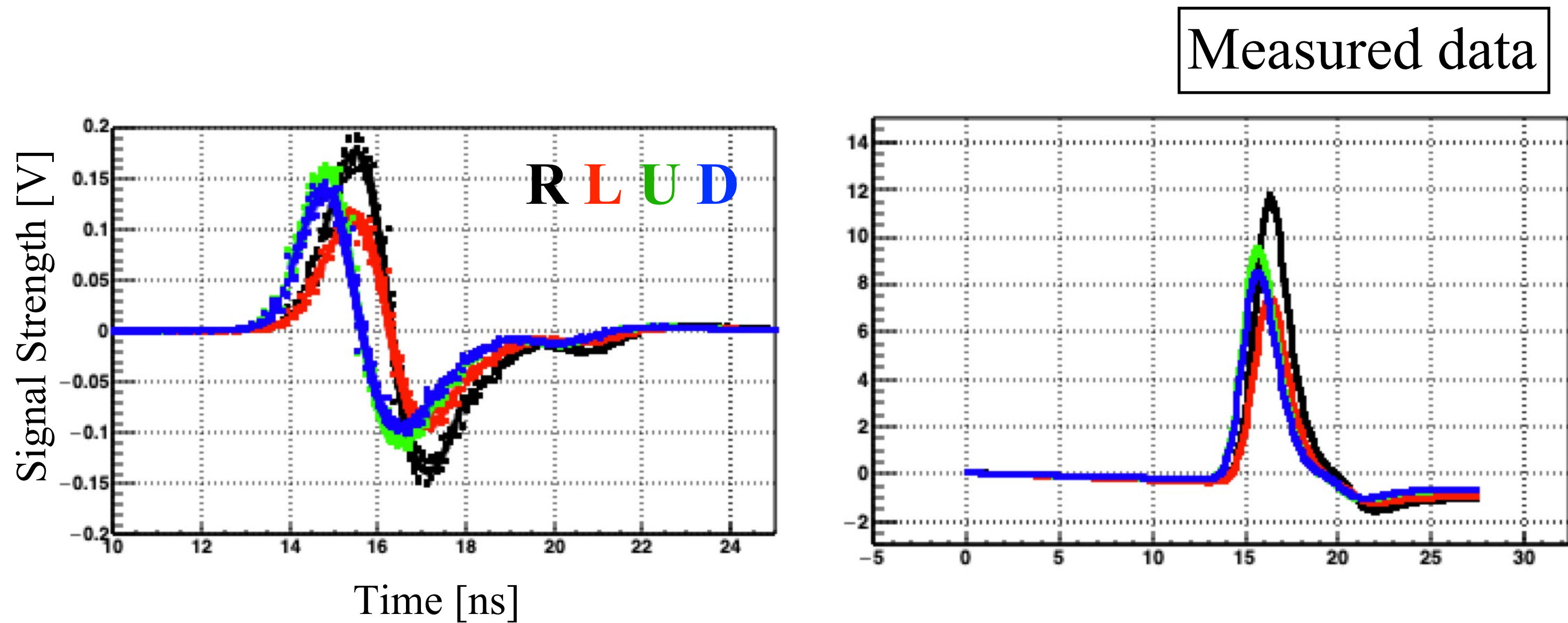
T. Adachi *et al.*, Proc. of PASJ2023, THOA4 (2023)  
Patent application number 2023-128268 (JP)



Double integration of the signal seems promising for eliminating the bias effect.  
**CST simulation shows no bias for double integration in any  $\beta$  / bunch length.**



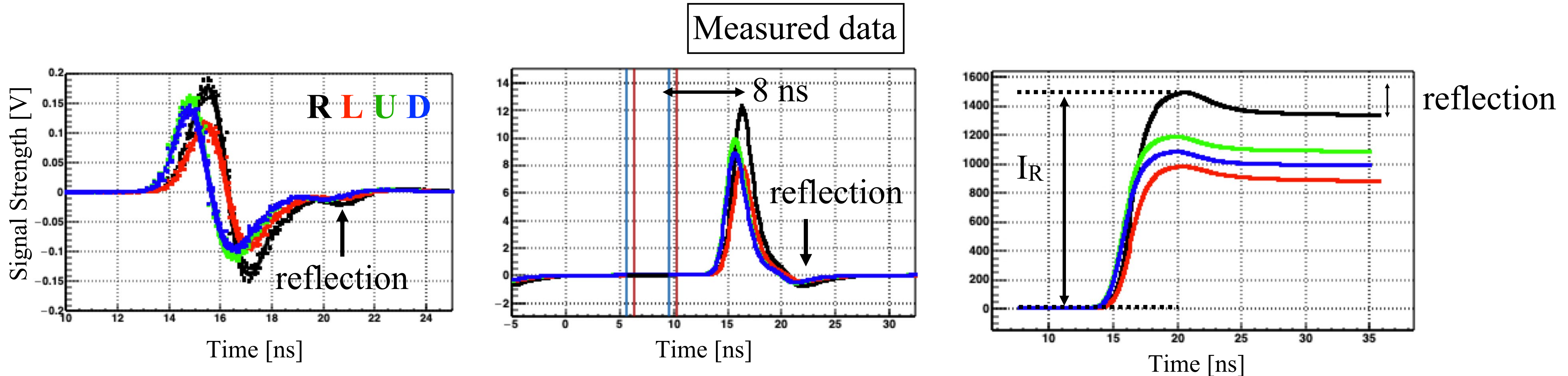
# Solution B: Integral wave form signals



Simple integration is not robust for offset of the signal.



# Solution B: Integral wave form signals



Simple integration is not robust for offset of the signal.

→ After the correction of the slope (cyclic boundary condition) and offset in integration, double integration and corresponding Qs are calculated.

$$Q_i^I = k_q \frac{I_{Li} + I_{Ri} - I_{Ui} - I_{Di}}{I_{Li} + I_{Ri} + I_{Ui} + I_{Di}} - \langle x^I \rangle^2 + \langle y^I \rangle^2$$

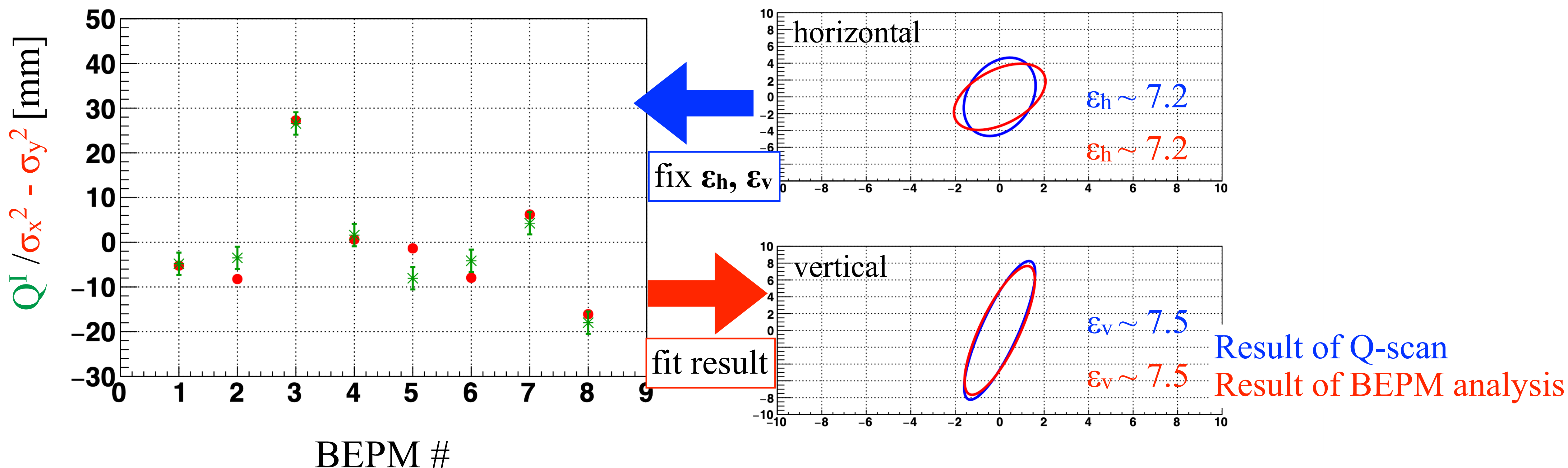
※ k<sub>q</sub> is the same as for the peak to peak values. / ⟨x⟩ , ⟨y⟩ should be also re-calculated with integrations.



# Solution B: Integral wave form signals

Fit with  $Q^I$   
calculated by double integration

Phase Ellipse at profile monitor e00



Measured  $Q$ s are again well reproduced as with calculated  $Q$  with bias corrections.

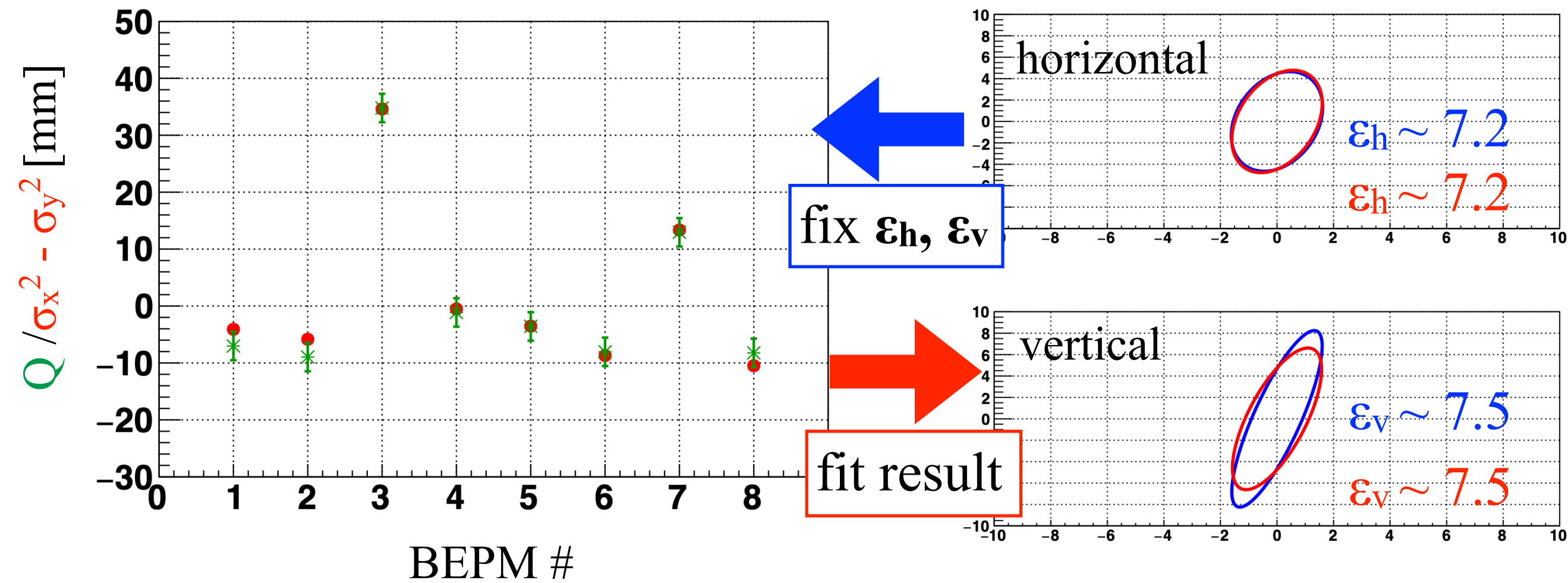
※  $\epsilon_h, \epsilon_v$  are still fixed!



# Comparison between solution A/B

Bias correction

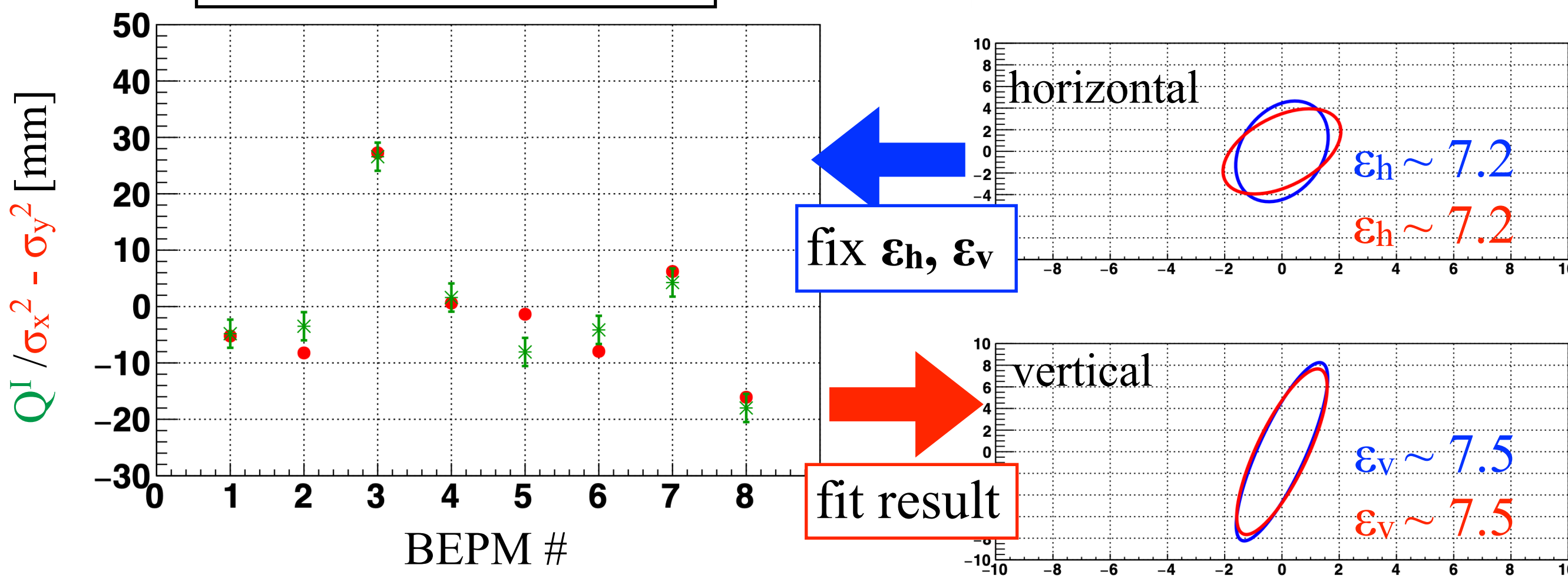
Phase Ellipse at profile monitor e00



- Both method works well
- Double integration method is more comprehensive / robust for beam conditions.
- So far, only peak to peak values are archived in data base.  
(wave form signals are not archived)

→ We are preparing program upgrade to archive double integration for coming beam series.

Double integration

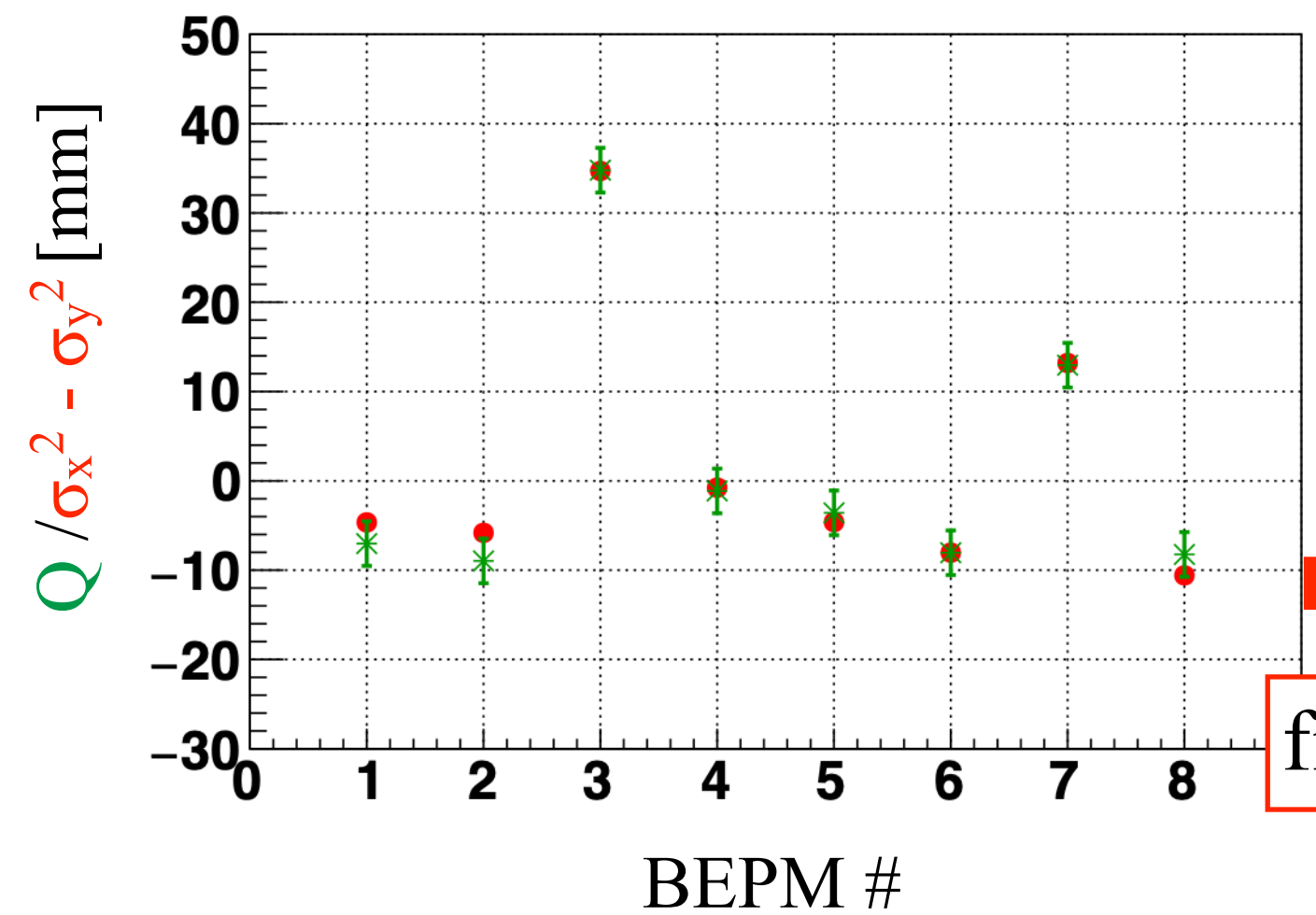


Result of Q-scan  
Result of BEPM analysis

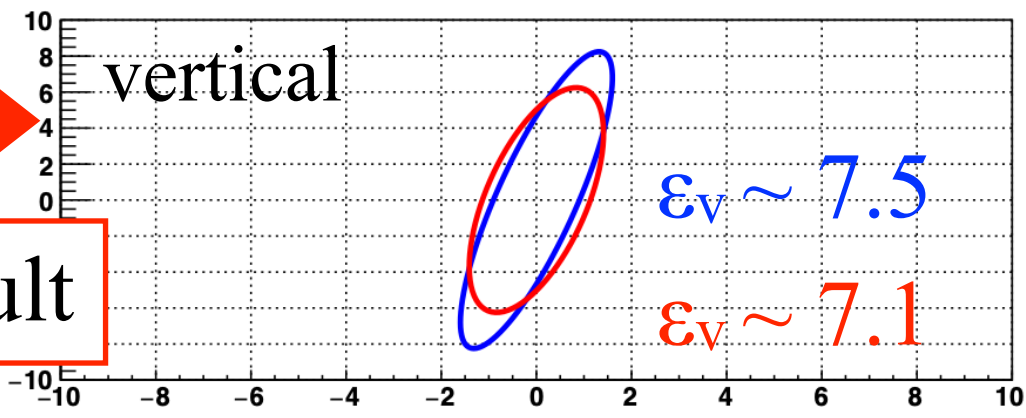
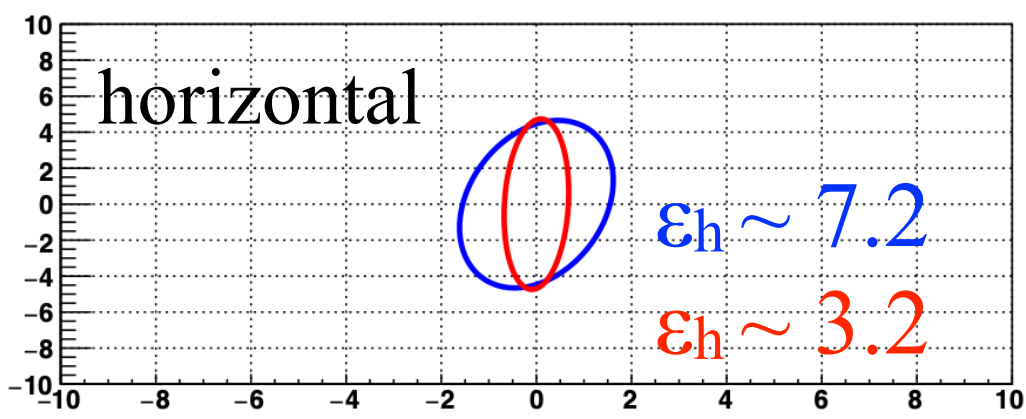


# Comparison between solution A/B

Bias correction

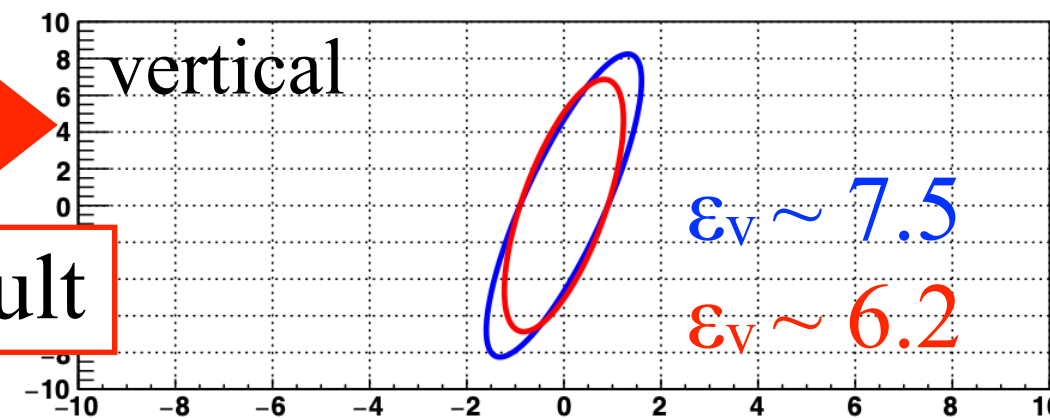
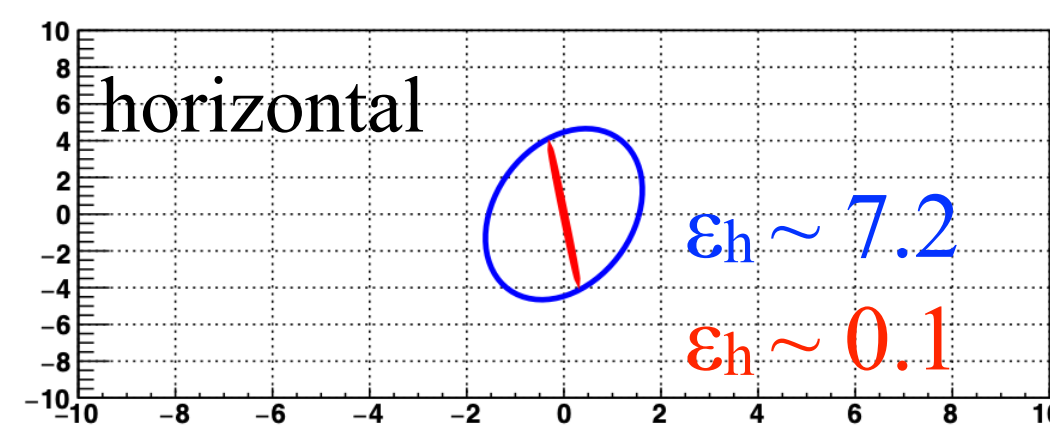
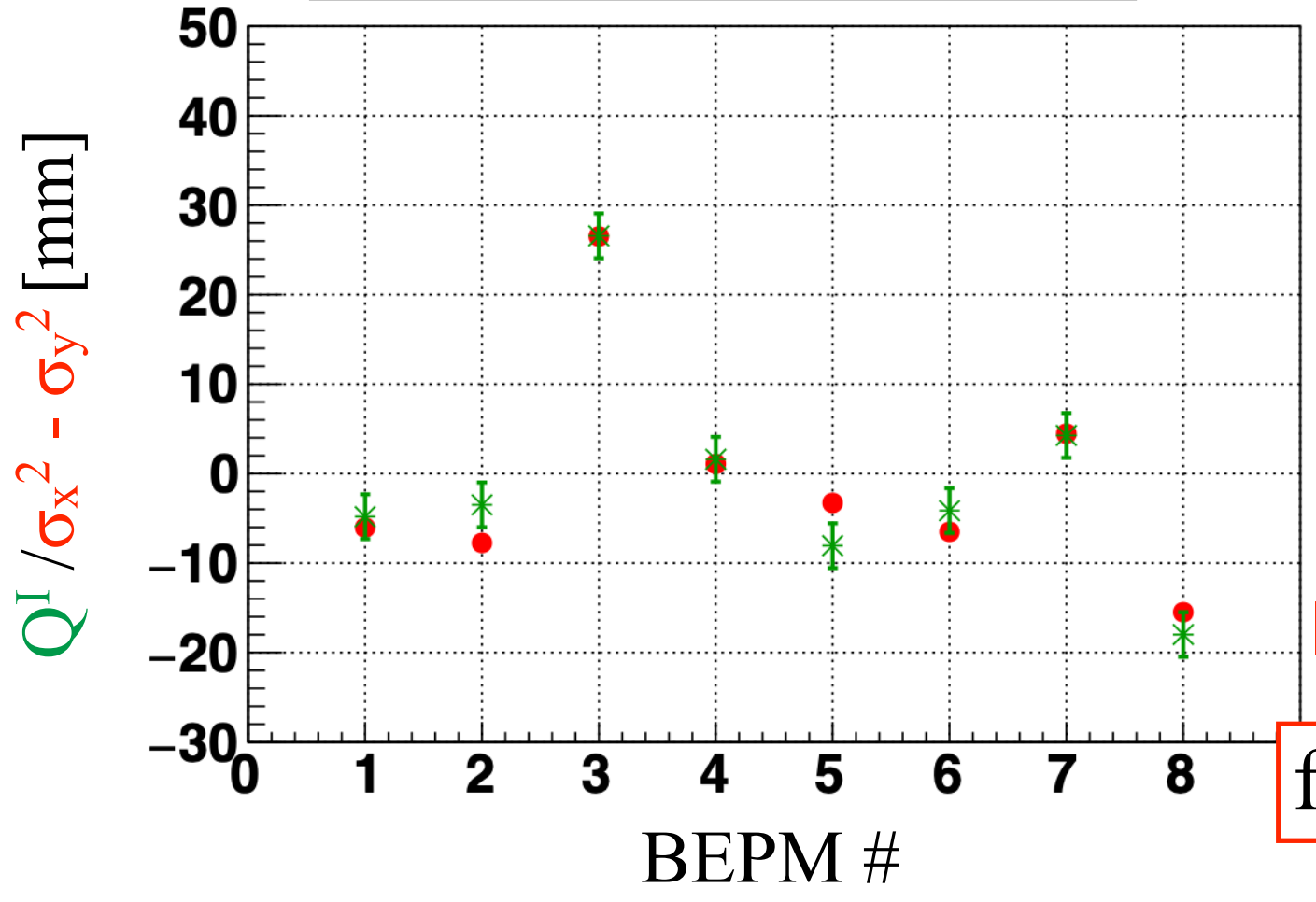


Phase Ellipse at profile monitor e00



fit result

Double integration



fit result

- Both method works well
- Double integration method is more comprehensive / robust for beam conditions.
- So far, only peak to peak values are archived in data base.  
(wave form signals are not archived)

→ We are preparing program upgrade to archive double integration for coming beam series.

In both methods, sensitivities for  $\epsilon_h$ ,  $\epsilon_v$  are poor...

Result of Q-scan  
Result of BEPM analysis





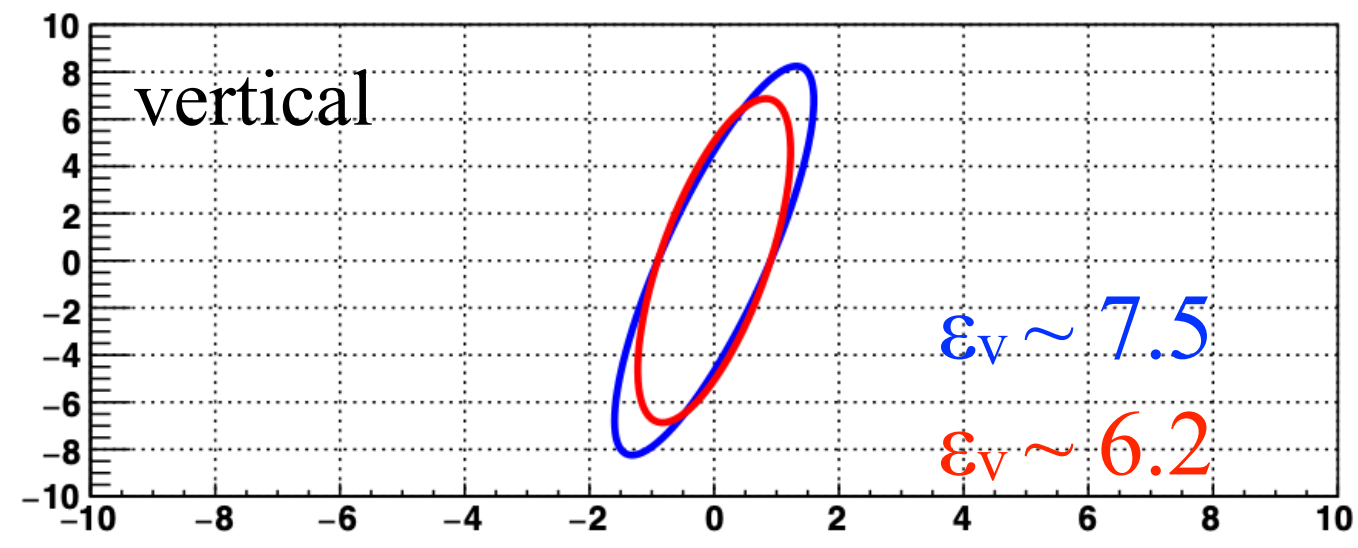
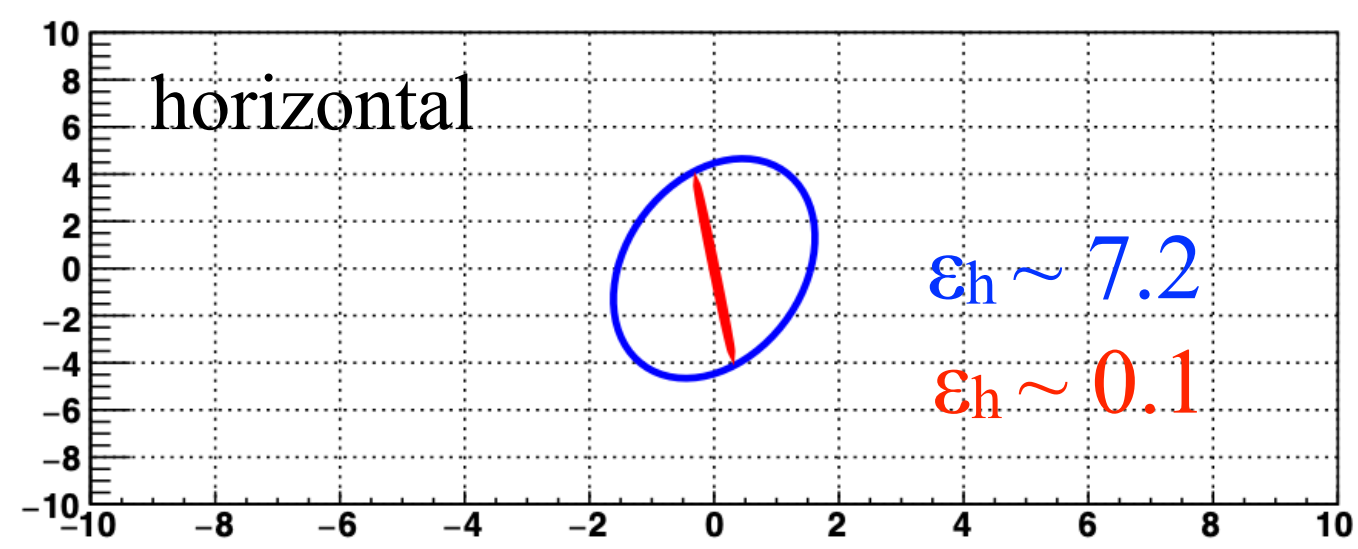
# Outline

1. Introduction: SRILAC and B(E)PMs
2. Beam envelope estimation by BPM signals
3. Signal distortions caused by BPM shapes with short bunch beam
- 4. Improvement of sensitivity for beam emittance**
5. Example of analysis with experimental data
6. Future Outlook and Summary

# Improvement of sensitivity for beam emittance

Phase Ellipse at profile monitor e00  
with double integral method

(1) Limitation of balance between  $\epsilon_h / \epsilon_v$   
ratio between  $\epsilon_h$  and  $\epsilon_v \rightarrow$  expected to be robust in some range  
Fit is performed under the following condition,



Result of Q-scan  
Result of BEPM analysis

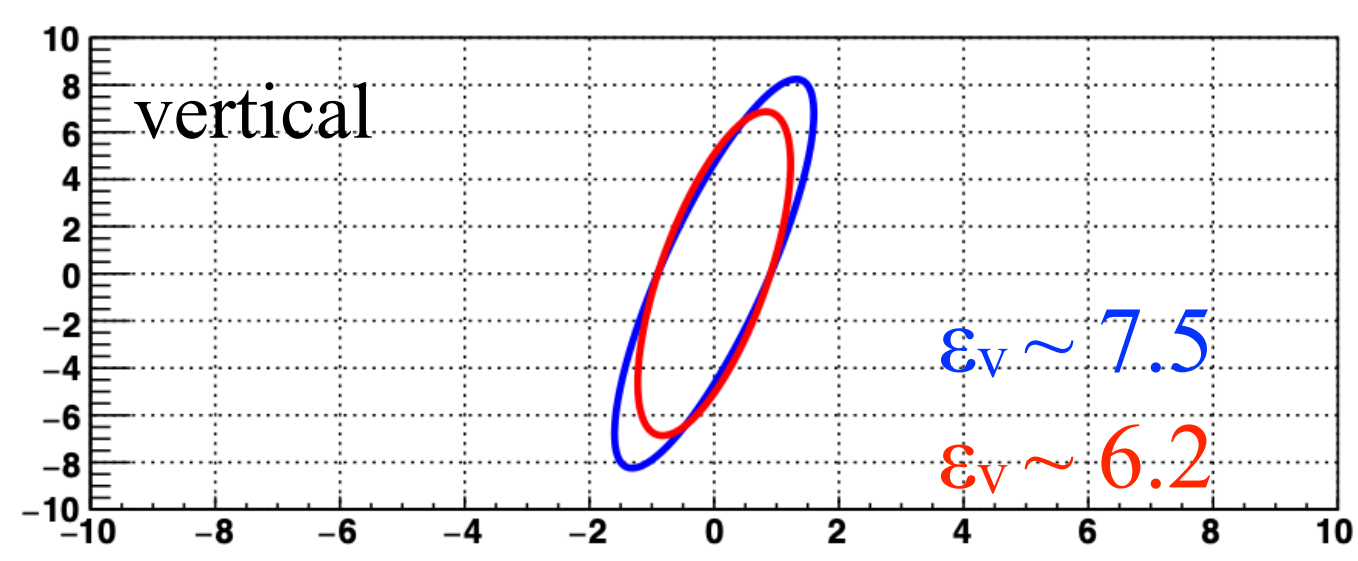
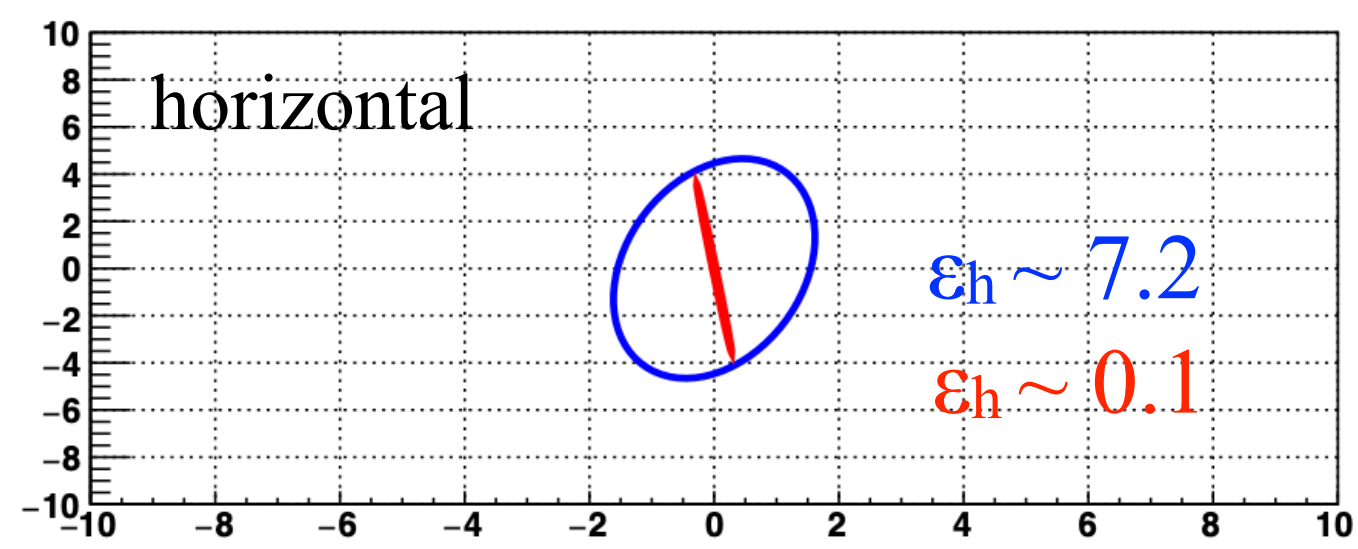
$$|\epsilon_{\text{asym}}| \equiv \left| \frac{\epsilon_h - \epsilon_v}{\epsilon_h + \epsilon_v} \right| \leq 0.1. \text{ ※ } \Delta\epsilon \sim 20\% \text{ in maximum}$$





# Improvement of sensitivity for beam emittance

Phase Ellipse at profile monitor e00 with double integral method

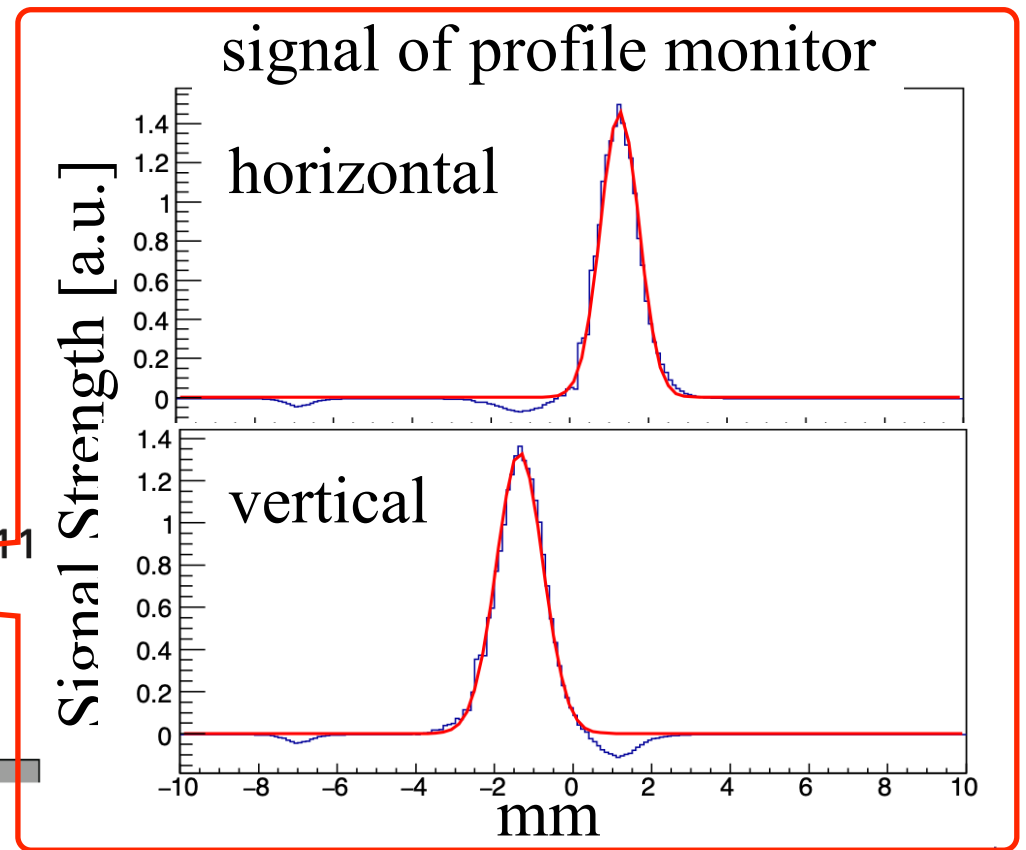
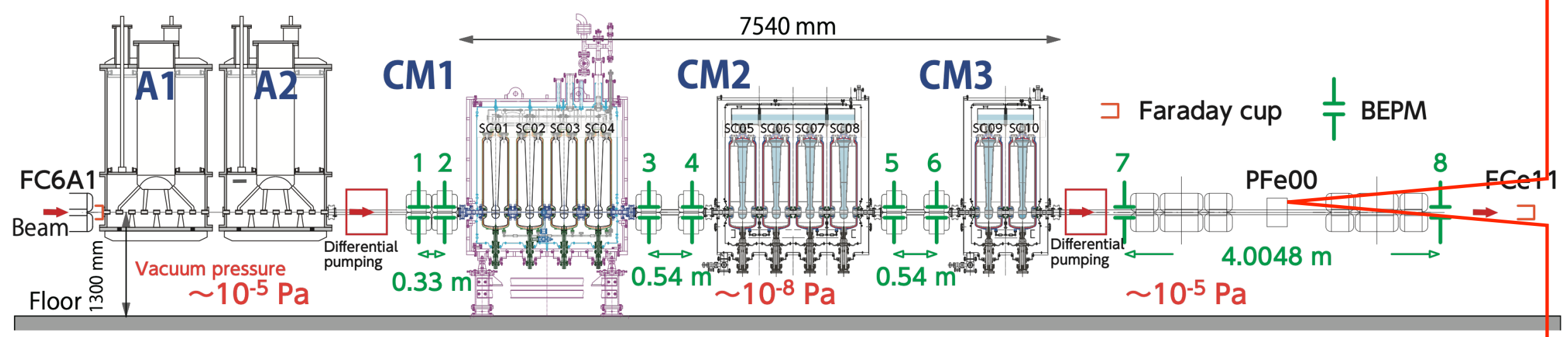


Result of Q-scan  
Result of BEPM analysis

- (1) Limitation of balance between  $\epsilon_h / \epsilon_v$  ratio between  $\epsilon_h$  and  $\epsilon_v \rightarrow$  expected to be robust in some range  
Fit is performed under the following condition,

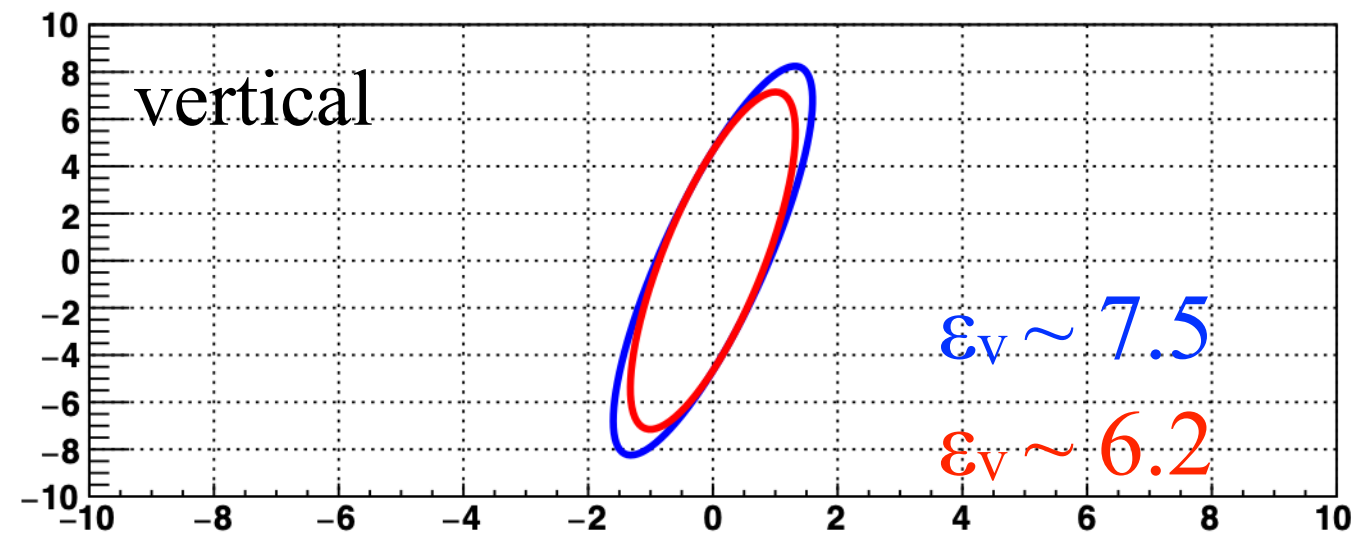
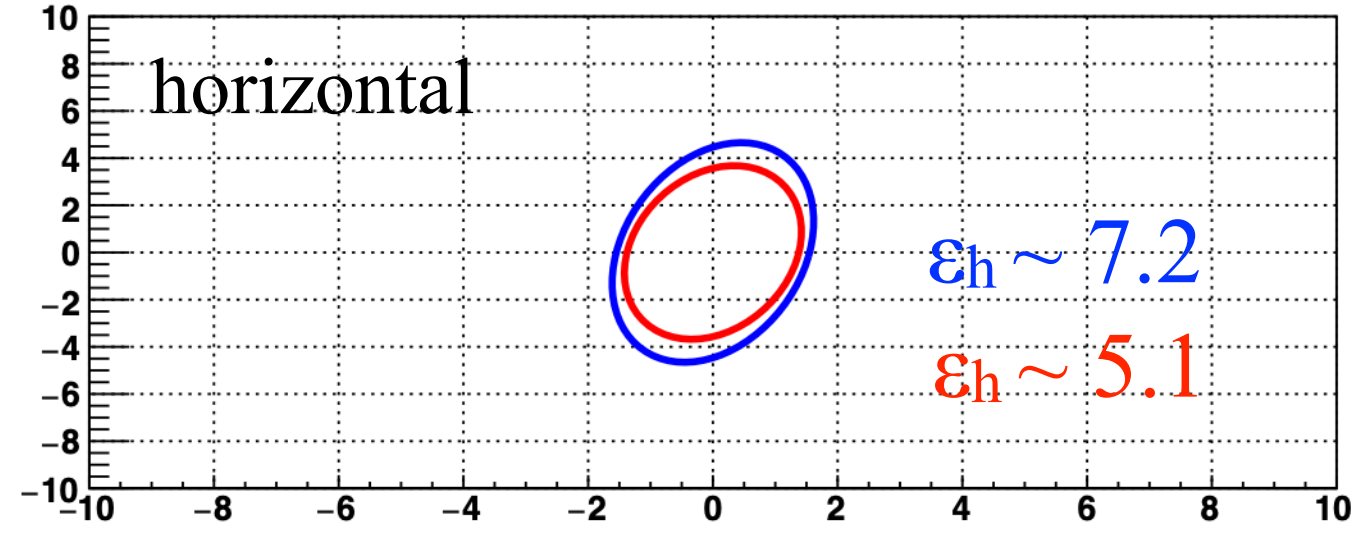
$$|\epsilon_{\text{asym}}| \equiv \left| \frac{\epsilon_h - \epsilon_v}{\epsilon_h + \epsilon_v} \right| \leq 0.1. \quad \text{※ } \Delta\epsilon \sim 20\% \text{ in maximum}$$

- (2) Utilize profile monitor data in the fitting  
Quadrupole momentums  $\sigma_x^2 - \sigma_y^2$  have less sensitivity for absolute beam size.  
 $\rightarrow$  Additional beam size in one point will improve the fitting result.



# Improvement of sensitivity for beam emittance

Phase Ellipse at profile monitor e00  
with double integral method  
+ (1), (2)



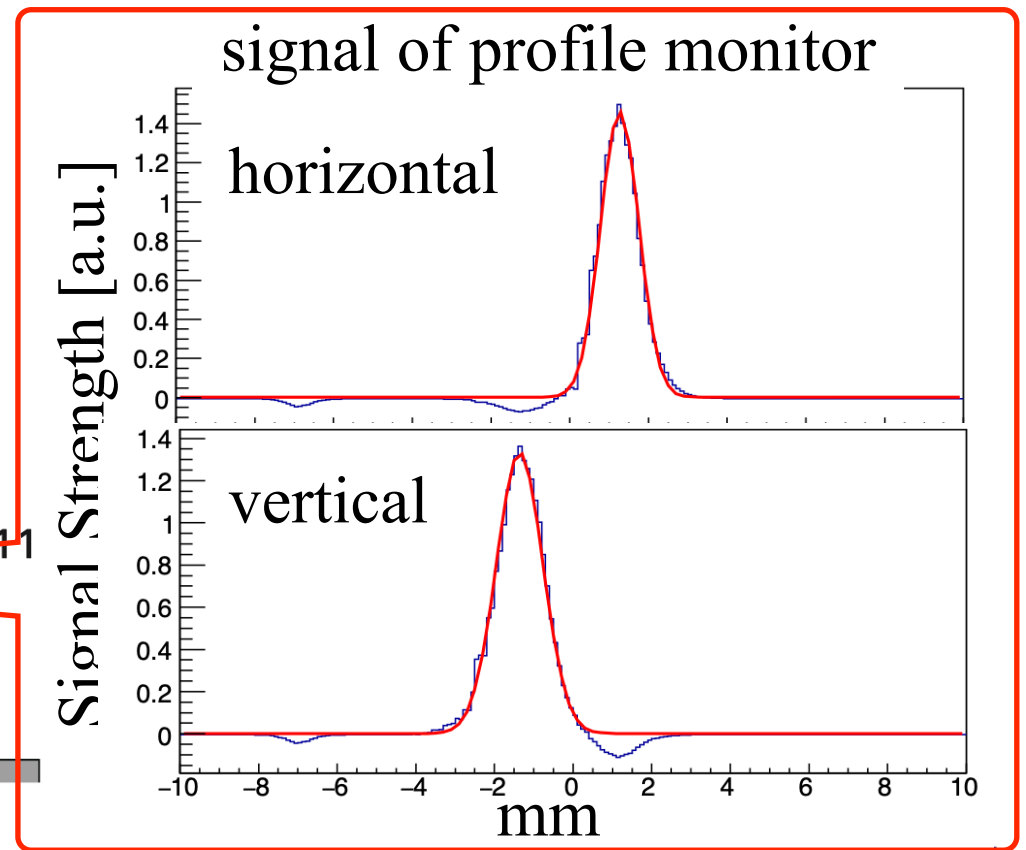
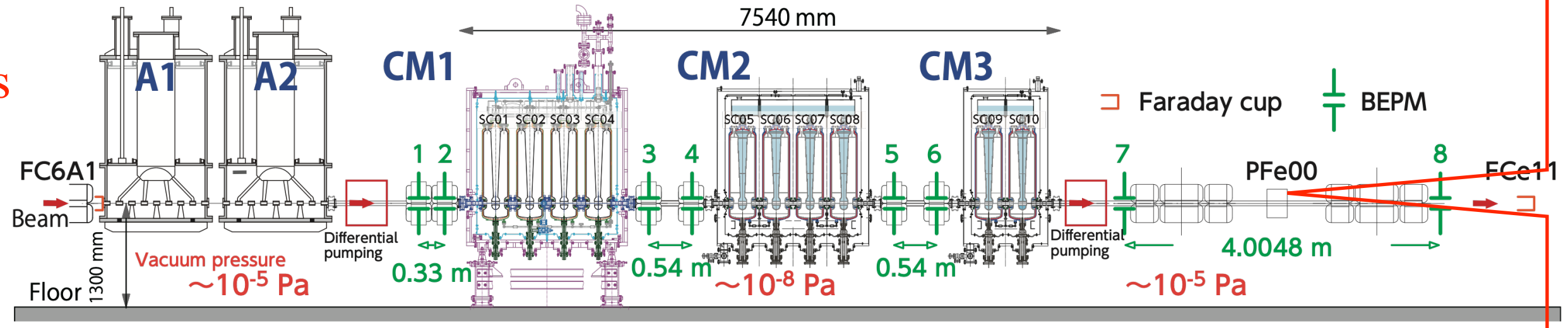
Result of Q-scan  
Result of BEPM + PF analysis

Improved so much!!

- (1) Limitation of balance between  $\epsilon_h / \epsilon_v$  ratio between  $\epsilon_h$  and  $\epsilon_v \rightarrow$  expected to be robust in some range  
Fit is performed under the following condition,

$$|\epsilon_{\text{asym}}| \equiv \left| \frac{\epsilon_h - \epsilon_v}{\epsilon_h + \epsilon_v} \right| \leq 0.1. \quad \text{※ } \Delta\epsilon \sim 20\% \text{ in maximum}$$

- (2) Utilize profile monitor data in the fitting  
Quadrupole momentums  $\sigma_x^2 - \sigma_y^2$  have less sensitivity for absolute beam size.  
 $\rightarrow$  Additional beam size in one point will improve the fitting result.





# Operation procedure of the improved method (plan)

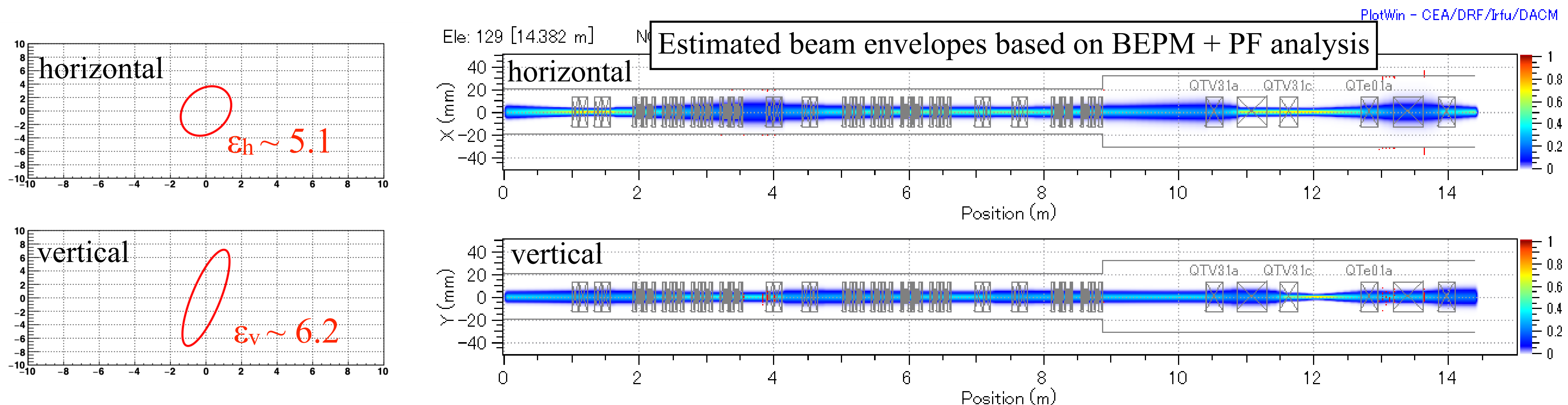
## (1) Beginning of the beam supply

- Measure the beam emittance by Q-scan and check balance between  $\epsilon_h / \epsilon_v$

## (2) During the beam supply

- Check the beam size by profile monitors once a day
- Calculate transfer matrix in the beam line from the setting values
- Continuous display of the beam envelope during beam supply

→ **“semi” non-destructive beam envelope monitor**



# Outline

1. Introduction: SRILAC and B(E)PMs
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6. Future Outlook and Summary

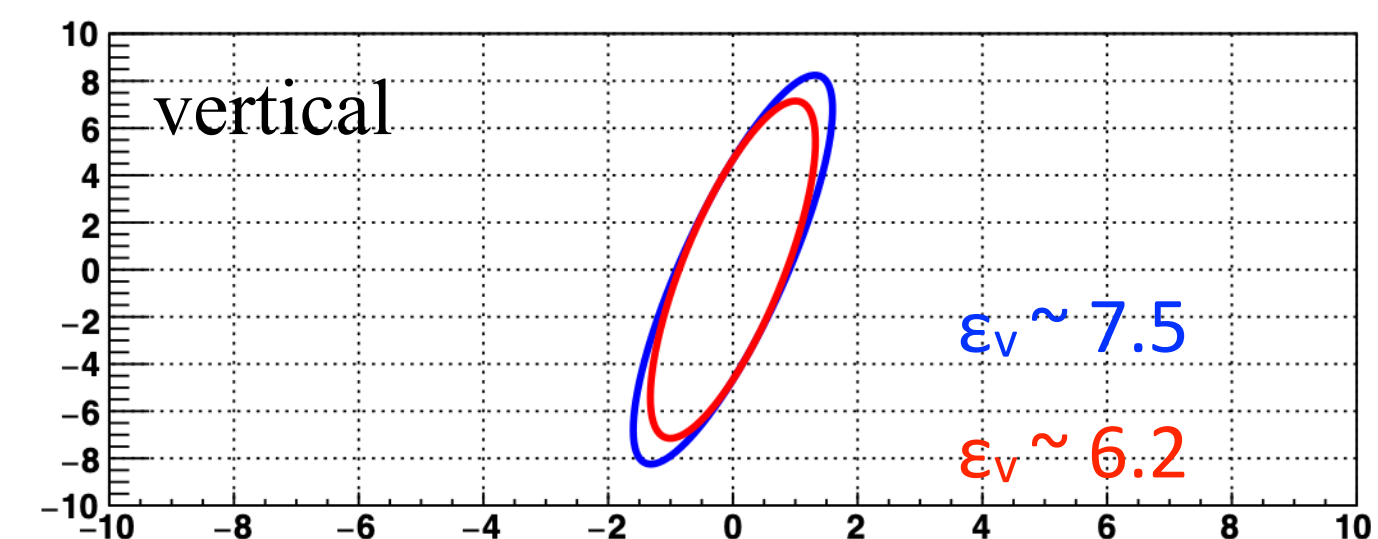
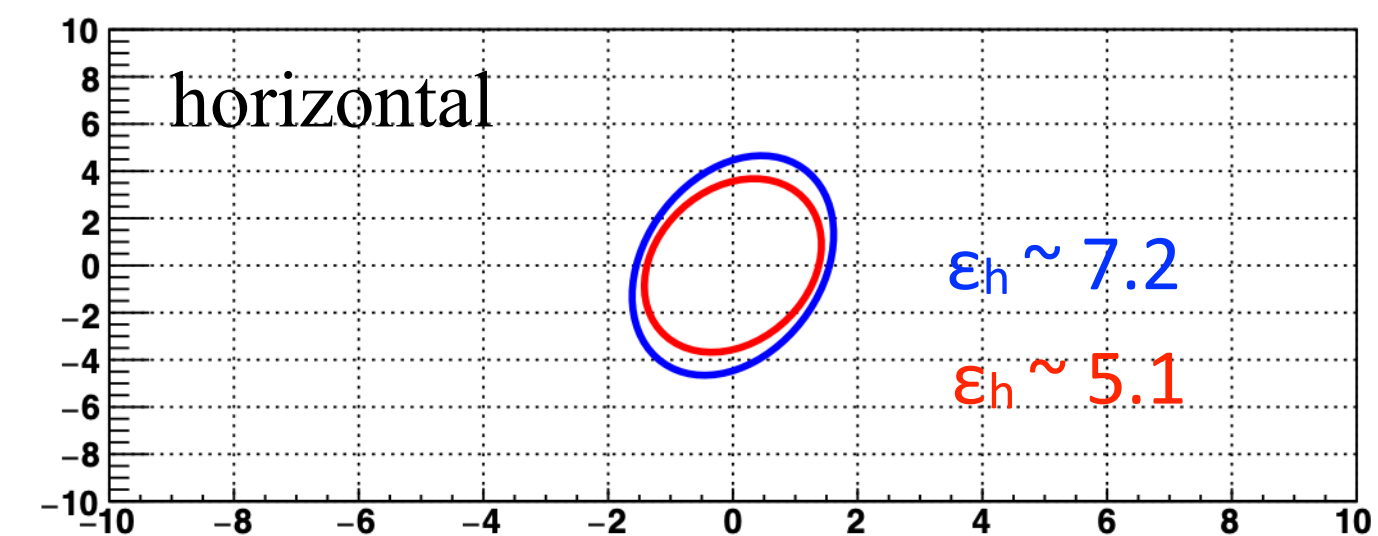
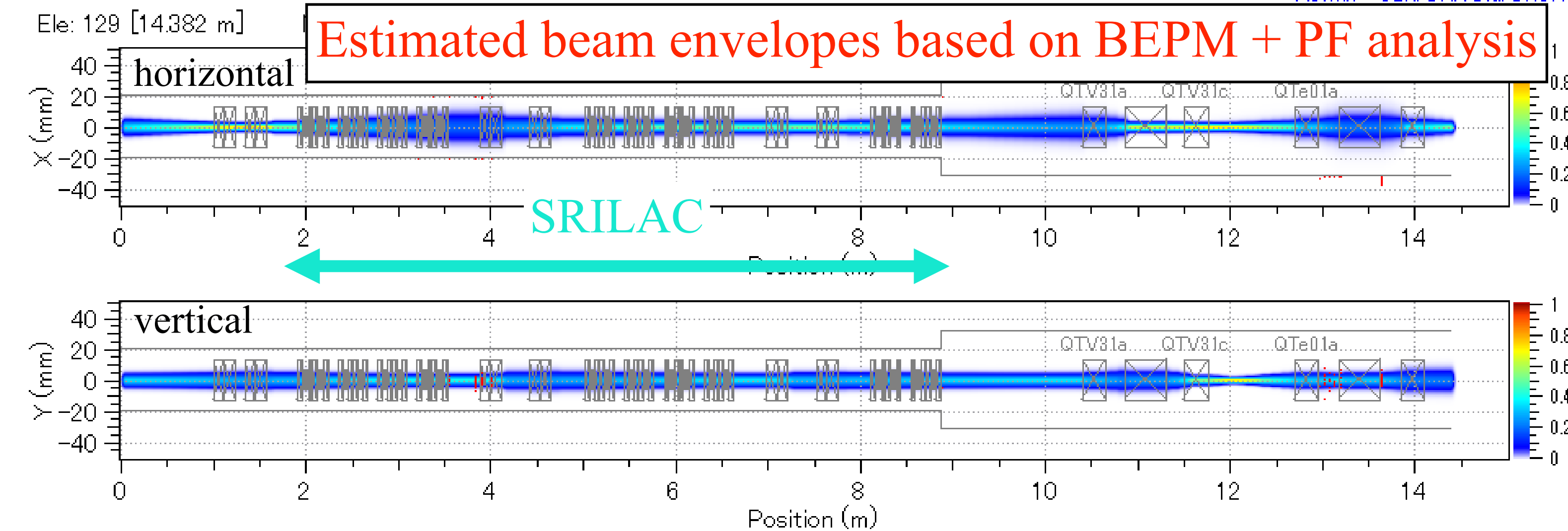


# Examples of estimated beam envelopes

2022 Nov. 5th

PlotWin - CEA/DRF/Ifu/DACM

Estimated beam envelopes based on BEPM + PF analysis



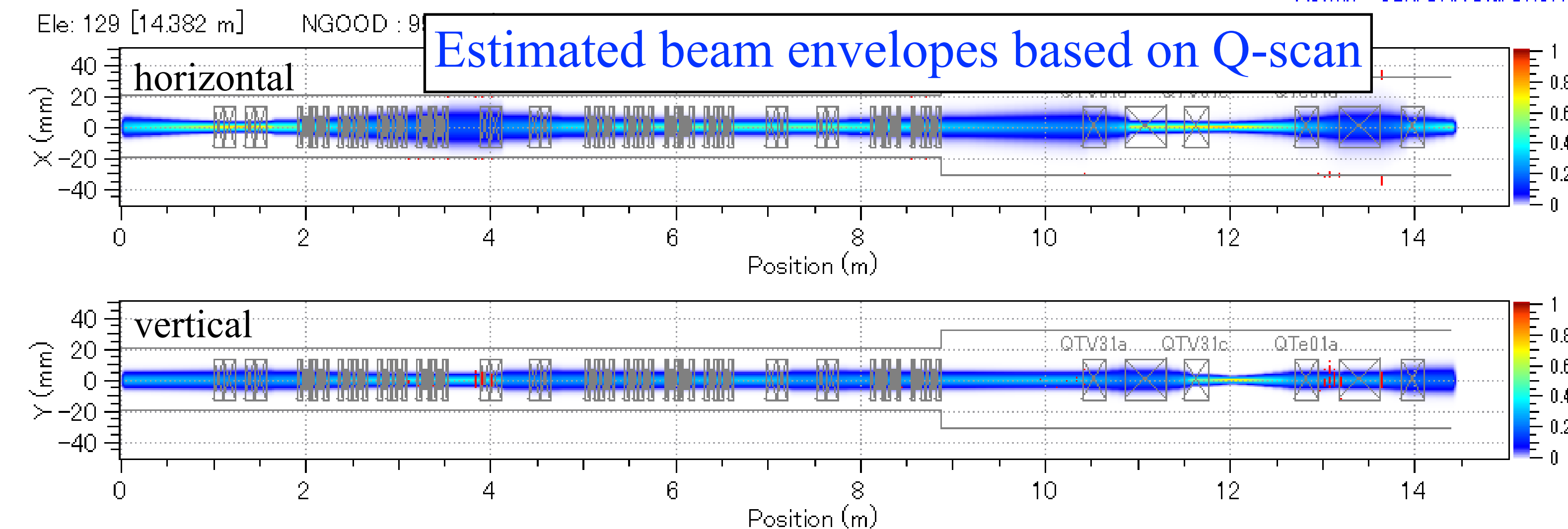
Result of Q-scan

Result of BEPM + PF analysis

While the absolute  $\epsilon$  tends to be small,  
beam envelope shape is well reproduced.

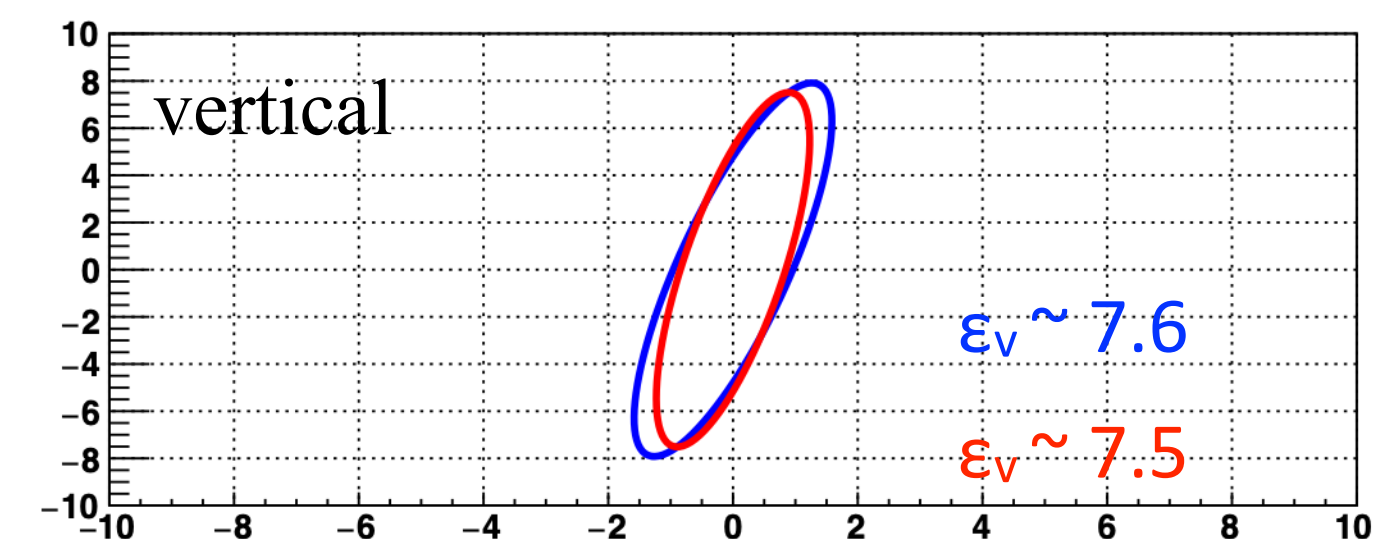
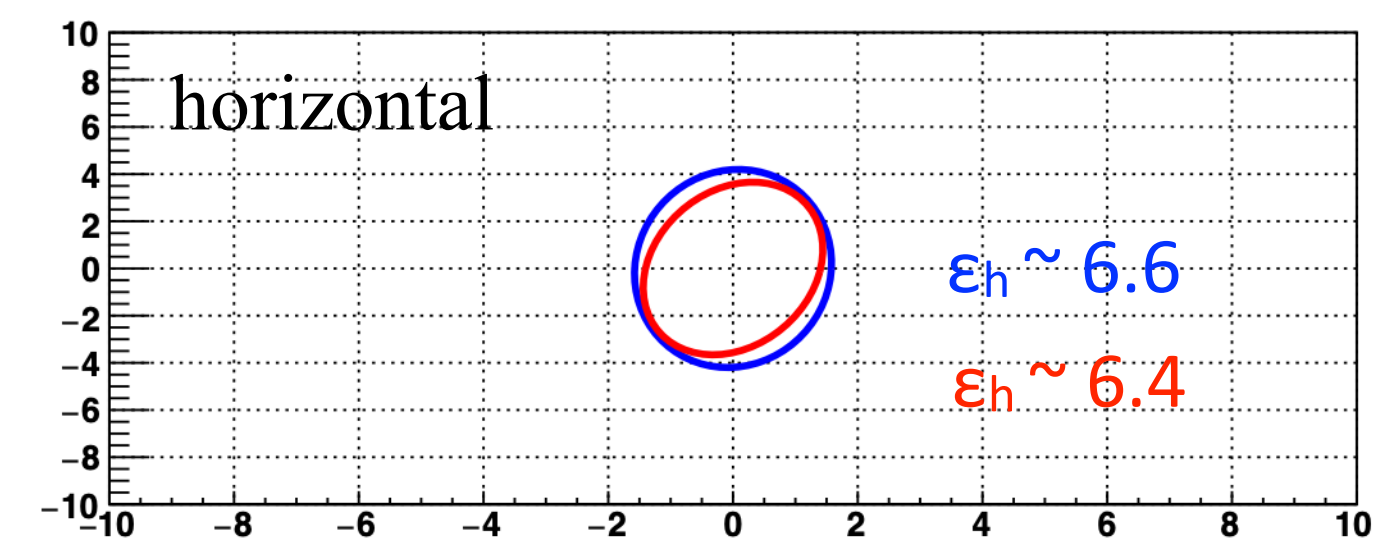
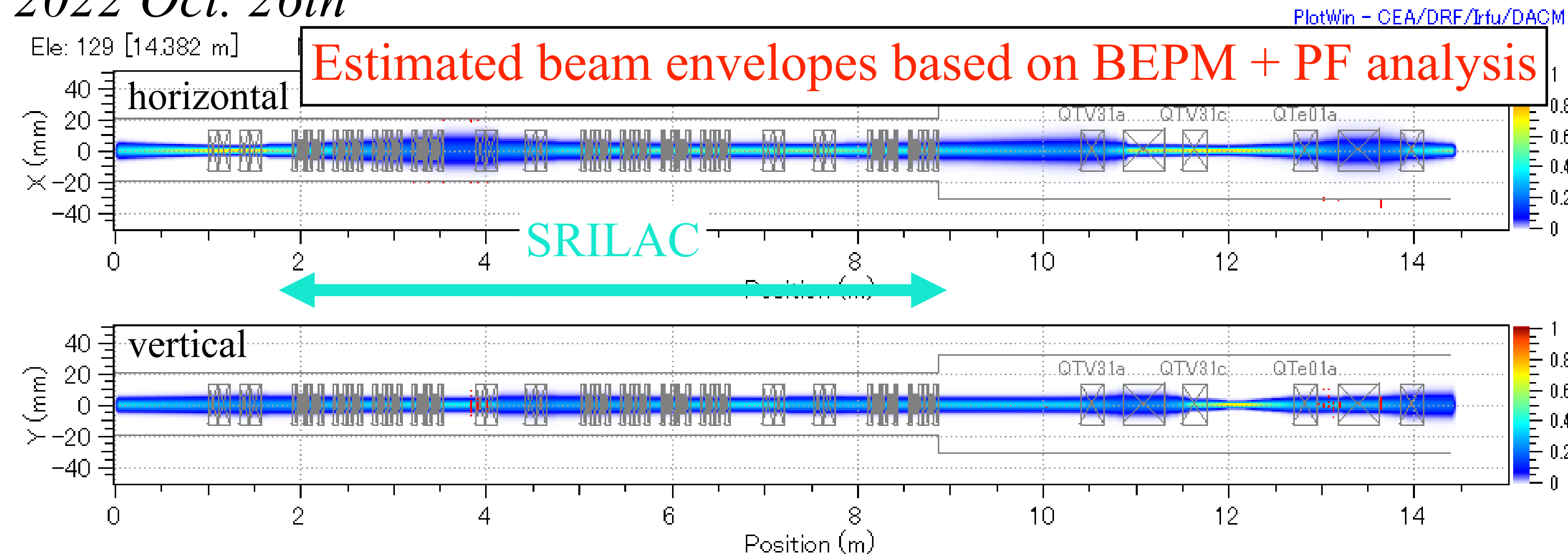
PlotWin - CEA/DRF/Ifu/DACM

Estimated beam envelopes based on Q-scan



# Examples of estimated beam envelopes

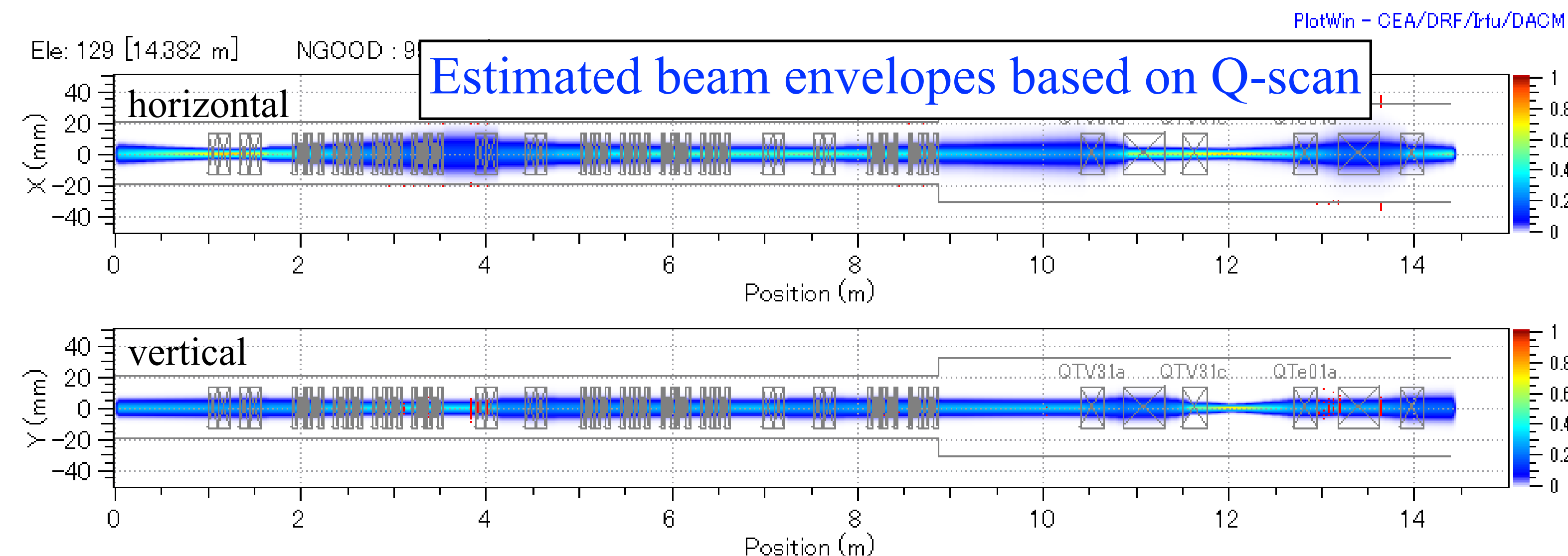
2022 Oct. 26th



Result of Q-scan

Result of BEPM + PF analysis

In this case, emittances are also well reproduced by BEPM + PF data.



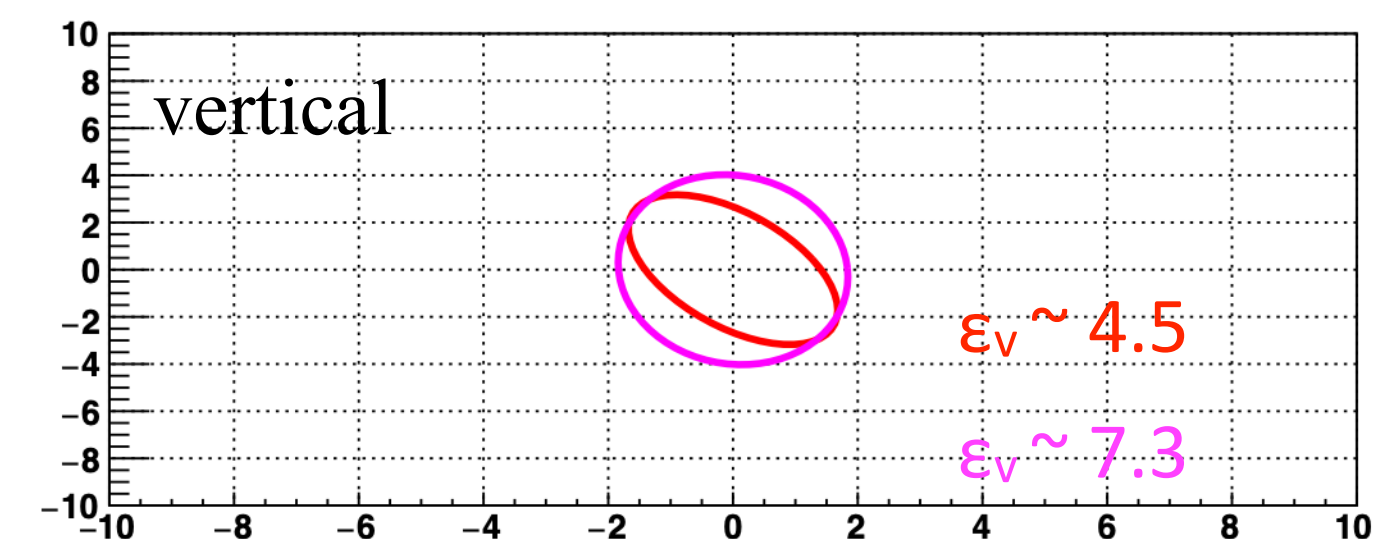
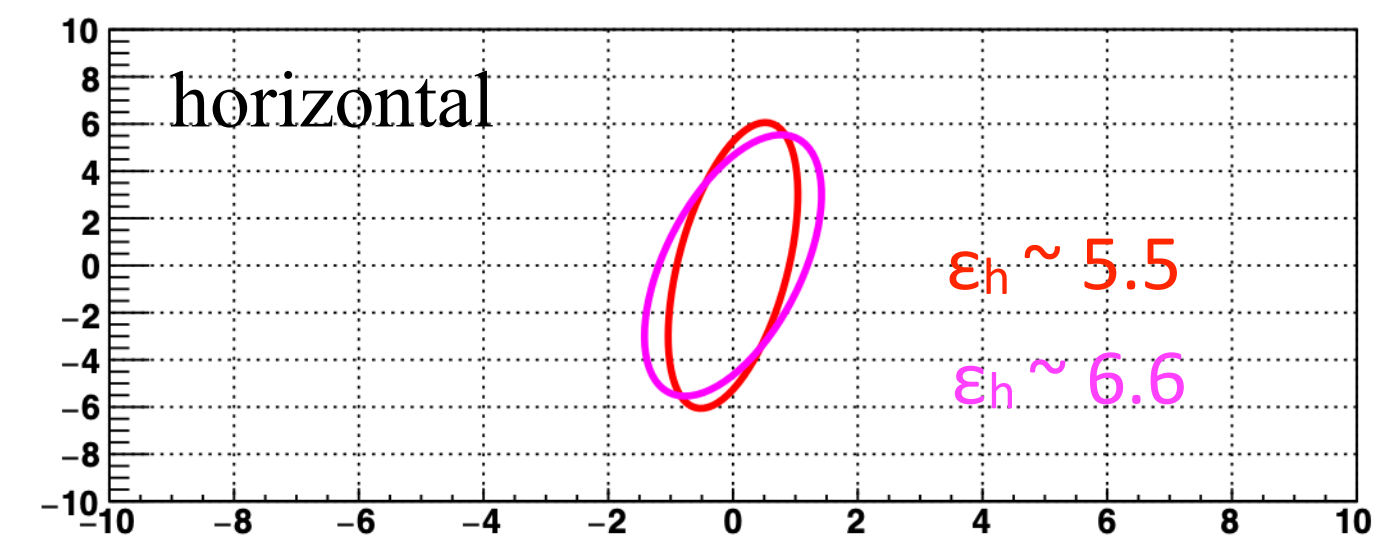
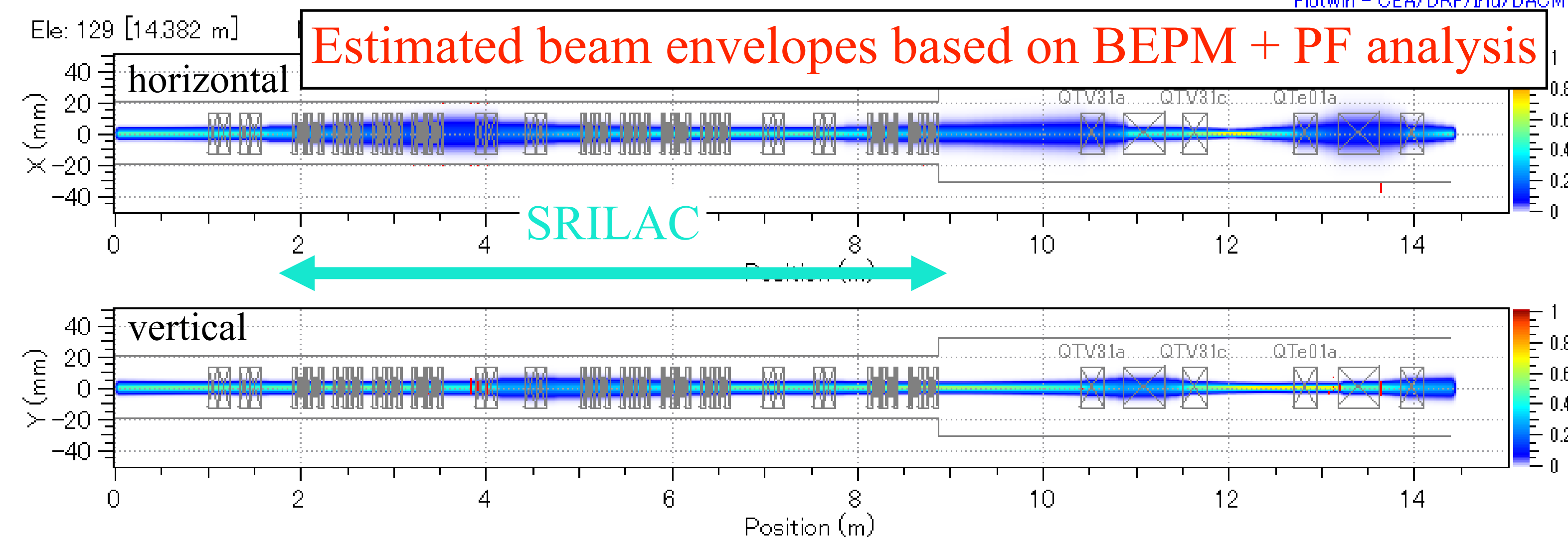


# Examples of estimated beam envelopes

2023 June 16th

※ These analysis based on bias factor correction method

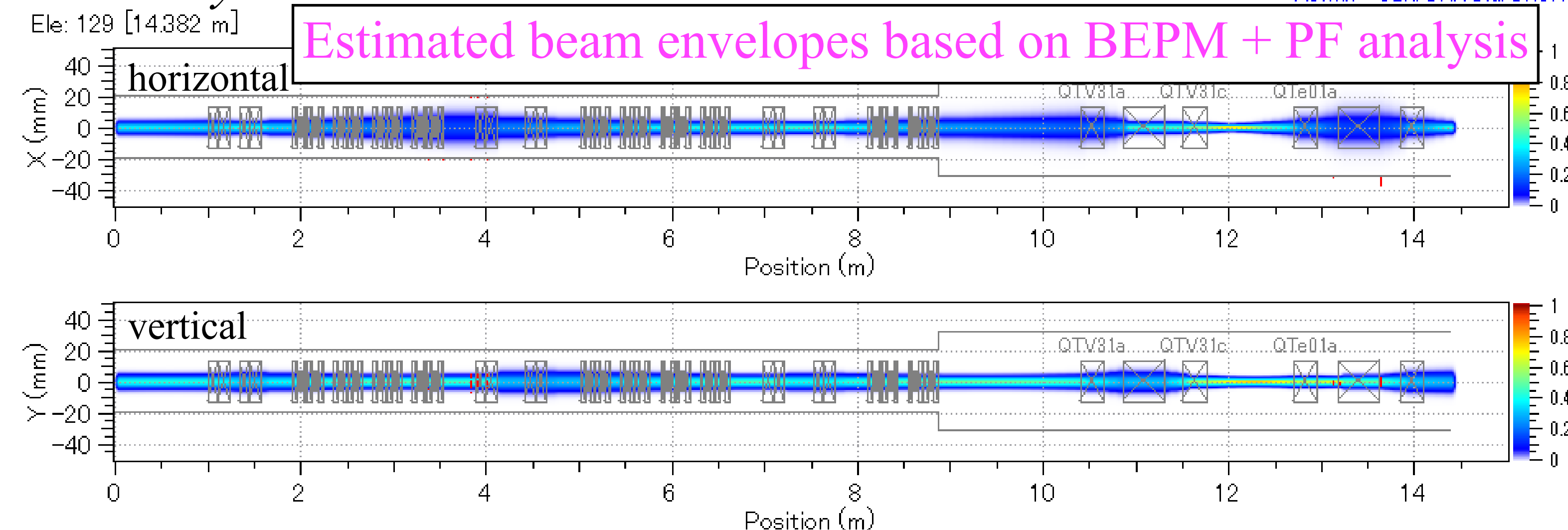
PlotWin - CEA/DRF/Ifu/DACM



Result of BEPM + PF analysis in June 16th  
Result of BEPM + PF analysis in July 5th

2023 July 5th

PlotWin - CEA/DRF/Ifu/DACM



Estimated beam envelope has slightly changed in a few weeks during beam supply.  
→ We need to check this change is real or not...

# Outline

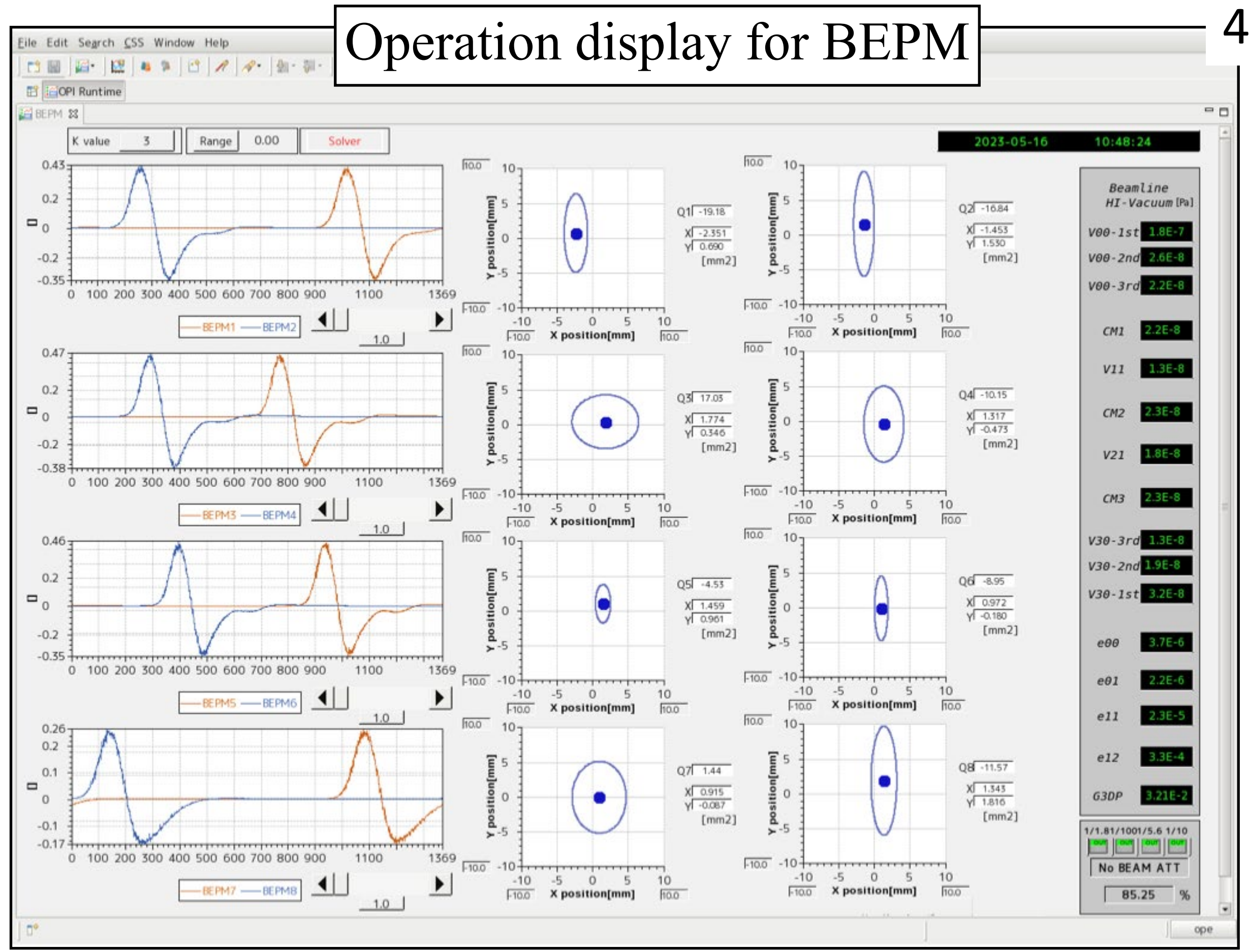
1. Introduction: SRILAC and B(E)PMs
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# Operation display for BEPM

## 6. Future outlook and Summary

- We developed “semi” non-destructive beam envelope measurement using BPMs.
- With double integration of the signals, we obtained consistent result with Q-scan method.
- So far information from some destructive monitors are essential to estimate accurately.
- An improved program for the measurement will be introduced in the coming beam supply series.



### Remained Issue:

- Estimation uncertainty of the analysis
- Introduction of this system to other beam line
- Further development w/o wire scanner info.  
(Location of BEPM considering optics etc....)

Beam envelope will be displayed simultaneously in future

